

# Low-inertia Grids and the Role of Oscillator-based Controllers

Brian Johnson

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**University of Washington**

**Department of Electrical and Computer Engineering**

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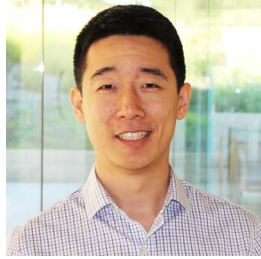


**ELECTRICAL ENGINEERING**  

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**UNIVERSITY *of* WASHINGTON**

# Collaborators



Yashen  
Lin



Sairaj  
Dhople



Francesco  
Bullo



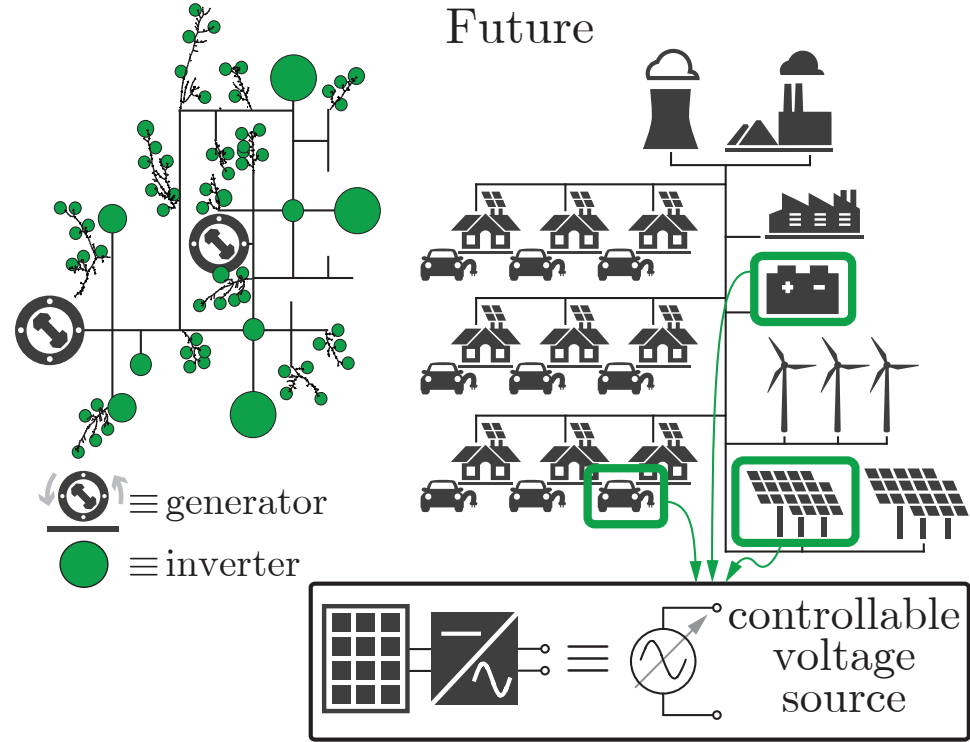
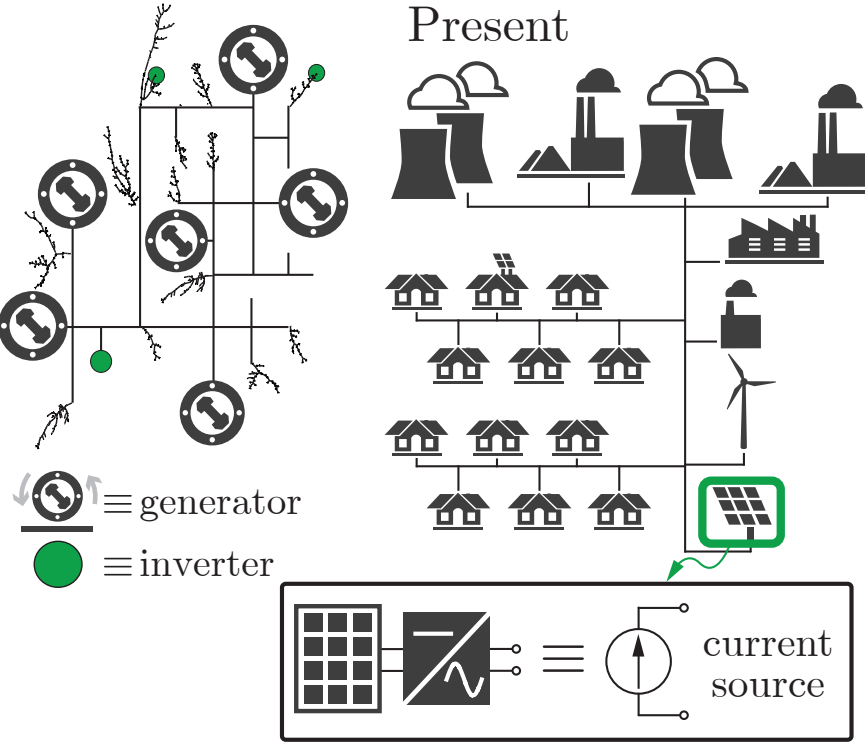
## Funding:



# Evolution of the Grid

Present

Future



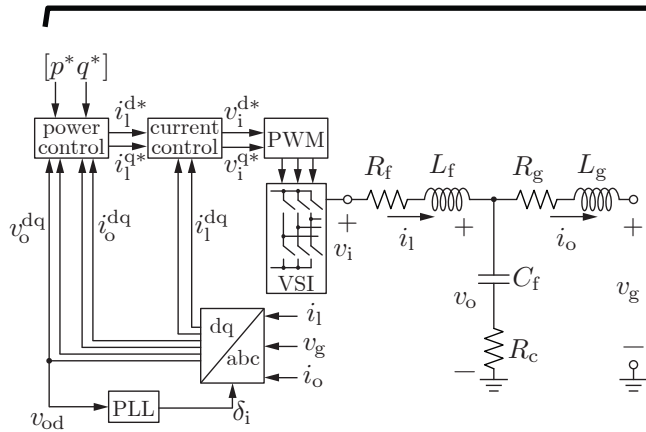
Grid-following  
controls

to next-generation  
grid-forming controls

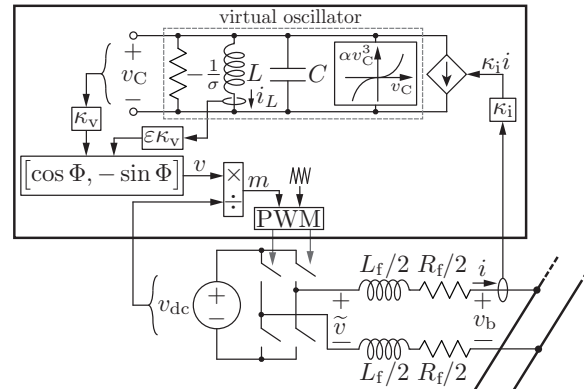


# Controllers Under Consideration

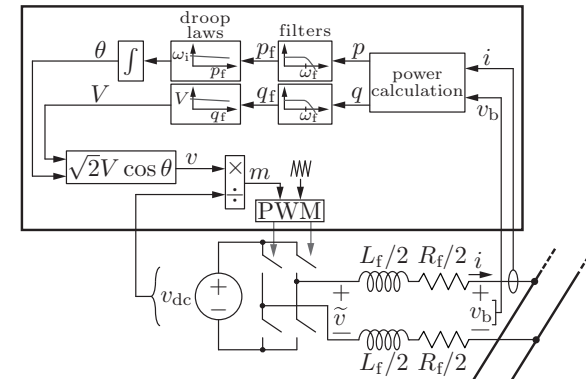
Discussed today



Grid-following:  
Current control with PLL



Grid-forming:  
Virtual oscillator control

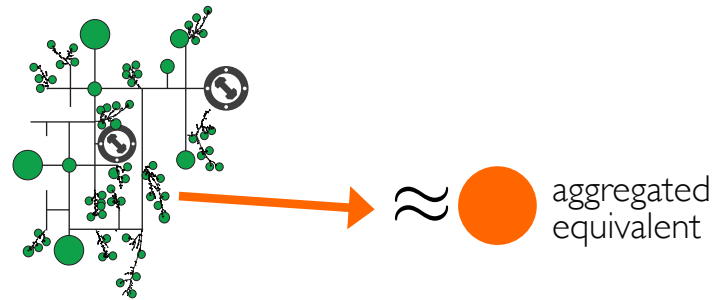


Grid-forming:  
Droop control

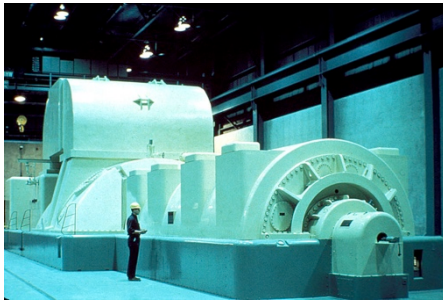
Have similarities

# Outline

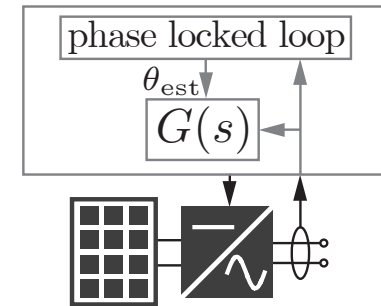
1. How do we solve the modeling complexity problem?



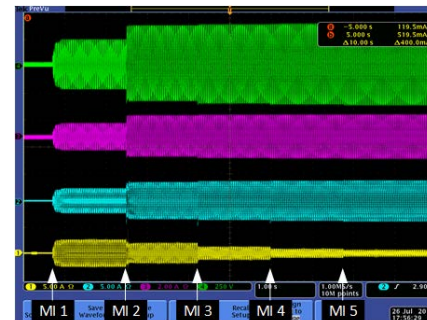
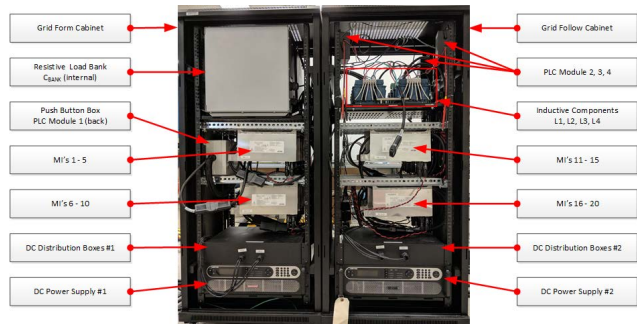
2. Is there an upper limit for inverter penetration before stability is lost?



How many machines can we replace with electronics?

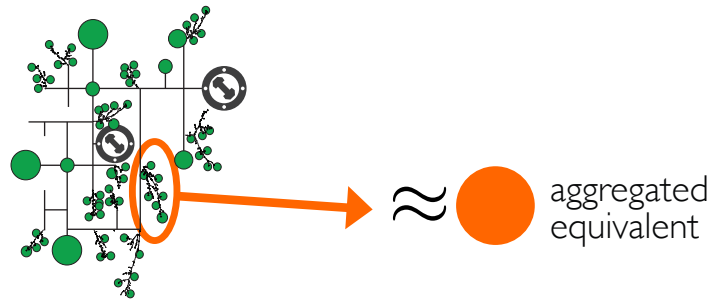


3. A **hardware** demo with 20 commercial inverters.

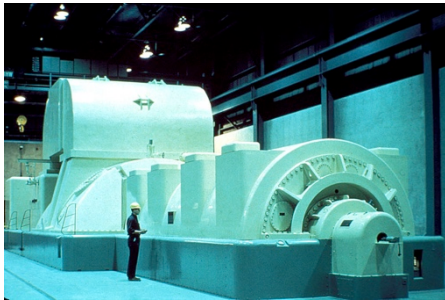


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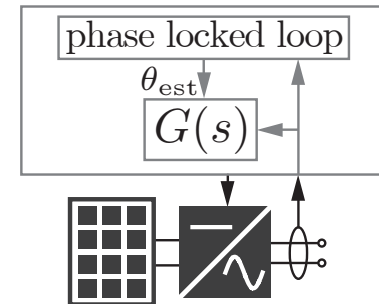
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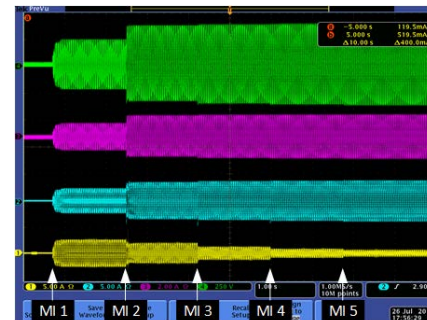
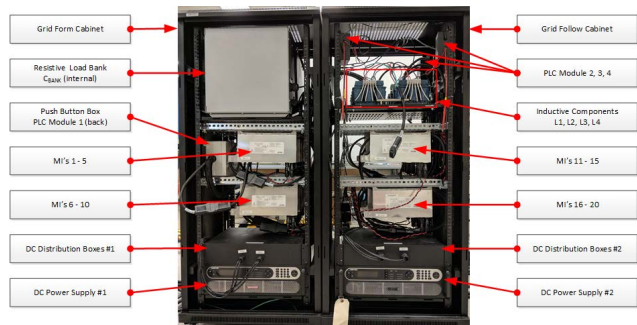
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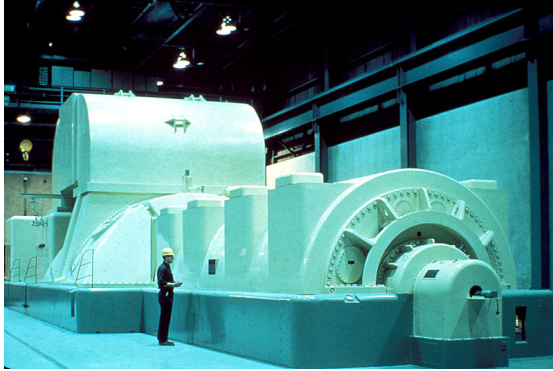


3. A **hardware** demo with 20 commercial inverters.



# The Scaling Problem

A large disparity in ratings



100's of MVA

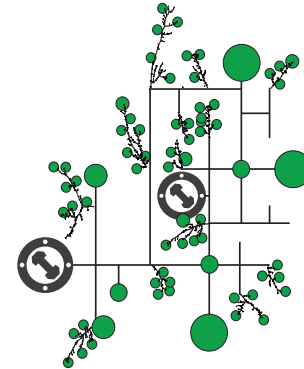
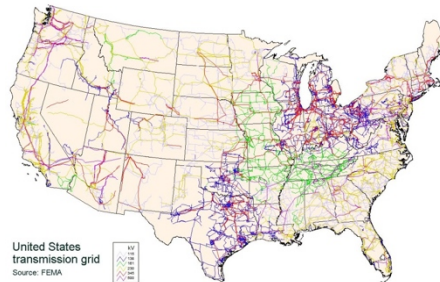
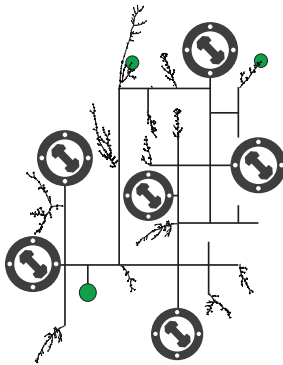


,



100's of VA – 100's of kVA

... implies a larger number of generating devices to satisfy load



From ~7,500 power plants



To millions of inverters?

