Game-Theoretic Methods for Security Investment in Cyber-physical Control Systems



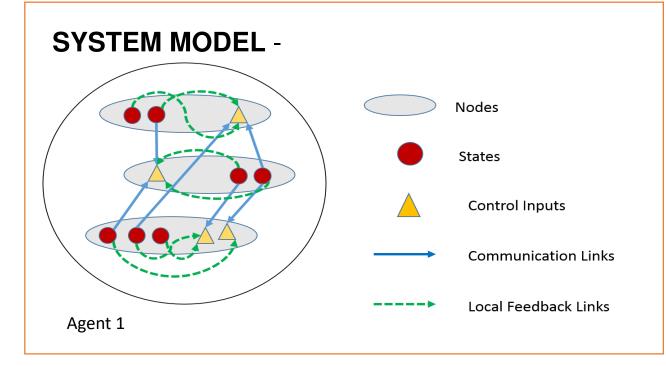
Overview

PROBLEM OBJECTIVE

- Security of control systems is becoming a pivotal concern in critical national infrastructures.
- Identify critical nodes for protecting against cyber-attacks
- Maintain stability and control objectives
- Relate control performance to protection and attack resources
- Attacker and Defender's resource allocation

2. SYSTEM DESCRIPTION

Consider a multi-agent dynamic system with *n* nodes.



Let us consider the linear dynamic system with n

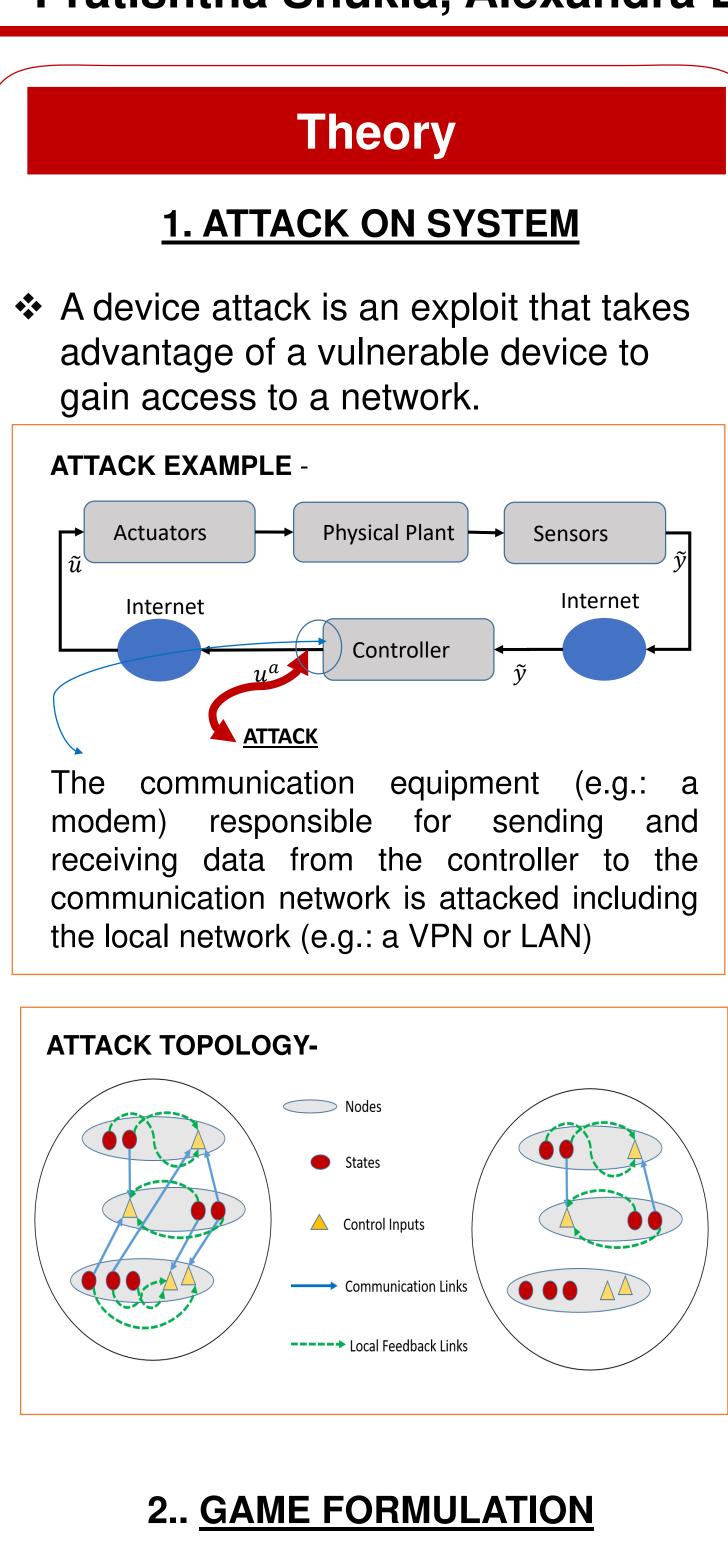
$$\dot{x(t)} = Ax(t) + Bu(t)$$
$$y = Cx(t)$$

✤ We assume linear static feedback is u(t) = -Kx(t)employed,

The LQR Objective

$$V = \int [x^T(t)Qx(t) + u^T(t)Ru(t)]dt$$
,

Where $Q \ge 0$, R > 0



Pratishtha Shukla, Alexandra Duel-Hallen and Aranya Chakrabortty

The attacker tries to cause a noticeable amount of Loss in the system by increasing the energy of the system.

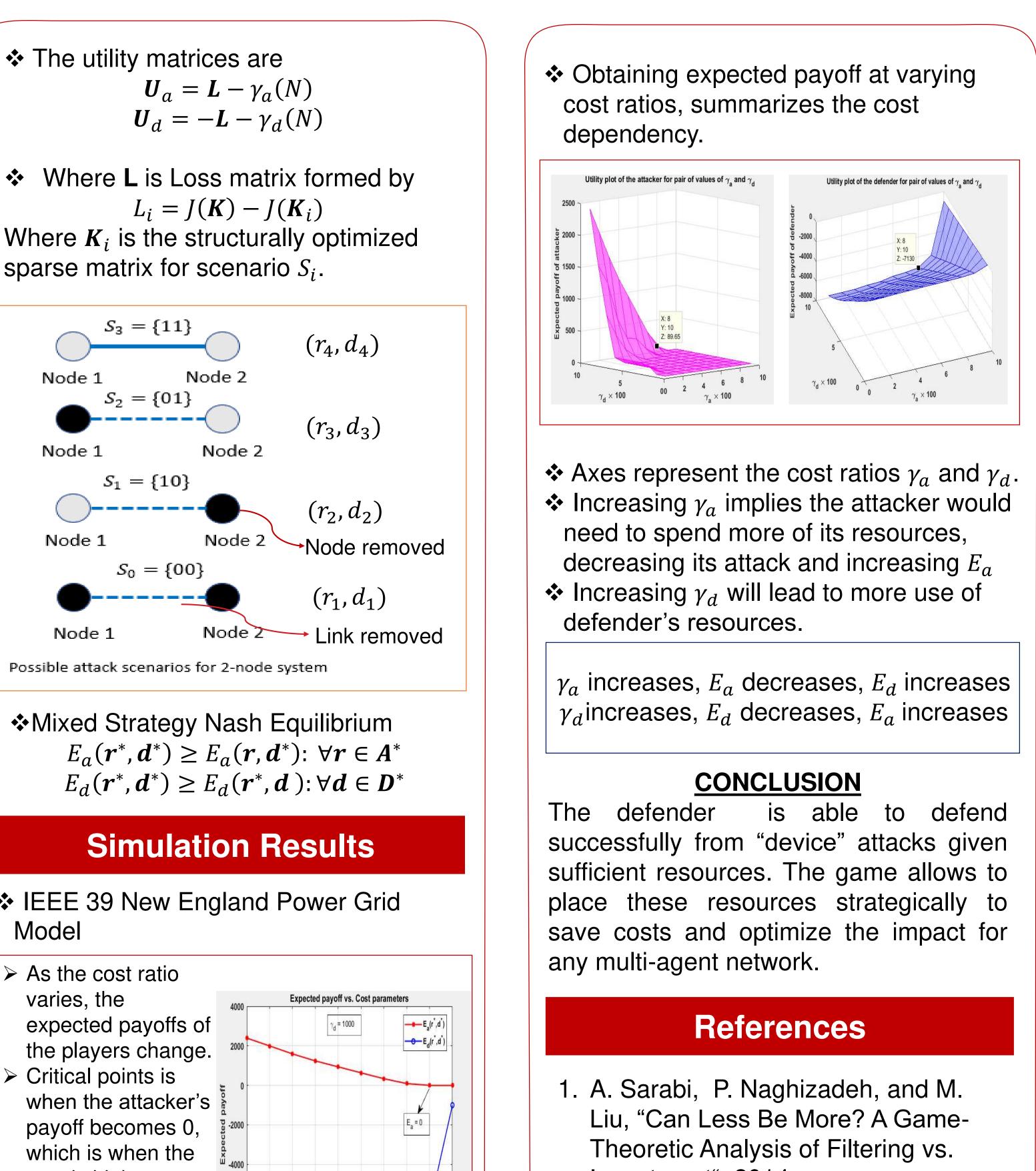
With attacker and defender mixed strategies form the sets A^* , D^* , the expected payoffs of the players become $E_a(\mathbf{r}, \mathbf{d}) = \mathbf{r} U_a \mathbf{d}^T$ $E_d(\mathbf{r}, \mathbf{d}) = \mathbf{r} \mathbf{U}_{\mathbf{d}} \mathbf{d}^T$