# Motivational Example: Oahu



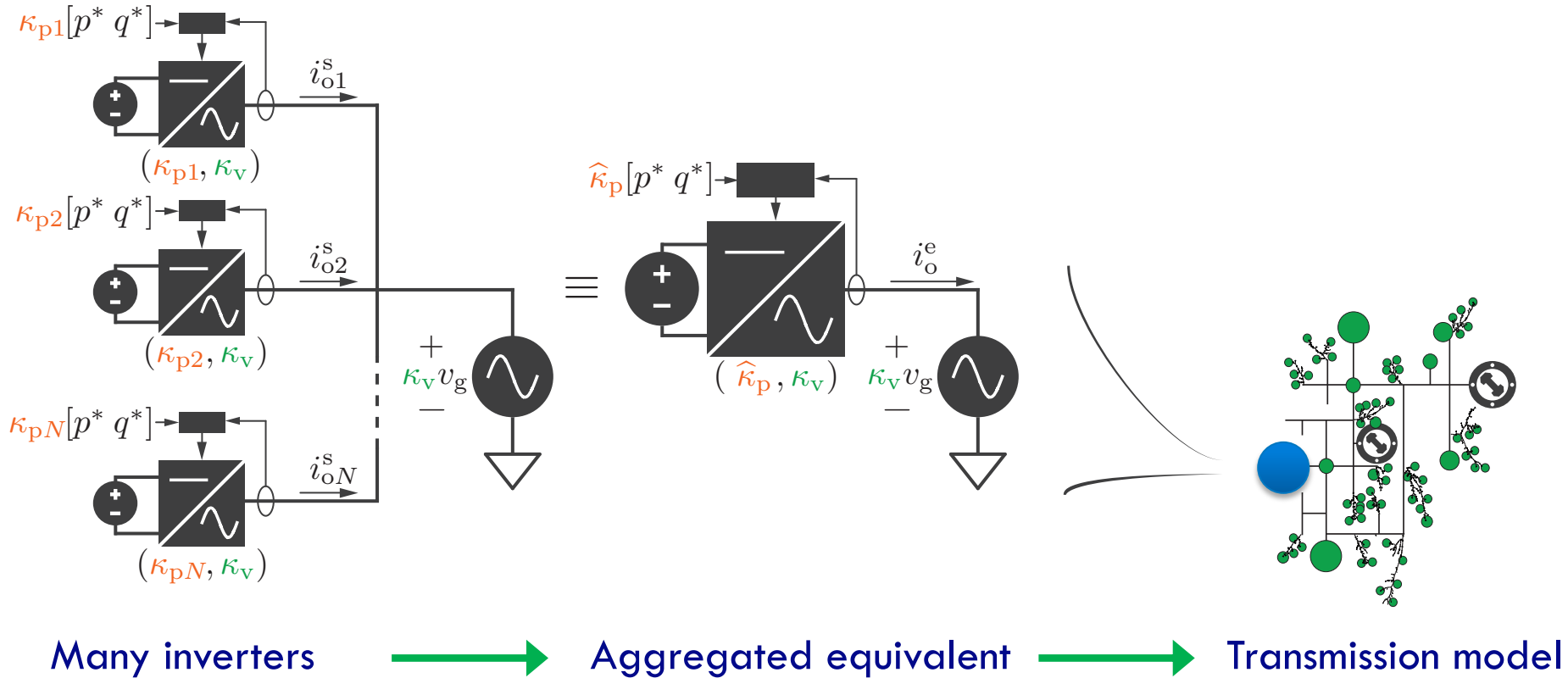
An island of 950,000 people and 800,000 Enphase microinverters



“800,000 Microinverters Remotely Retrofitted on Oahu in One Day.” <http://spectrum.ieee.org/energywise/green-tech/solar/in-one-day-800000-microinverters-remotely-retrofitted-on-oahu>.

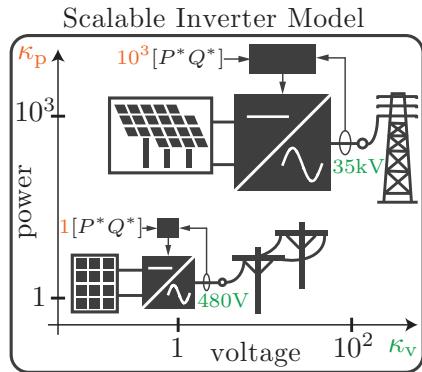


# Our Solution: Aggregation

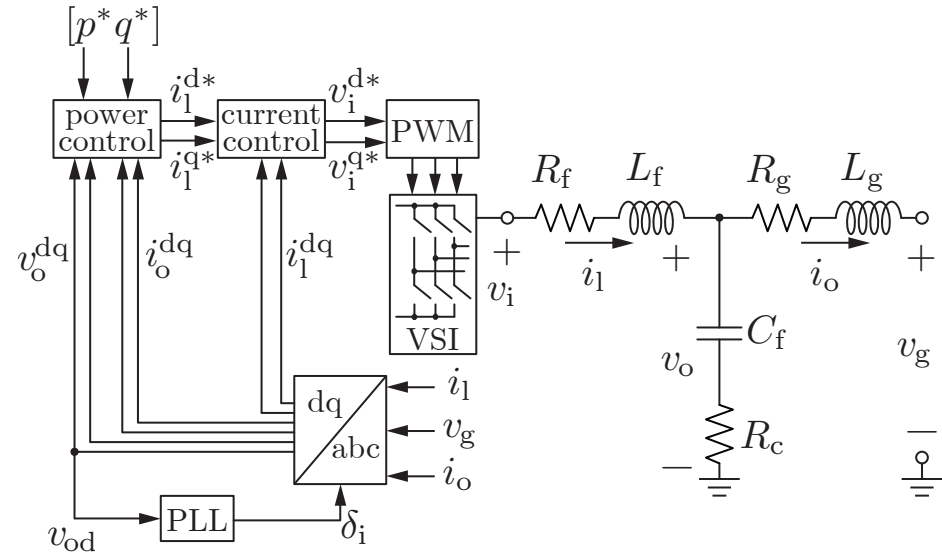


# Foundation of Aggregation Approach: Scaling Laws

Introduce power and voltage scaling factors,  $\kappa_p$  and  $\kappa_v$

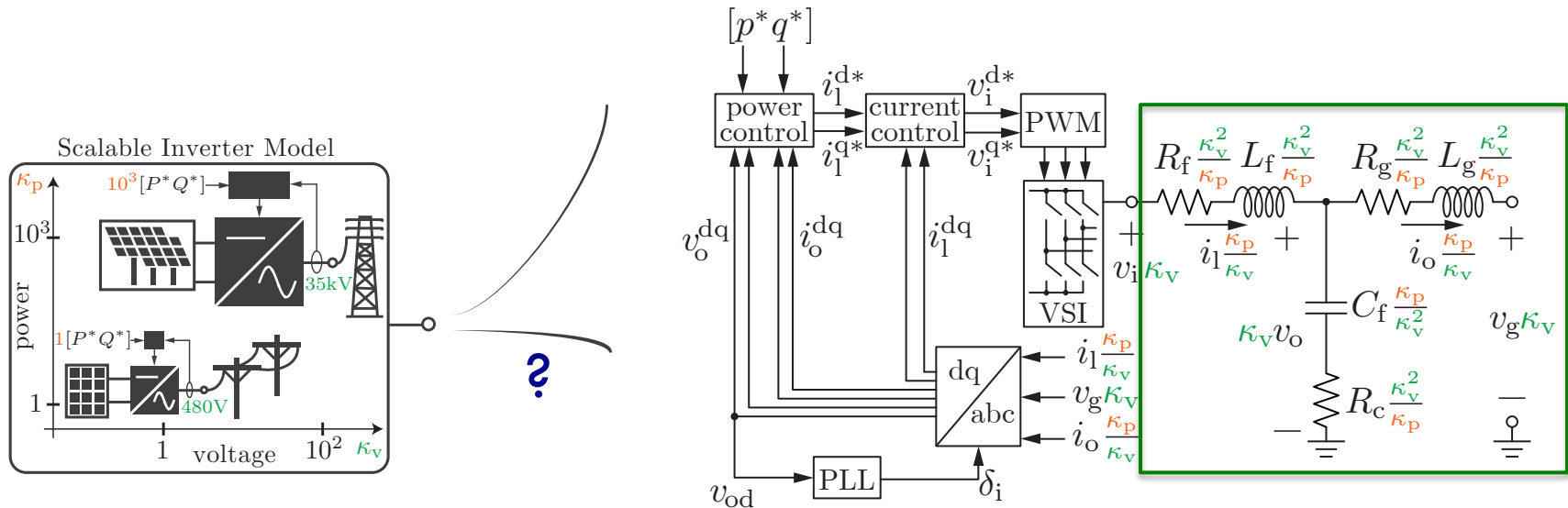


?



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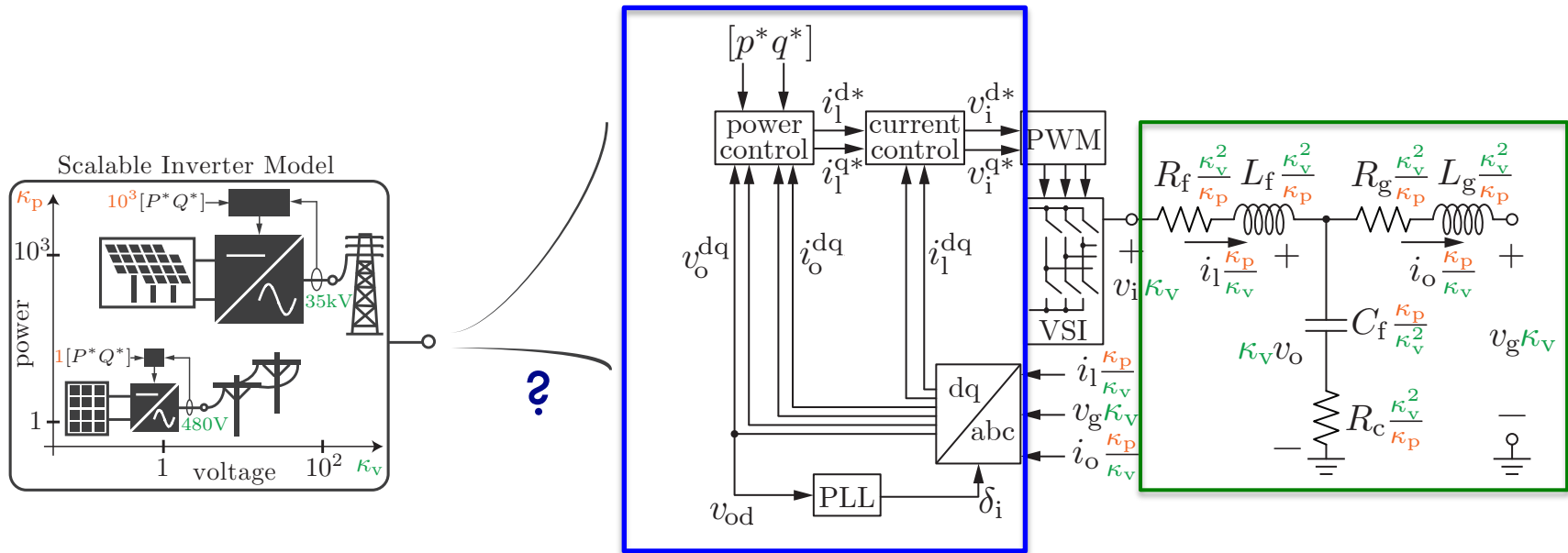
- Based on power electronics & controls rules of thumb

- Fixed voltage drop across filter

- Fixed total harmonic distortion across ratings:  $\frac{\text{switching ripple}}{I_{\text{rated}}} = \text{constant}$

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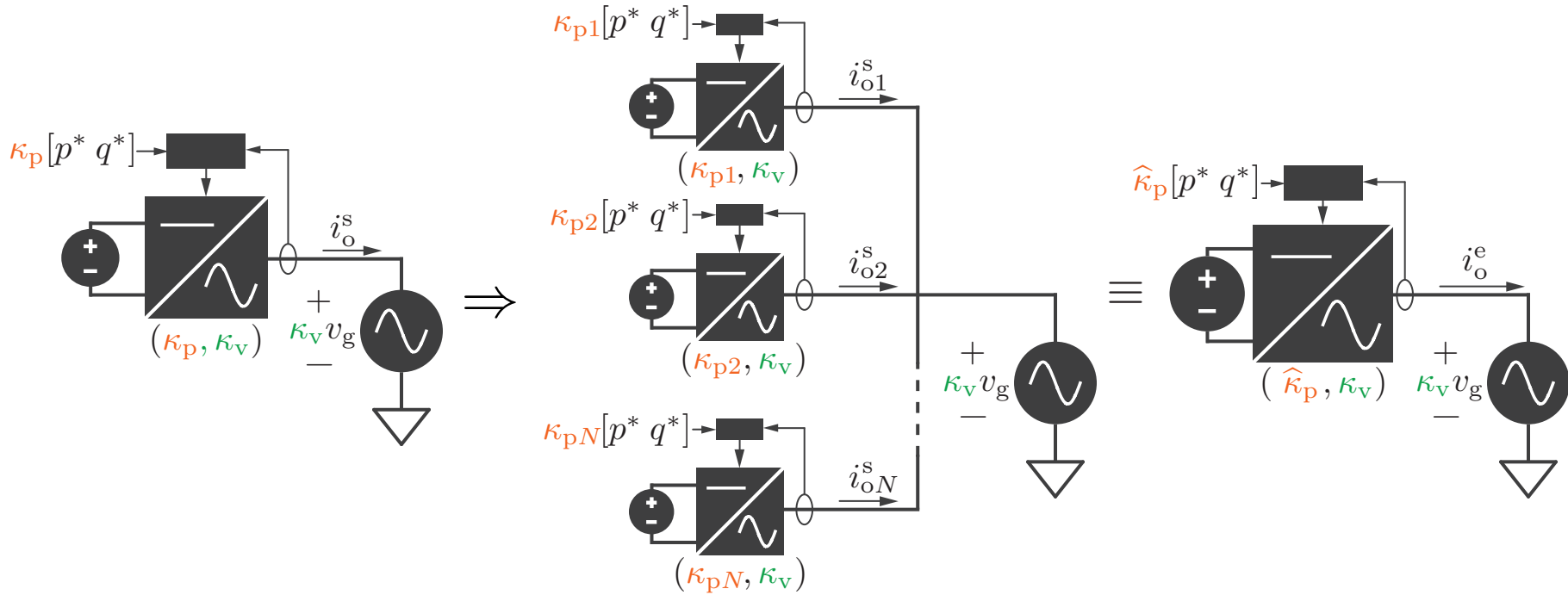
Introduce power and voltage scaling factors,  $\kappa_p$  and  $\kappa_v$



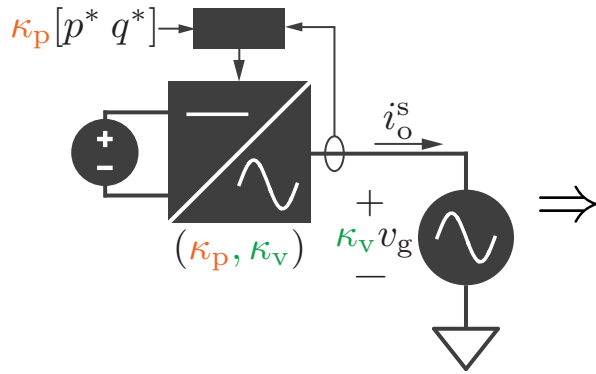
- Based on power electronics & controls rules of thumb

- Fixed voltage drop across filter
- Fixed total harmonic distortion across ratings:  $\frac{\text{switching ripple}}{I_{\text{rated}}} = \text{constant}$
- Preserve closed-loop response with scaled control gains

# Scaling Laws and Aggregation

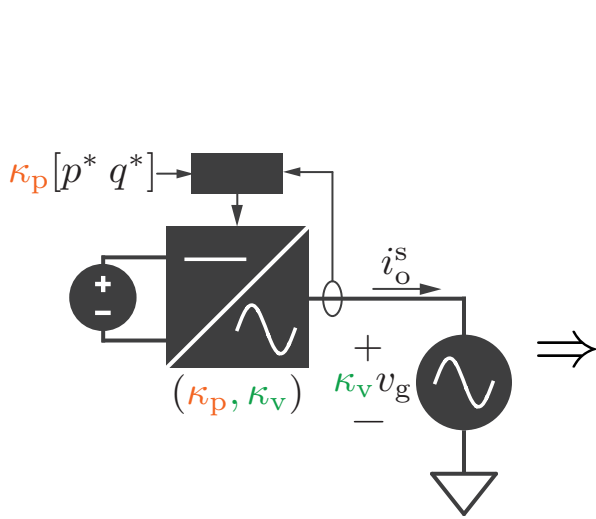


# Scaling Laws and Aggregation

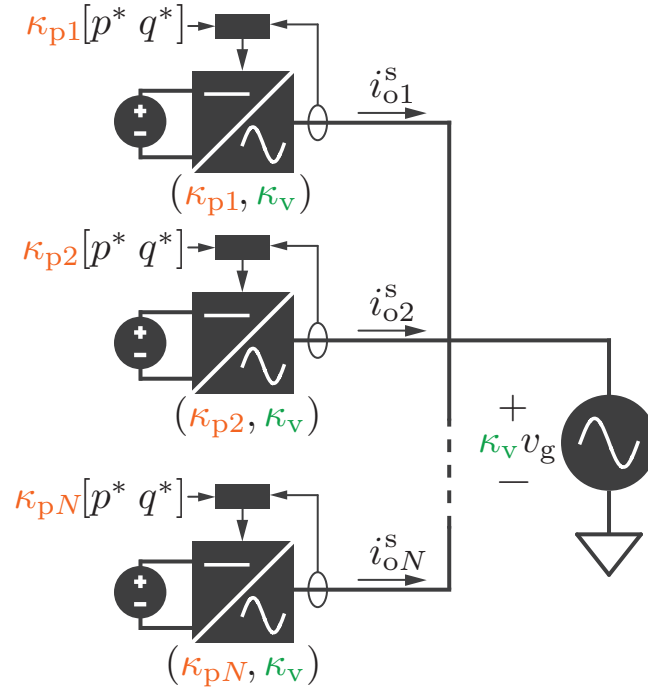


(a) Single **grid following** or **grid forming** inverter

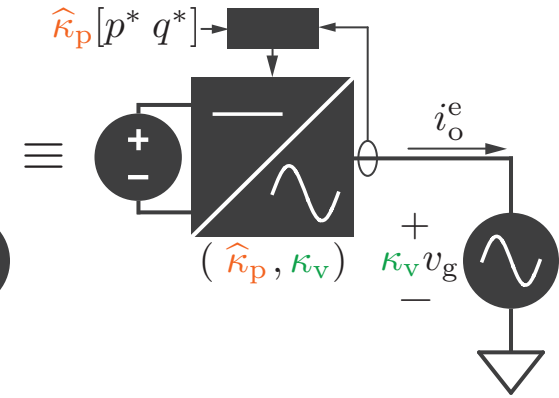
# Scaling Laws and Aggregation



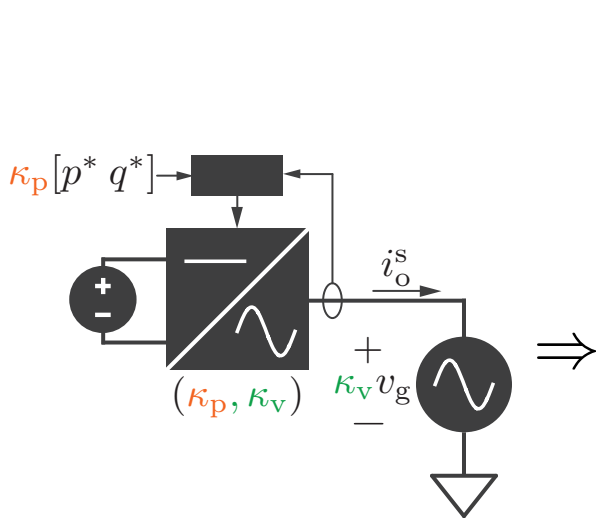
(a) Single **grid following** or **grid forming** inverter



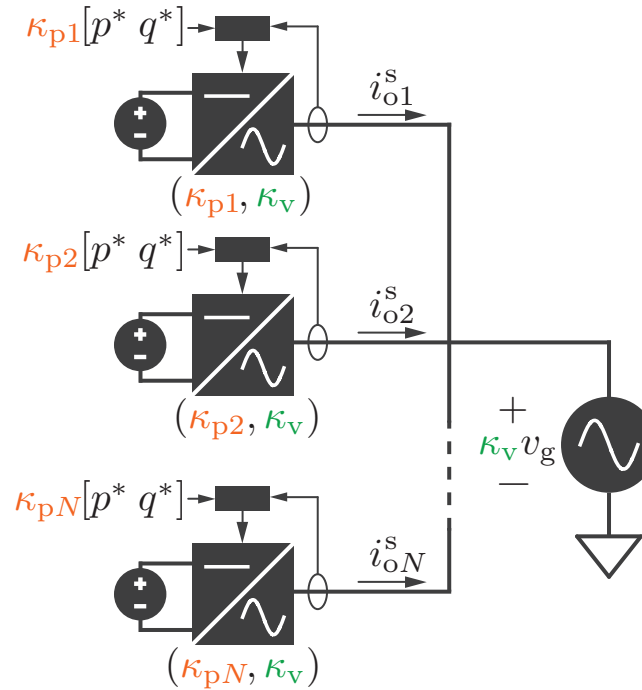
(b) System of  $N$  such parallel inverters



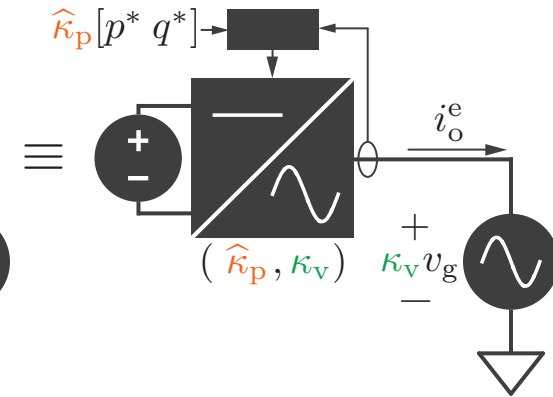
# Scaling Laws and Aggregation



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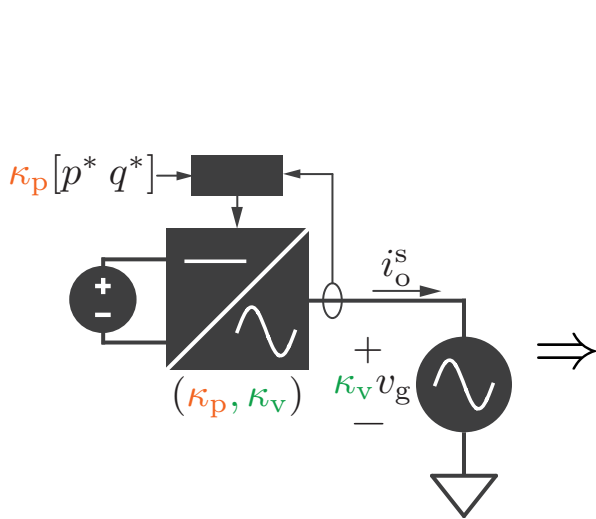
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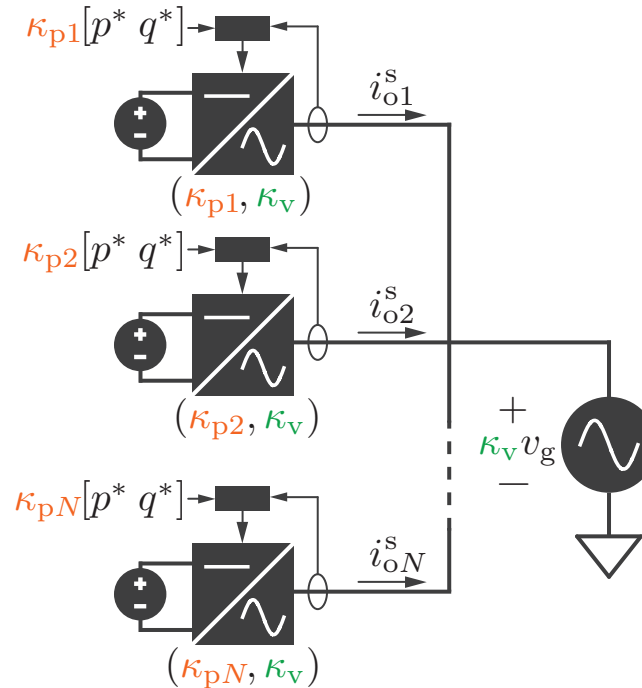
(c) Aggregated equivalent



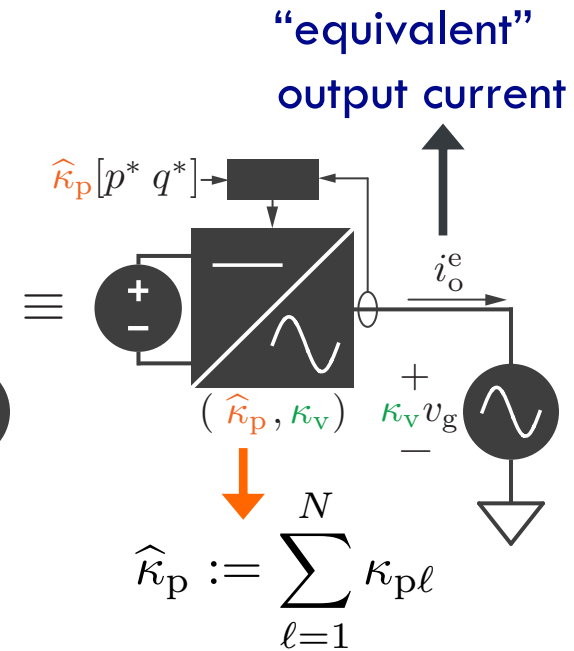
# Scaling Laws and Aggregation



(a) Single **grid following** or **grid forming** inverter

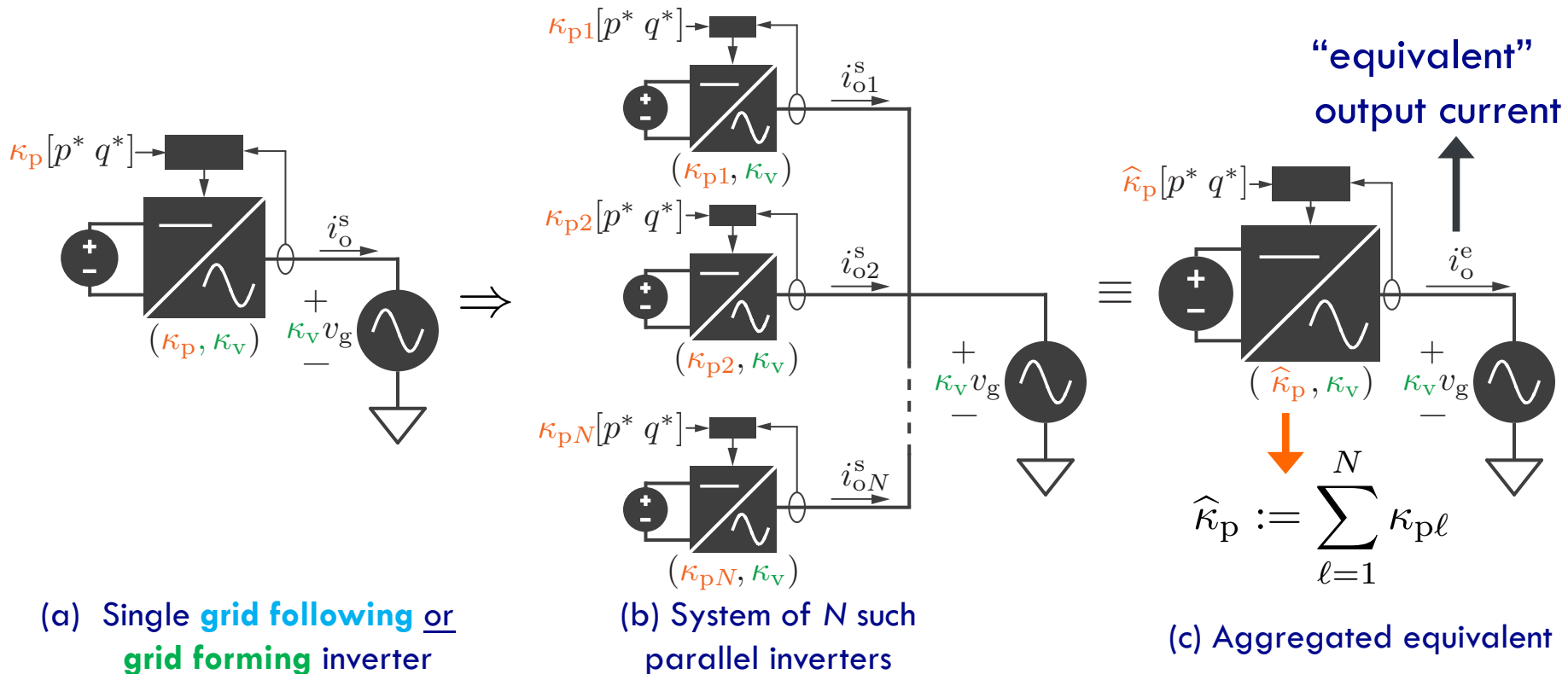


(b) System of  $N$  such parallel inverters



(c) Aggregated equivalent

# Scaling Laws and Aggregation



- If each inverter conforms to scaling laws in [1]-[2], then

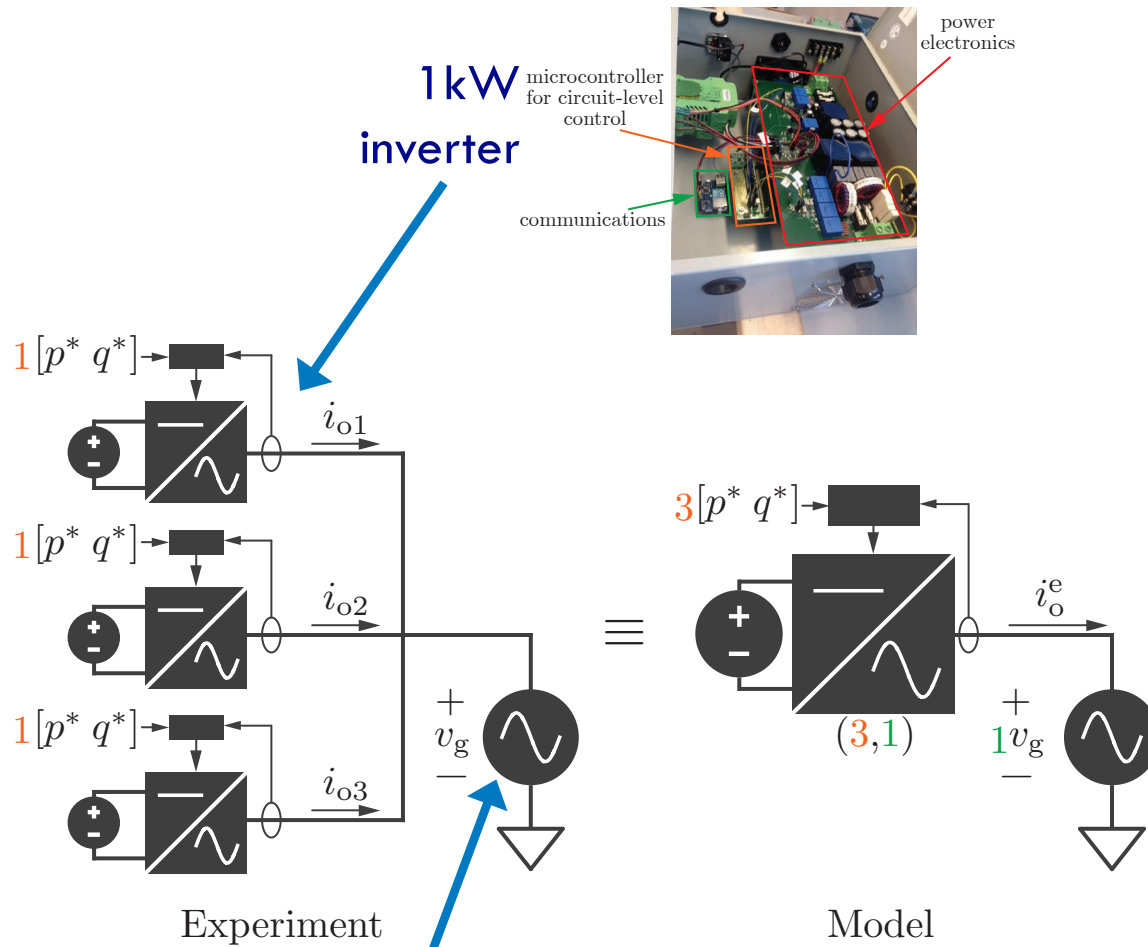
$$i_o^e = \sum_{l=1}^N i_{ol}^s$$

for  $t \geq t_o$ .