The utility matrices are

$$\boldsymbol{U}_d = -\boldsymbol{L} - \boldsymbol{\gamma}_d(\boldsymbol{N})$$

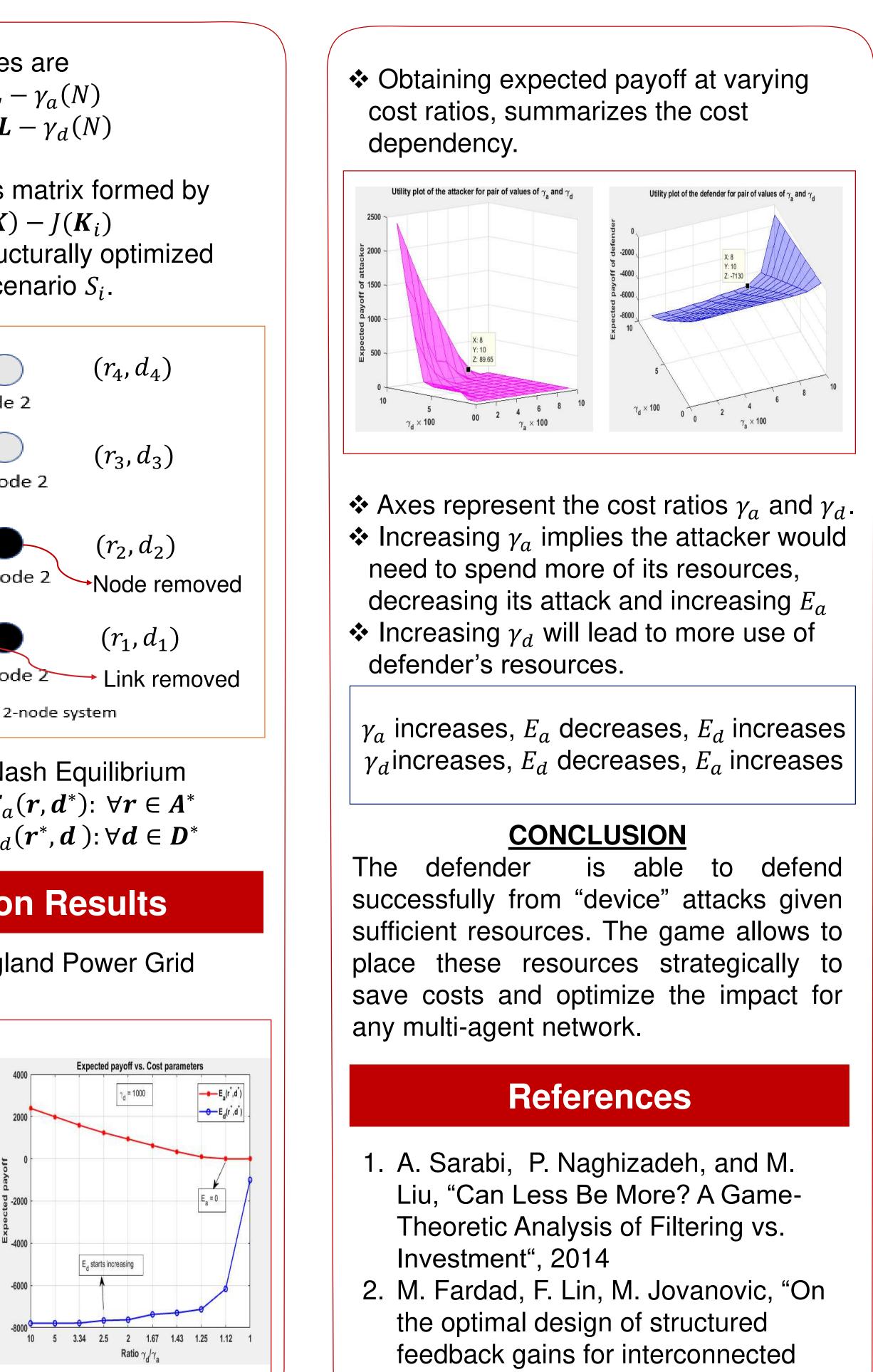
 $L_i = J(\mathbf{K}) - J(\mathbf{K}_i)$

sparse matrix for scenario S_i .



Possible attack scenarios for 2-node system

- IEEE 39 New England Power Grid Model
- \succ As the cost ratio
- Critical points is cost is high.
- At this point onwards, the defense investment gives us critical nodes



systems", 2009.

NC STATE

JNIVERSITY