[1] Scaling laws for **grid following**: V. Purba, B. Johnson, S. Jafarpour, F. Bullo, and S. Dhople, “Reduced-order Structure-preserving Model for Paralleled Three-phase Grid-tied Inverters,” *Workshop on Control and Modeling for Power Electronics*, 2017.

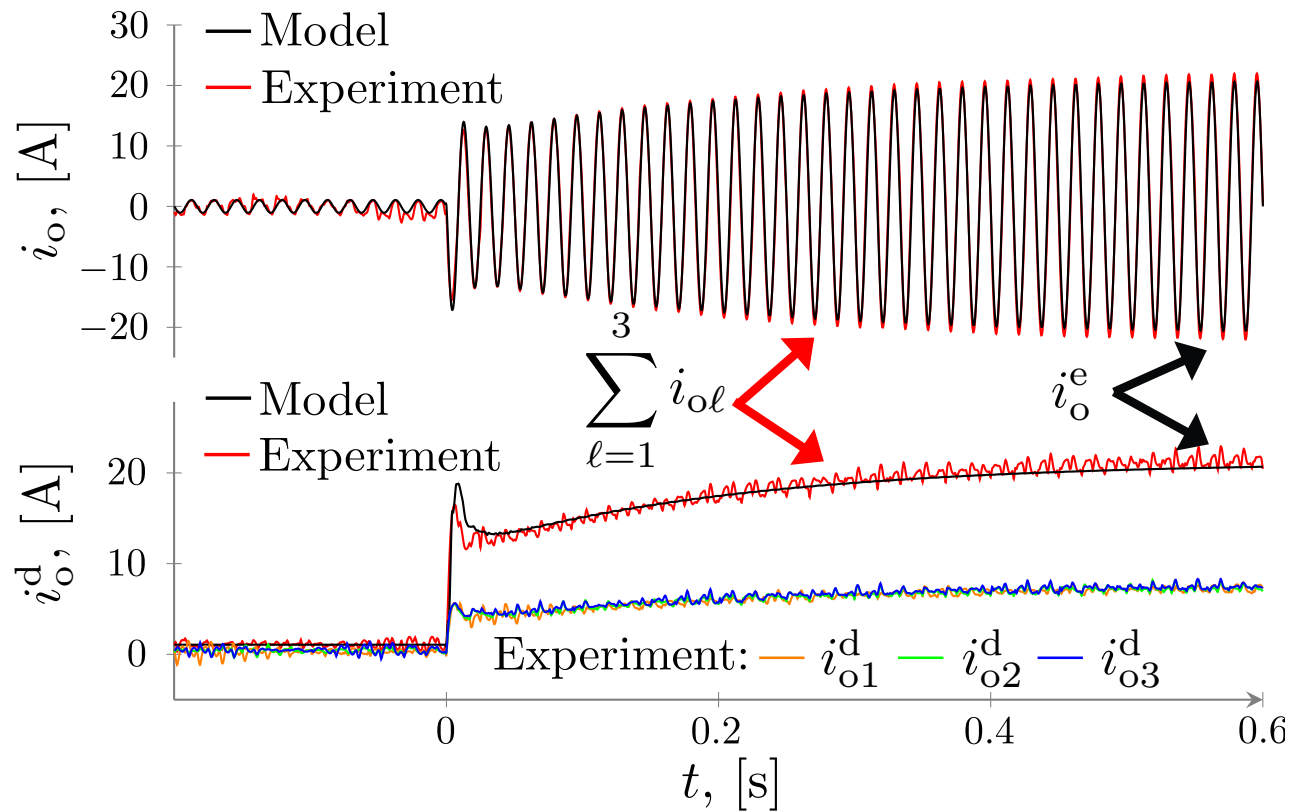
[2] Scaling laws for **grid forming**: M. Khan, B. Johnson, V. Purba, and S. Dhople, “A Reduced-order Aggregated Model for Parallel Inverter Systems Controlled with Virtual Oscillator Control,” *Workshop on Control and Modeling for Power Electronics*, 2018.

# Experimental Validation of Aggregation



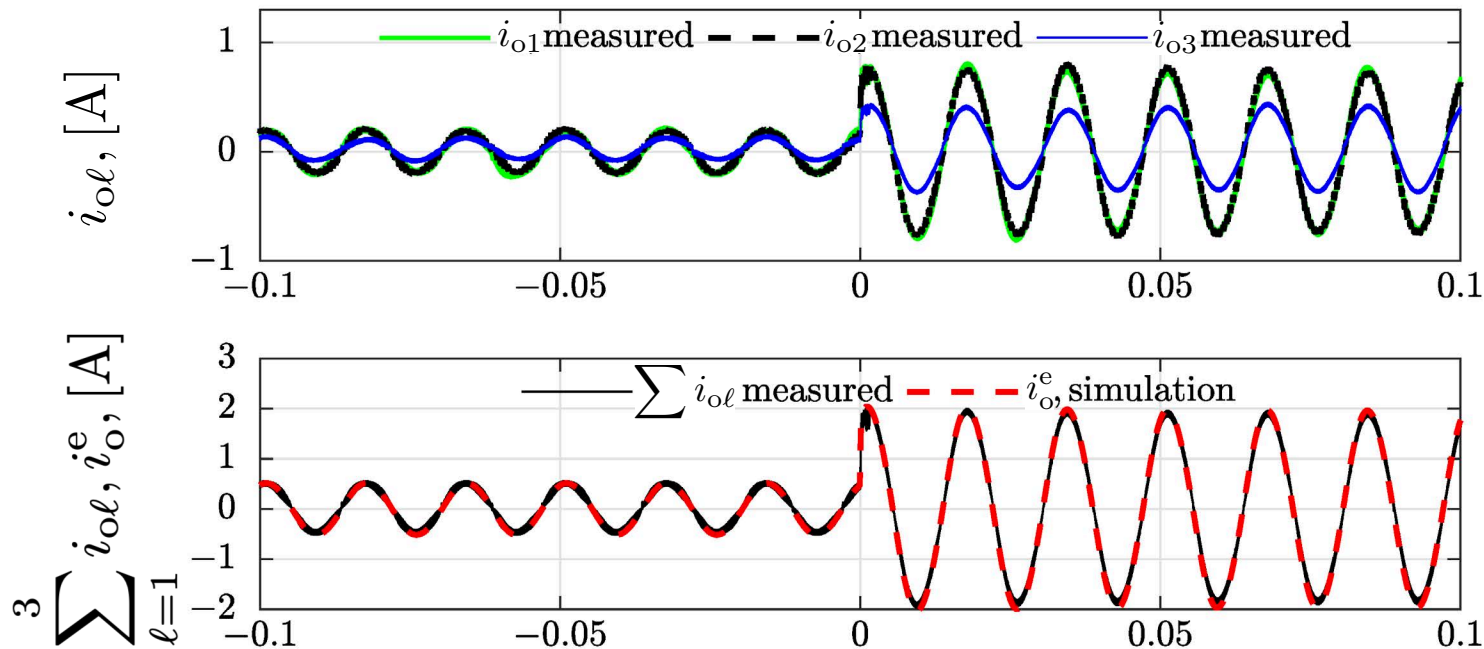
# Experimental Validation: Grid-Following Controls

- System of 3 grid-following inverters during power command step change.



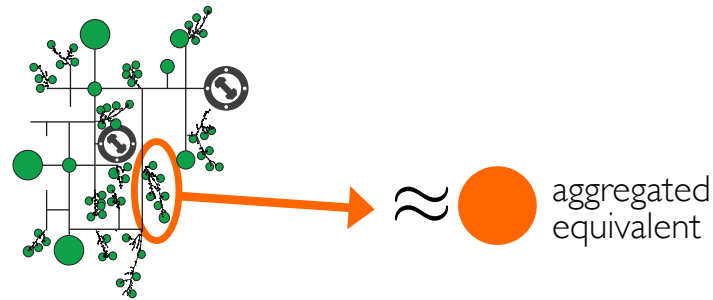
# Experimental Validation: Grid-Forming Oscillator Controls

- System of 3 inverters with Virtual Oscillator Control during load steps.

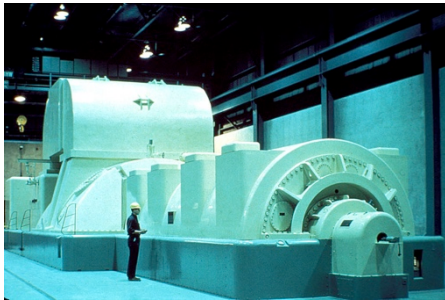


# Outline

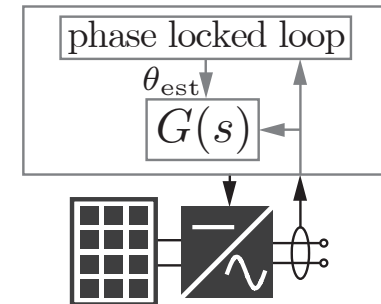
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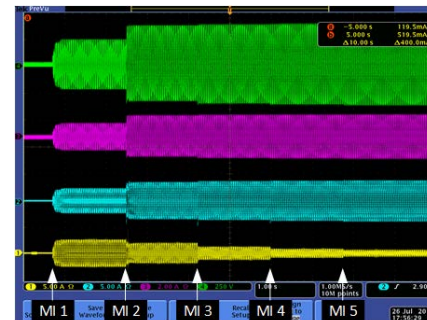
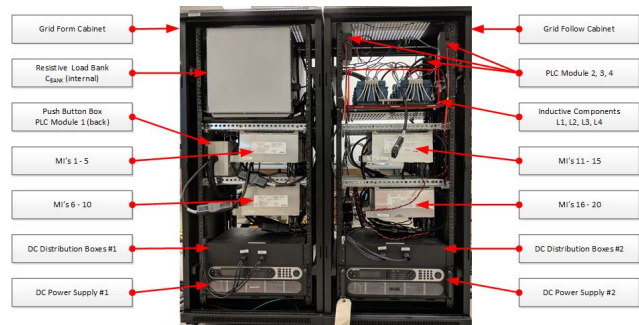
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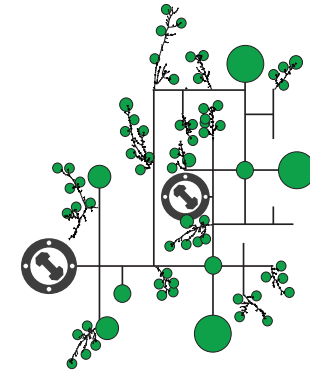
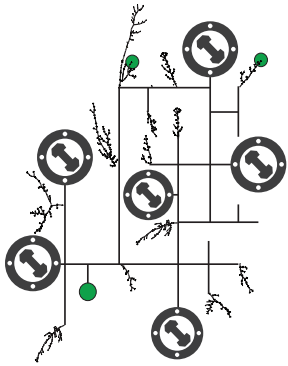
How many machines can we replace with electronics?



3. A **hardware** demo with 20 commercial inverters.



# The Key Question



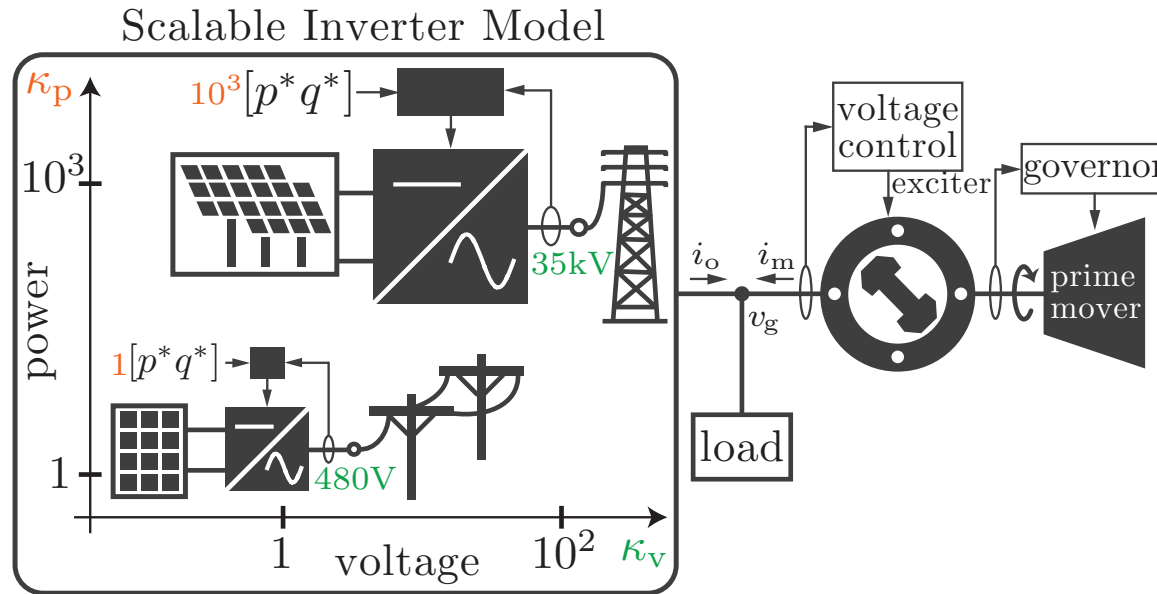
Can we get from here

to here?

- Look at this question with both **grid-following** and **grid-forming** inverters.

# An Elementary Model

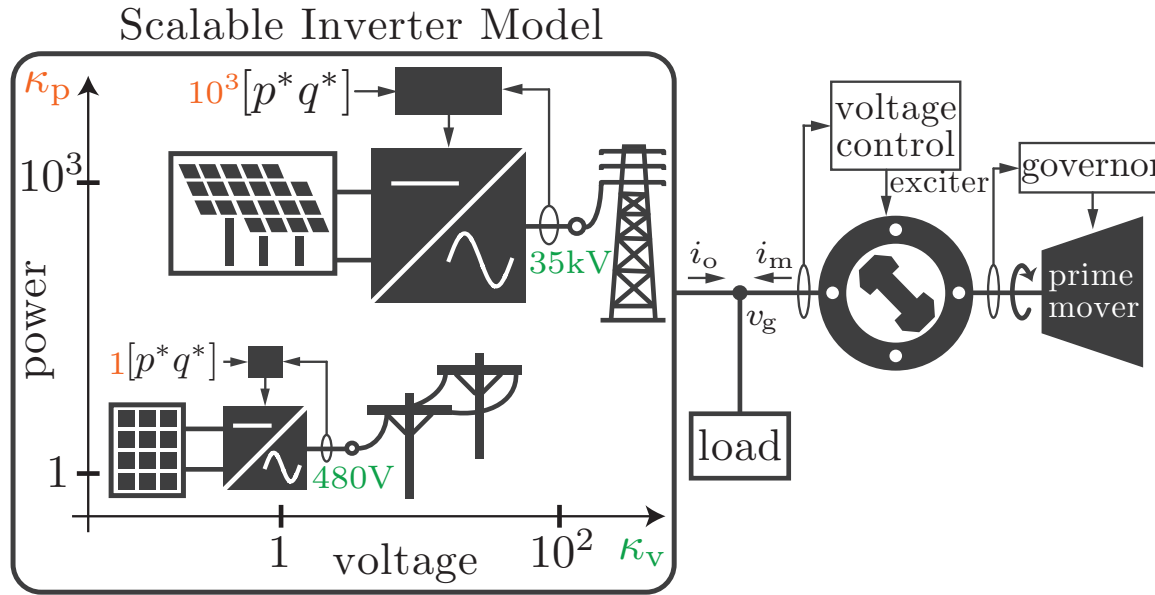
A good starting point:





# An Elementary Model

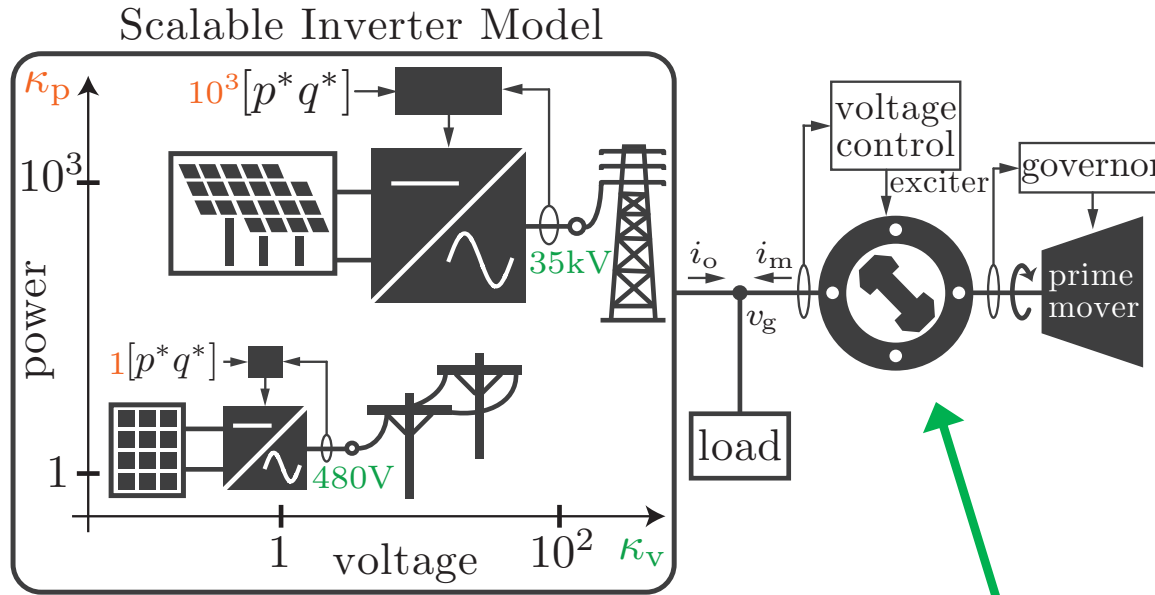
A good starting point:



Represents an aggregated  
collection of inverters

# An Elementary Model

A good starting point:

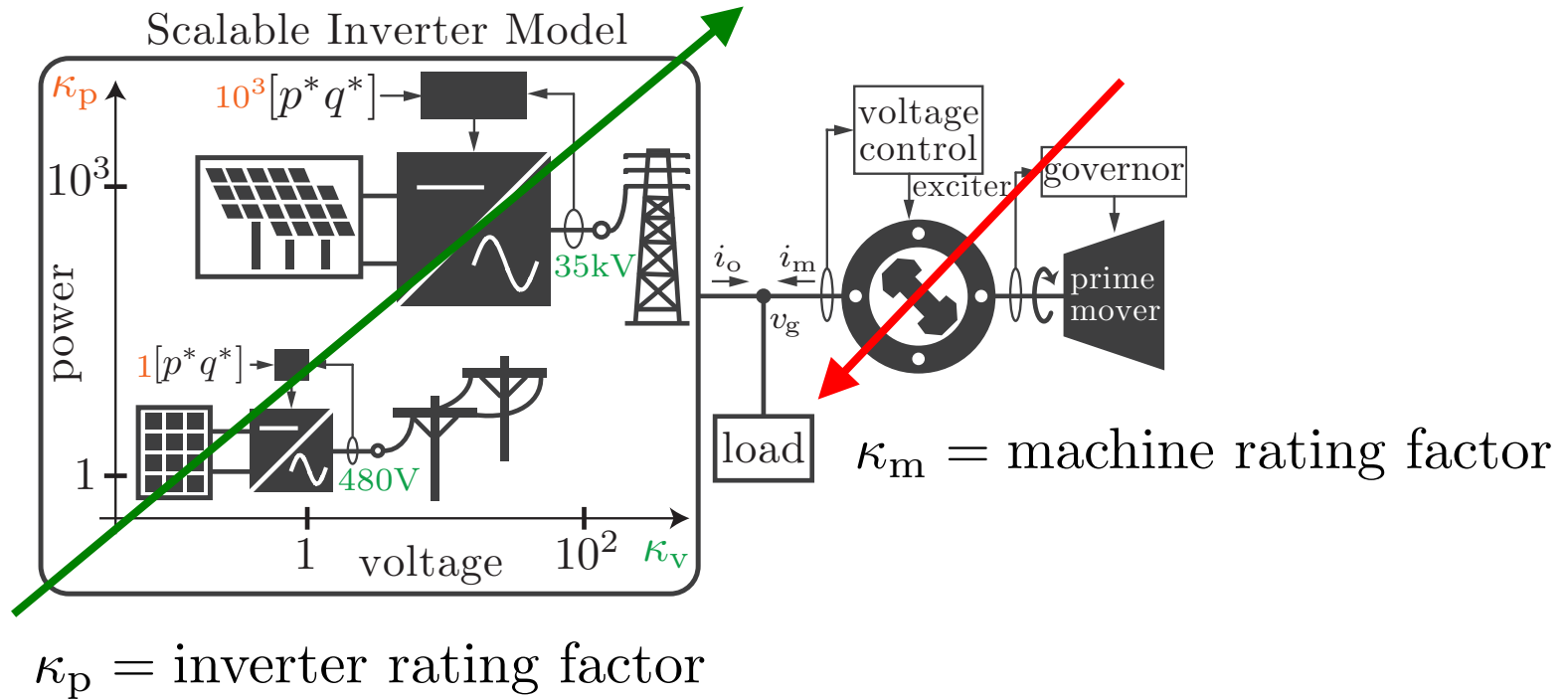


Represents an aggregated collection of inverters

Prototypical steam-driven generator at fossil-fuel plant

# A Fundamental Question

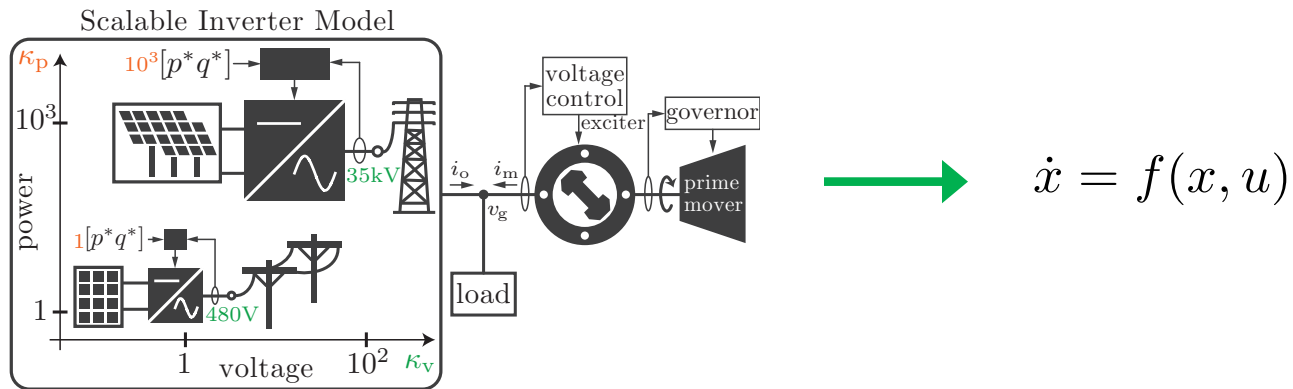
**Q:** What happens as the ratio of inverter/machine ratings increases?



Approach: Adjust scaling concurrently such that  $\kappa_p + \kappa_m = \text{constant}$

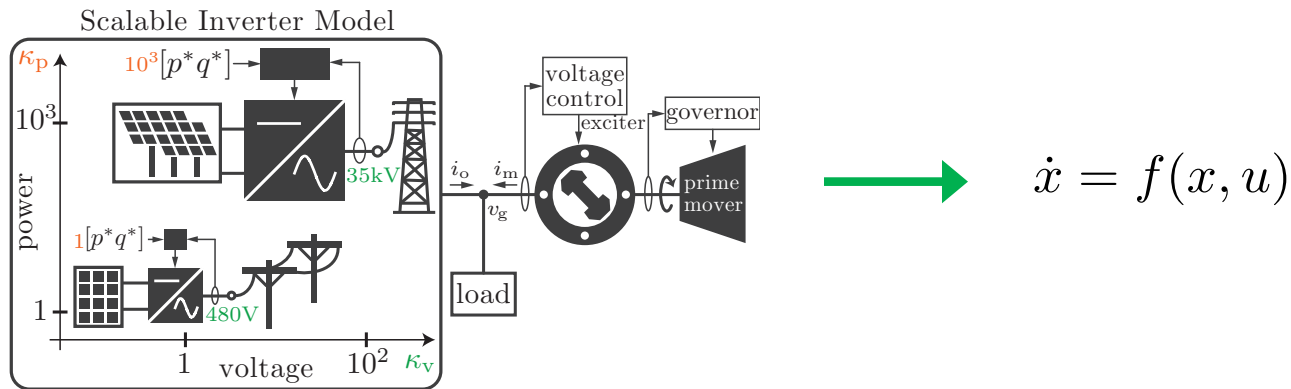
# Model Framework

- Start with zero inverter penetration:  $\kappa_m = \text{nominal}, \kappa_p = 0$



# Model Framework

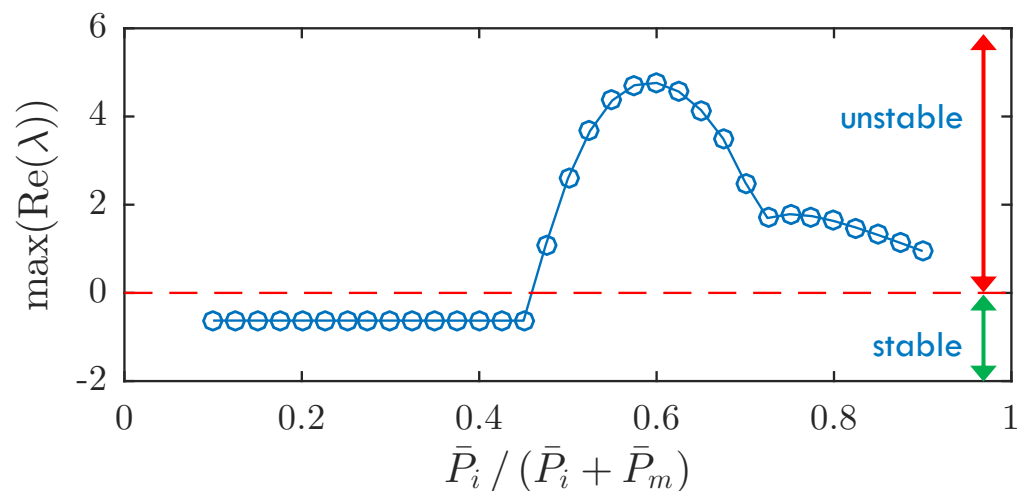
- Start with zero inverter penetration:  $\kappa_m = \text{nominal}, \kappa_p = 0$



- Find equilibrium  $x^*$
- Linearize to get  $\Delta \dot{x} = A \Delta x + B \Delta u$
- Compute eigenvalues  $\lambda \in \mathbb{C}^{|x|}$
- Increase  $\kappa_p$  and decrease  $\kappa_m$

# Results: Small-signal Stability with **Grid-Following** Inverter

- Fixed machine rating  $\bar{P}_m = 555\text{MVA}$ , parameters from [1]
- Unscaled inverter rating  $P_i = 1\text{kVA}$ , parameters for NREL hardware

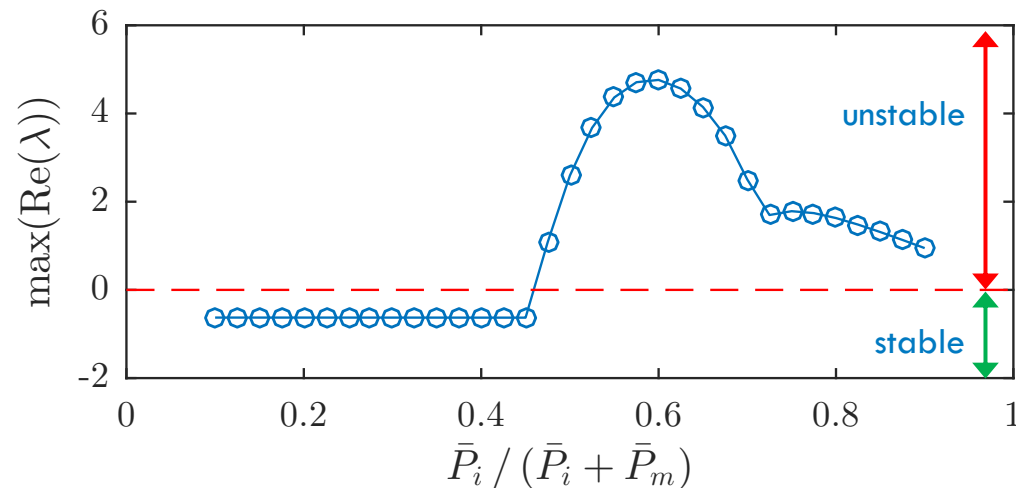


[1] P. Kundur, N. J. Balu, and M. G. Lauby, Power system stability and control. McGraw-hill New York, 1994.

[2] Y. Lin, B. Johnson, V. Purba, S. Dhople, V. Gevorgian, "Stability Assessment of a System Comprising a Single Machine and Inverter with Scalable Ratings," *North American Power Symposium*, 2017.

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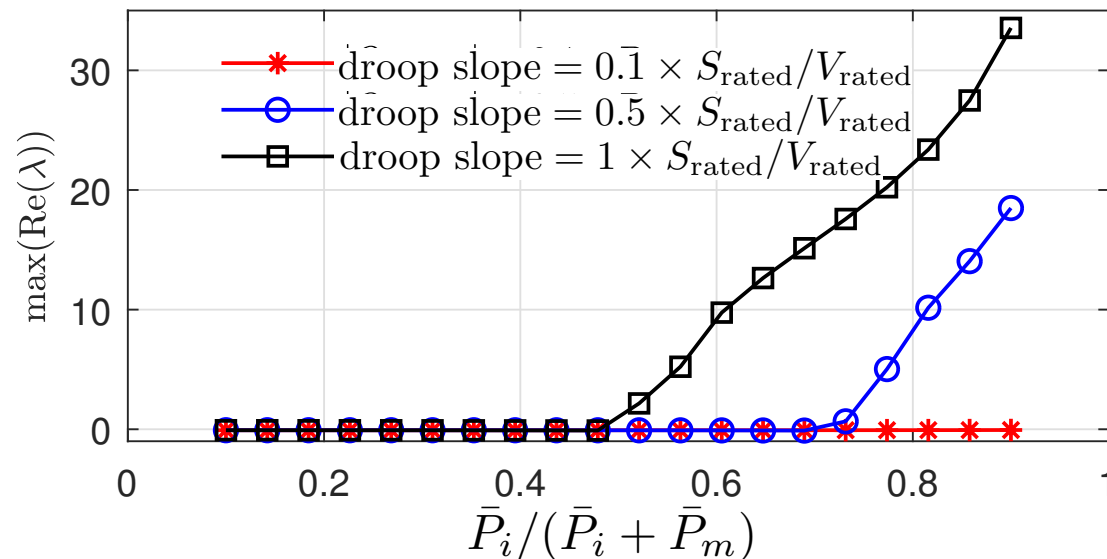
- Instability in this example at approximately 50% [2]
- Result varies between 40%-90%, depends on parameters

[1] P. Kundur, N. J. Balu, and M. G. Lauby, Power system stability and control. McGraw-hill New York, 1994.

[2] Y. Lin, B. Johnson, V. Purba, S. Dhople, V. Gevorgian, "Stability Assessment of a System Comprising a Single Machine and Inverter with Scalable Ratings," *North American Power Symposium*, 2017.

# Results: Small-signal Stability with **Grid-Forming** Inverter

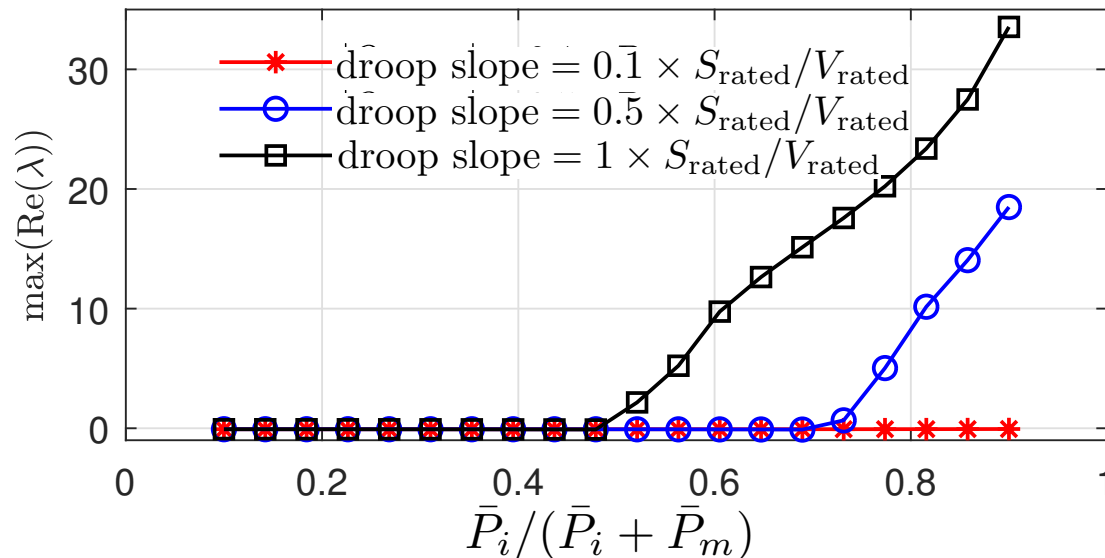
- Now look at inverter with Virtual Oscillator Control
- Machine same as before





# Results: Small-signal Stability with **Grid-Forming** Inverter

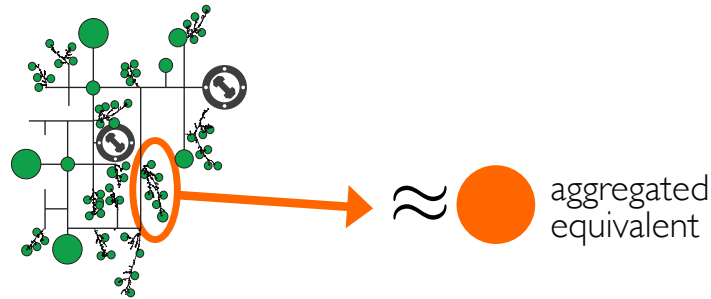
- Now look at inverter with Virtual Oscillator Control
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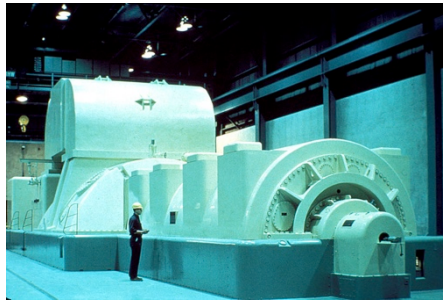
- Key finding: Instability can be eliminated with flatter Volt/VAR droop slope [1]

# Outline

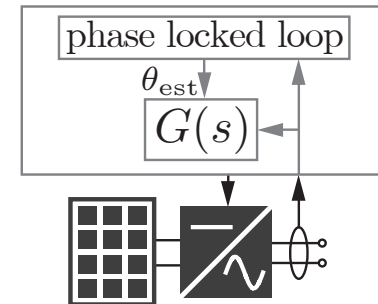
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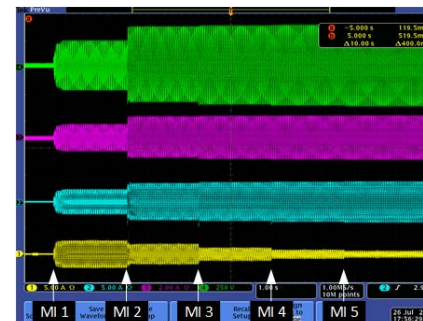
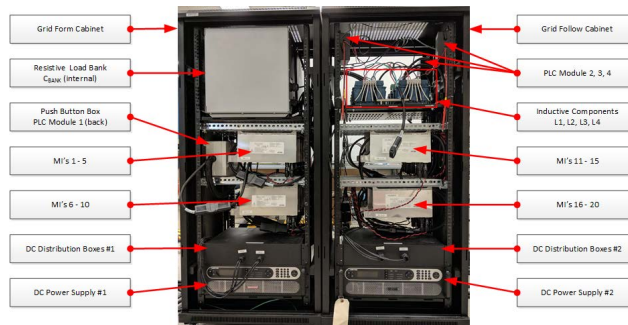
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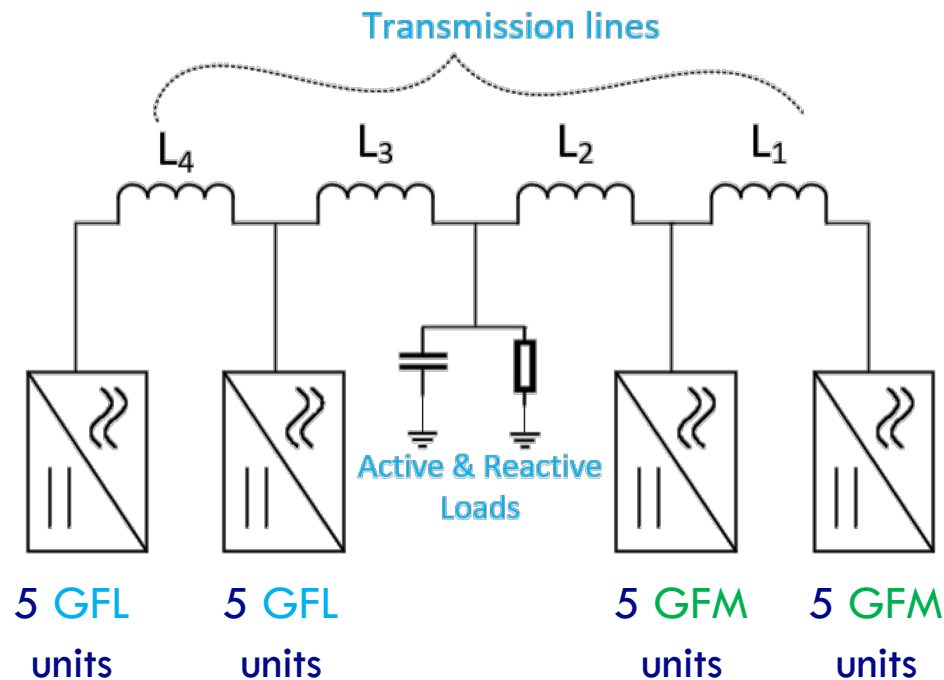
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# A Demo of a Complex Network

## Characteristics:

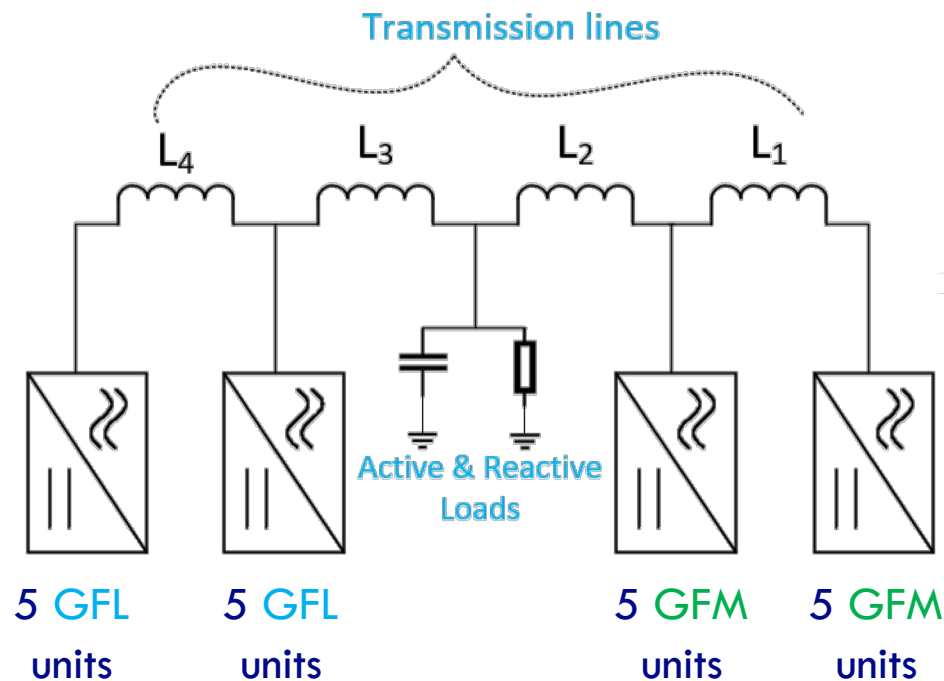
- Heterogenous **grid-forming (GFM)** + **grid following (GFL)**
- Relatively complex: 20 units total = 10 **GFM** + 10 **(GFL)**
- Radial distribution network with **line impedances + cap bank**
- Operation on **commercial hardware**



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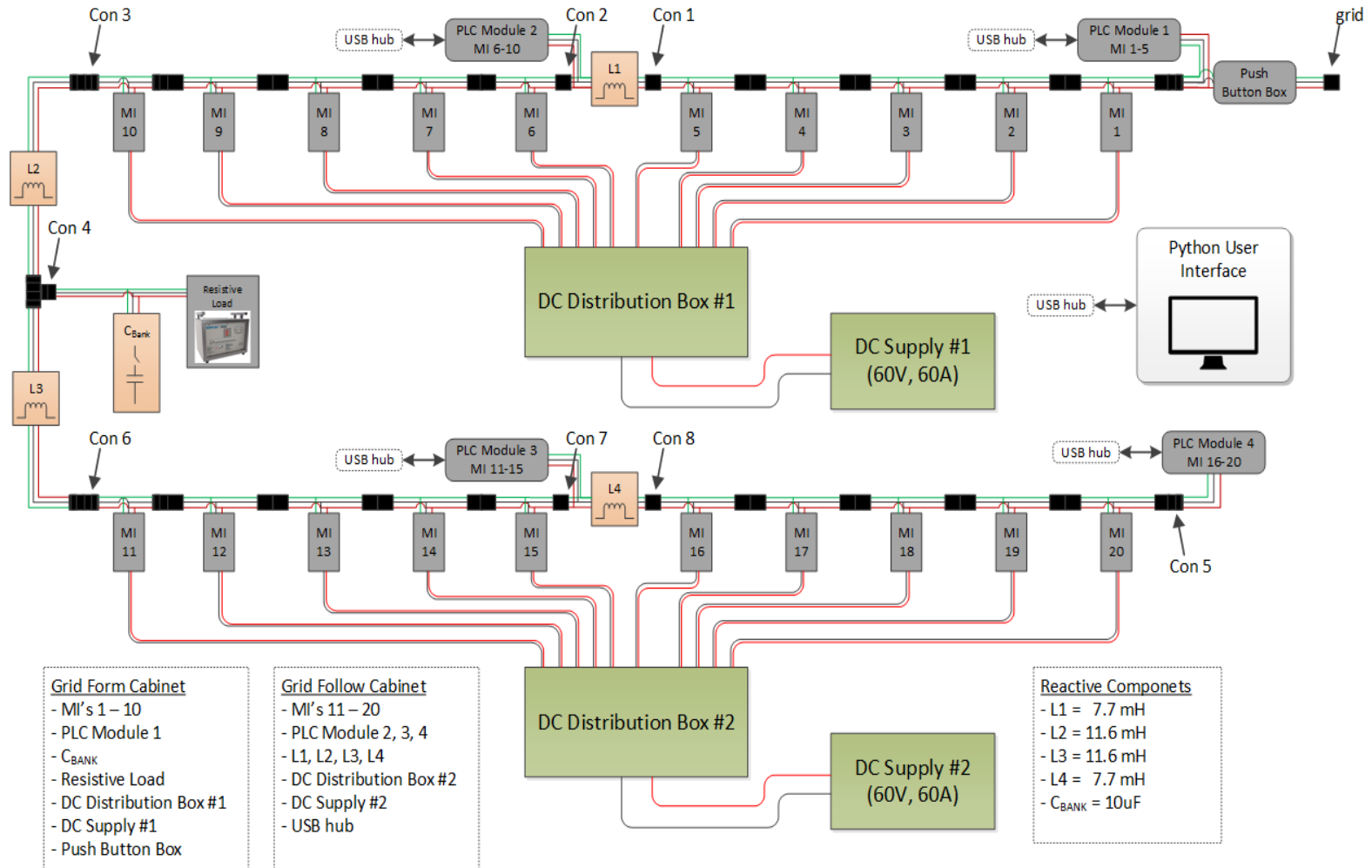
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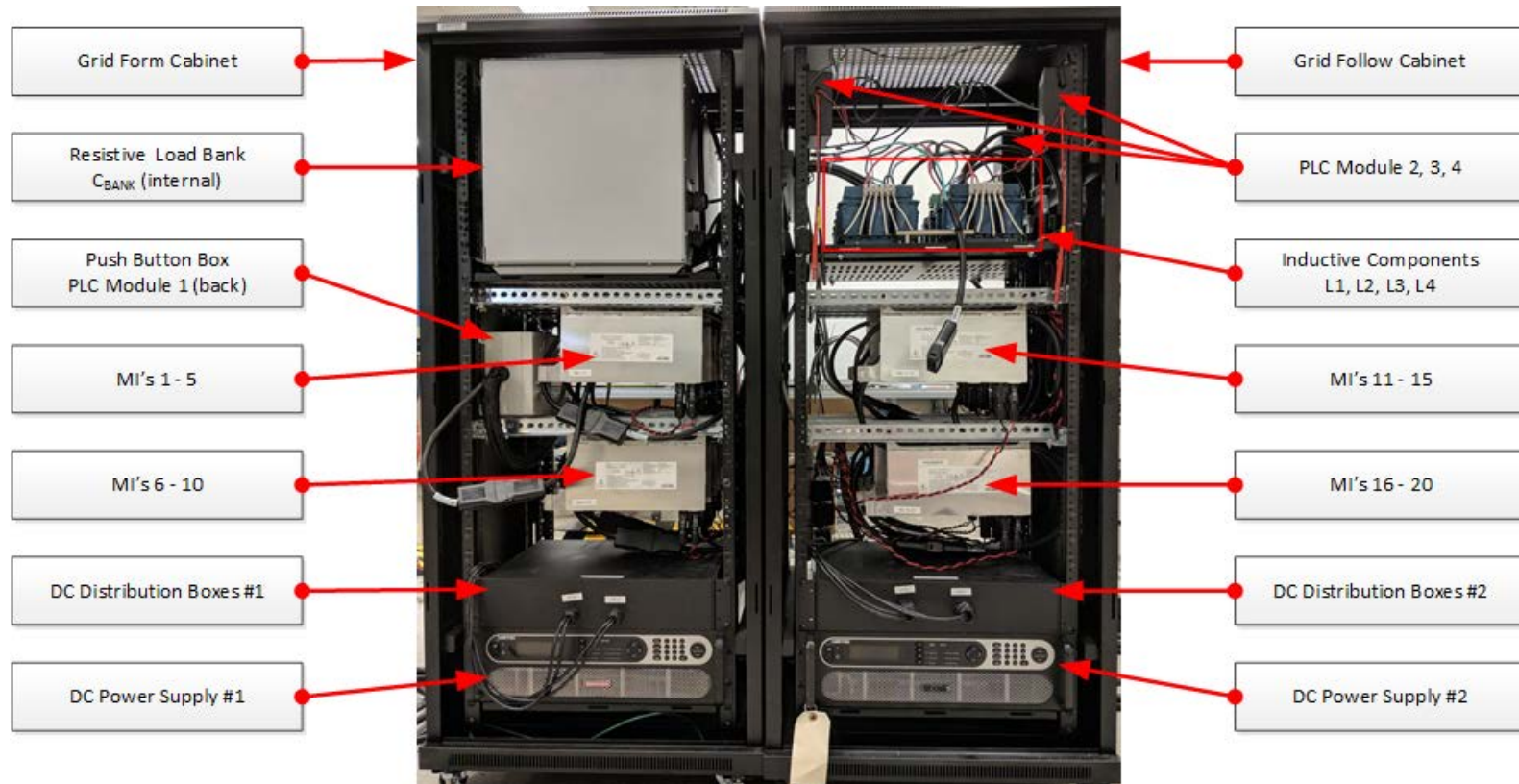


A closer look

# Network Details



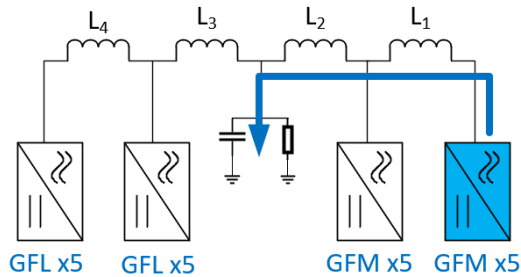
# Realization



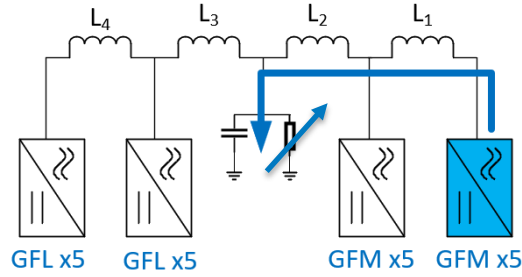
SunPower inverters with modified controls

# A Black-start to Full-system Sequence

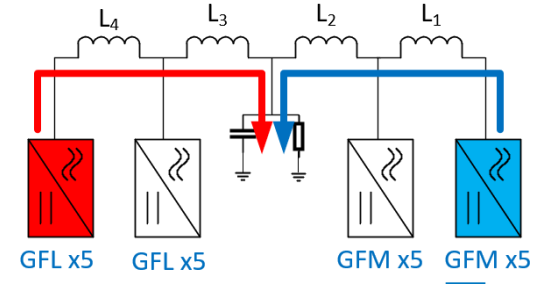
## Black start



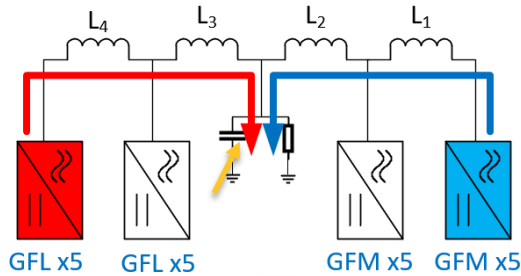
## Load step



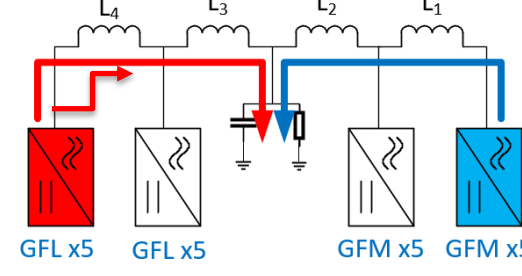
## Add GFL



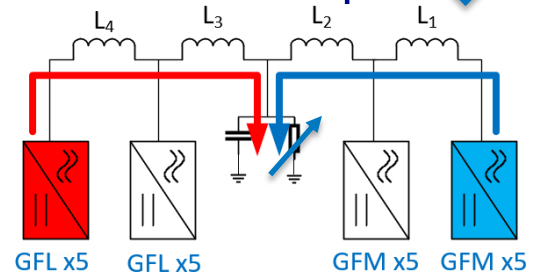
## Cap step



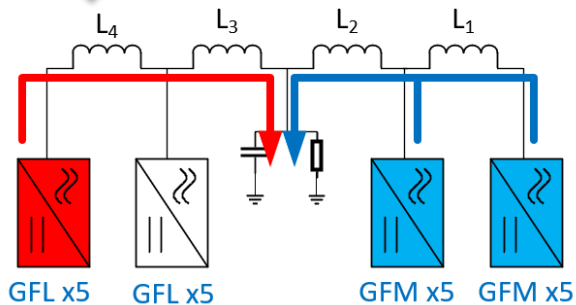
## Generation step



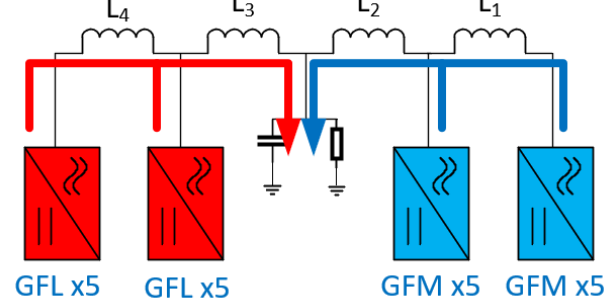
## Load step



## Add GFL

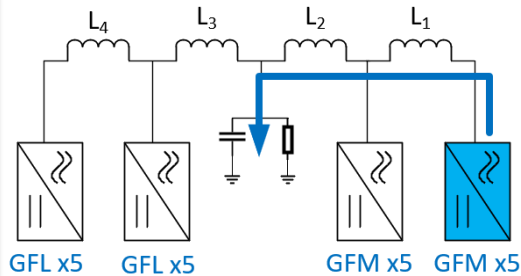


## Full System

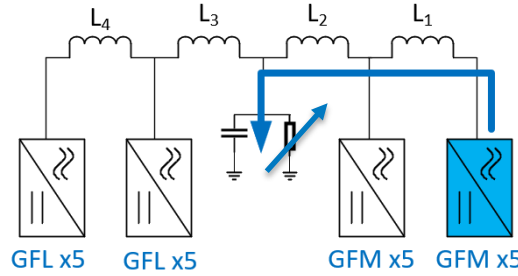


# A Black-start to Full-system Sequence

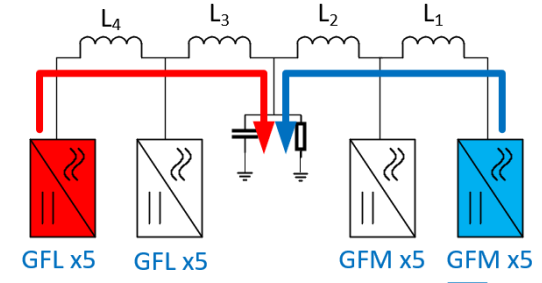
## Black start



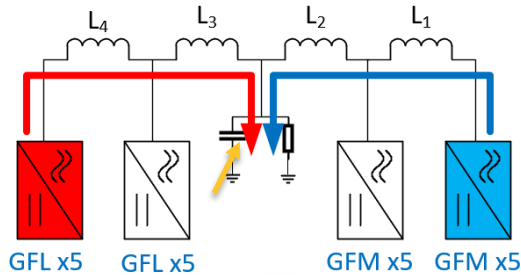
## Load step



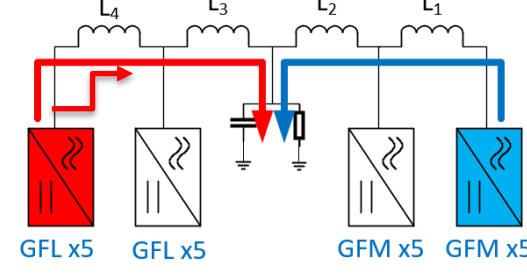
## Add GFL



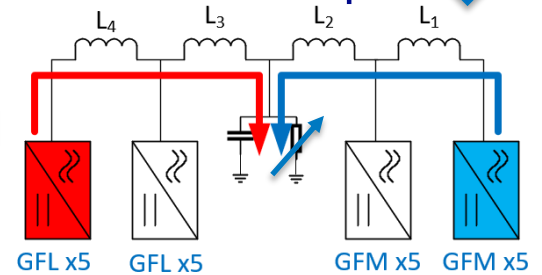
## Cap step



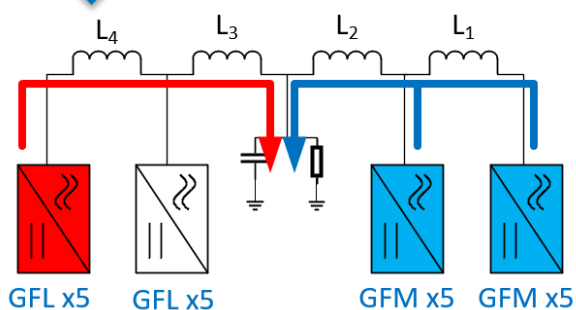
## Generation step



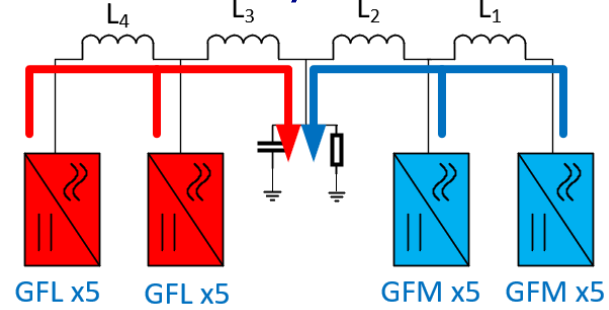
## Load step



## Add GFL

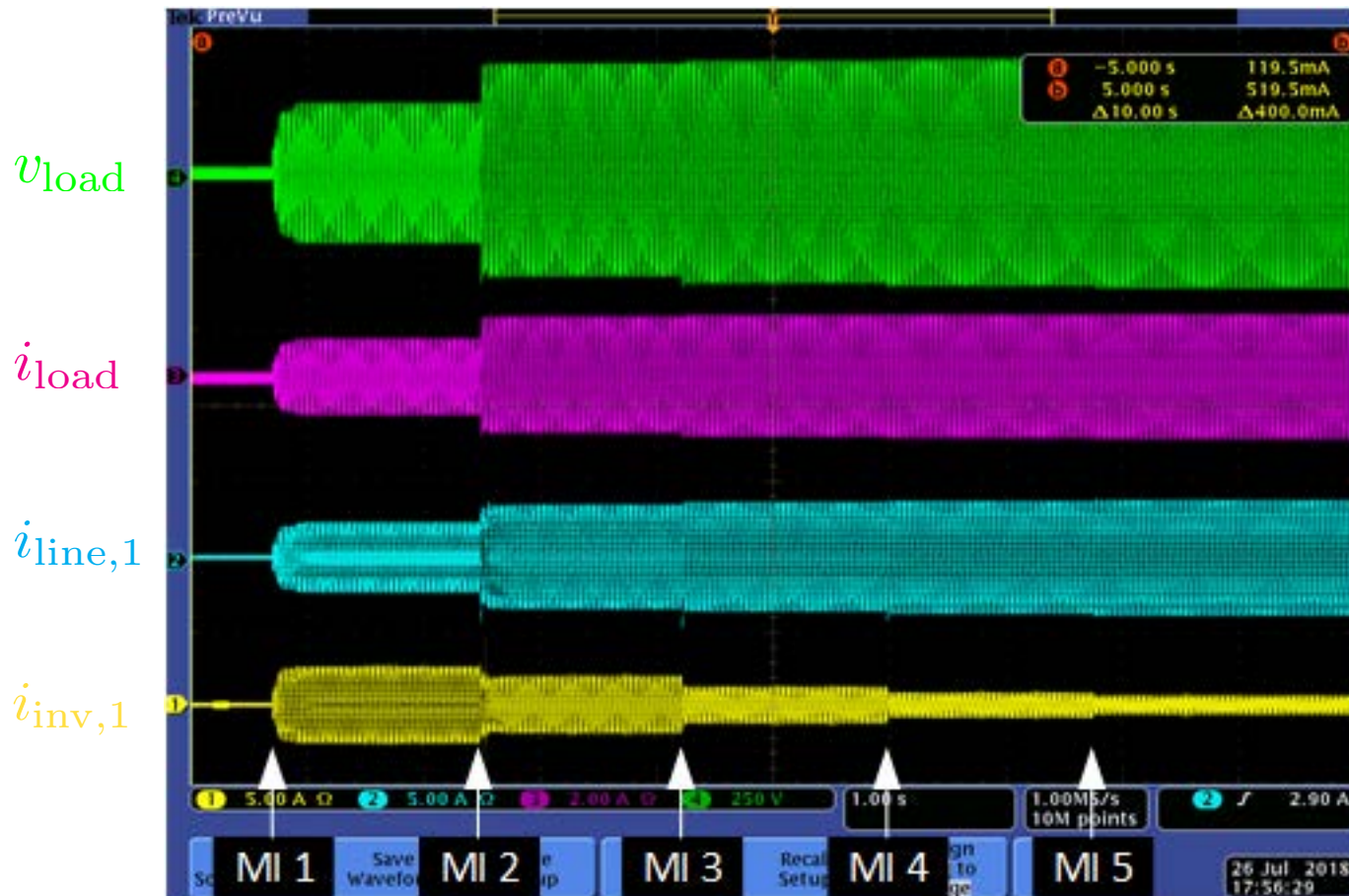


## Full System

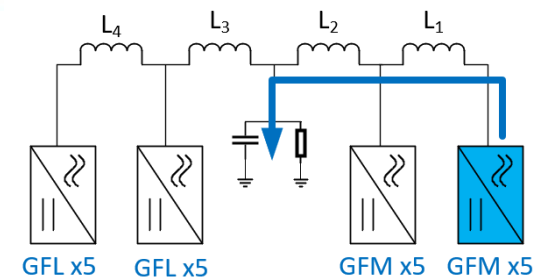




# Step 1: Black-start

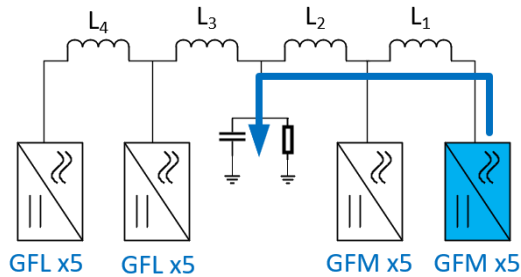


- Start with 250W load
- VOC units power share

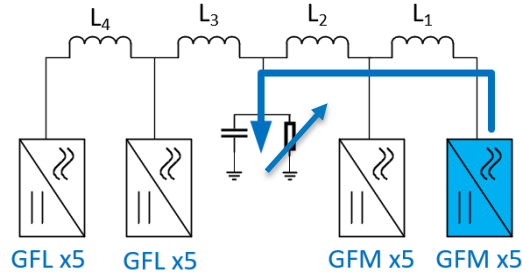


# A Black-start to Full-system Sequence

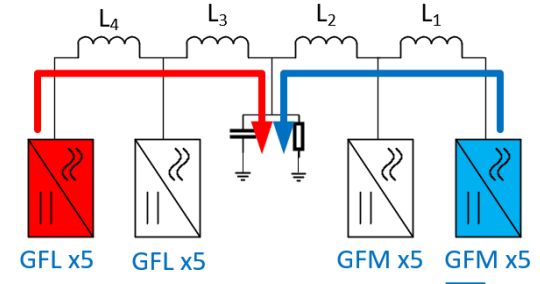
## Black start



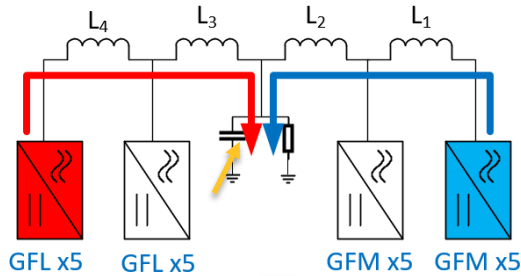
## Load step



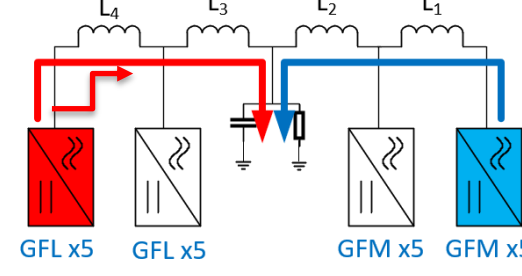
## Add GFL



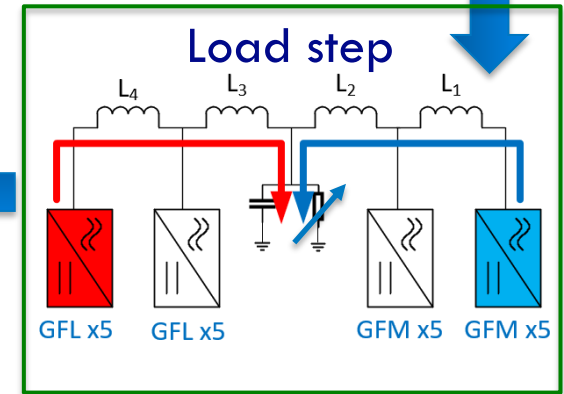
## Cap step



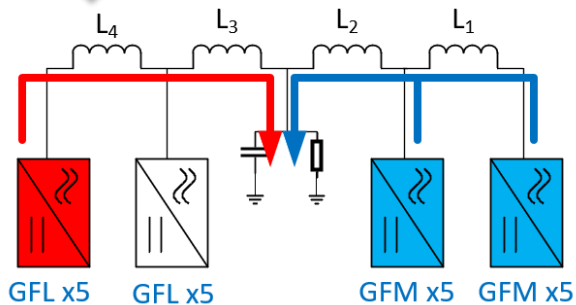
## Generation step



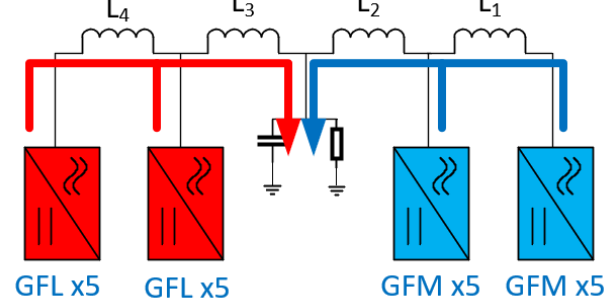
## Load step



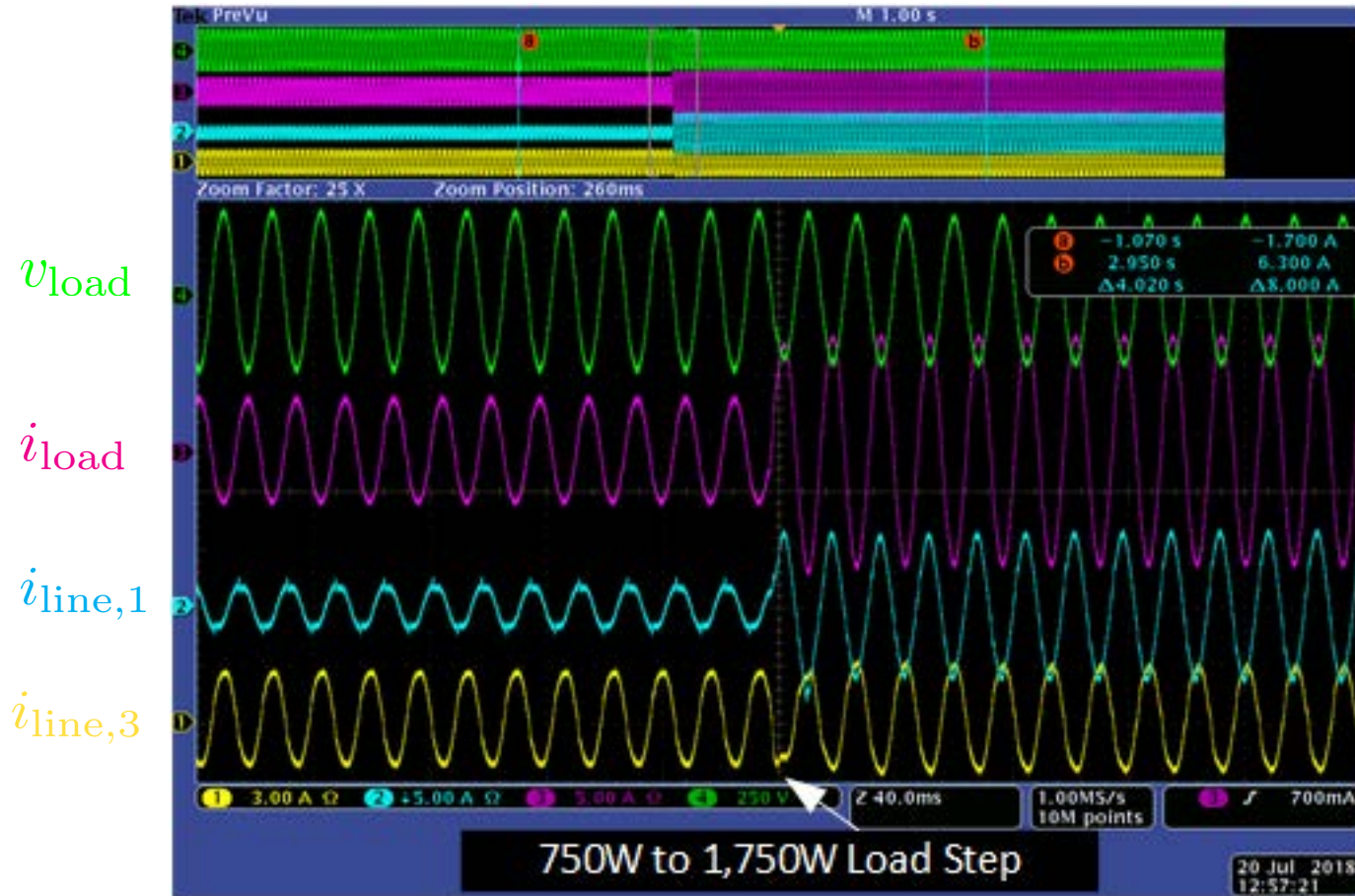
## Add GFL



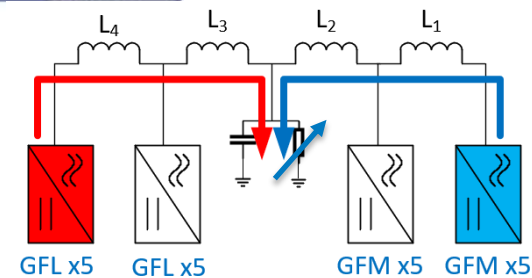
## Full System



# Step 4: Load Step with 10 Units

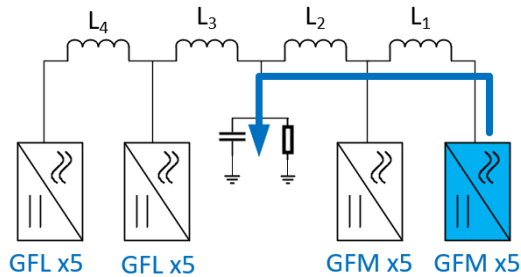


- GFL inverters share load step and regulate voltage
- GFM inverters generate 500 W

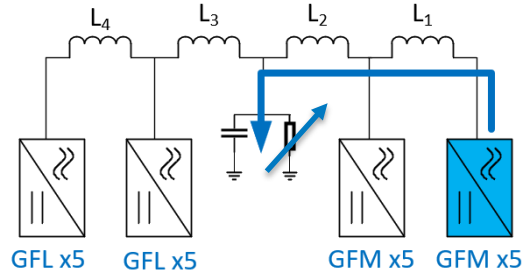


# A Black-start to Full-system Sequence

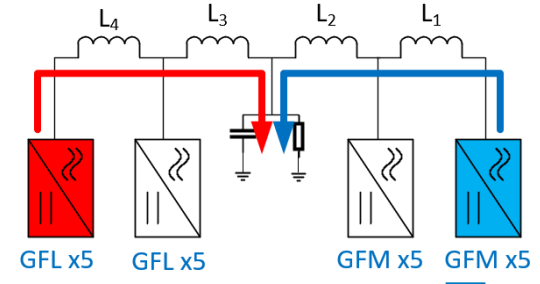
## Black start



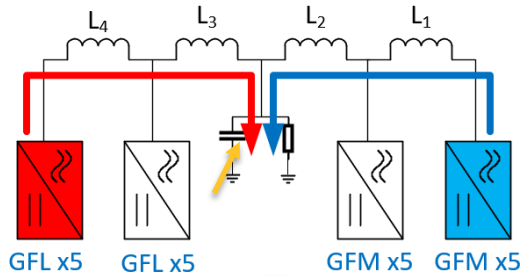
## Load step



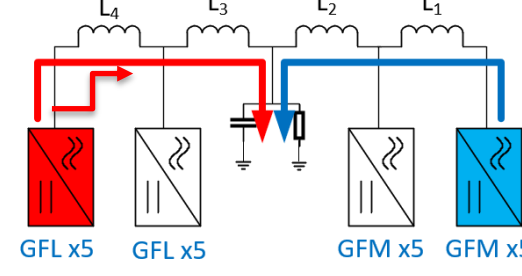
## Add GFL



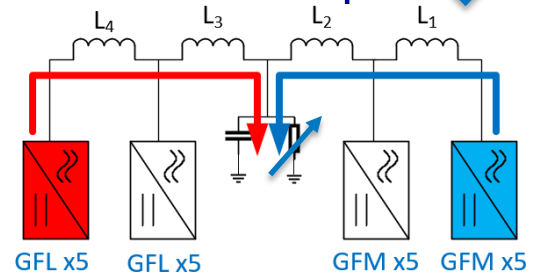
## Cap step



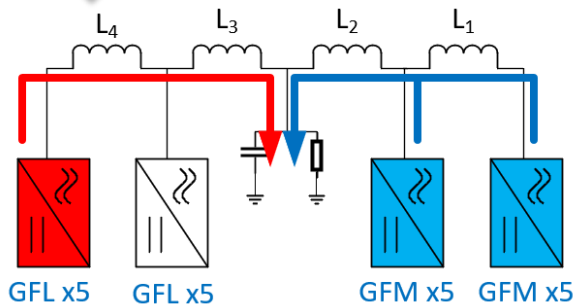
## Generation step



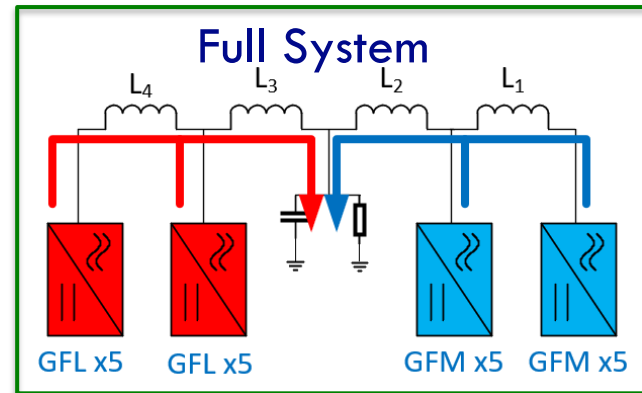
## Load step



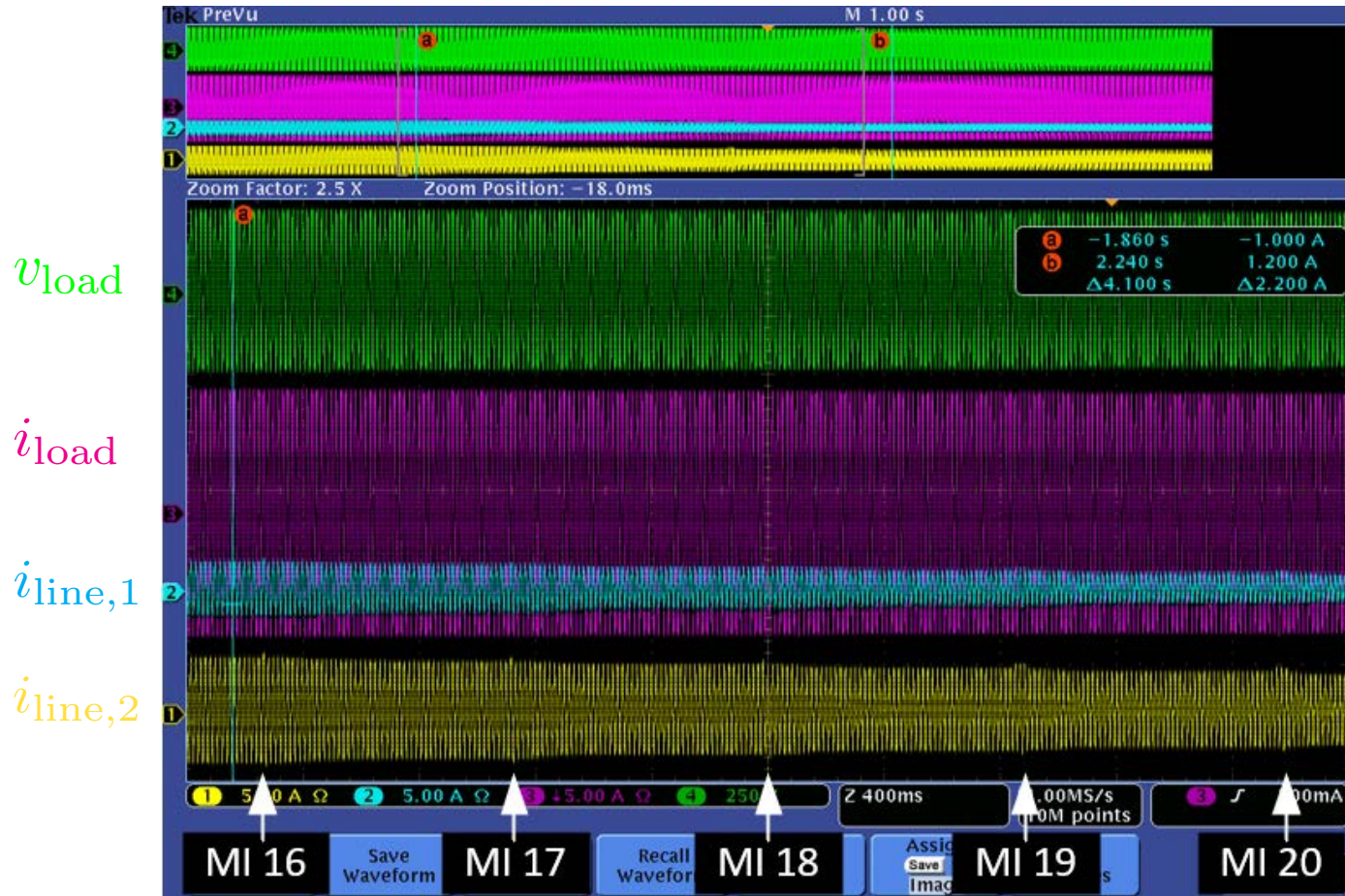
## Add GFL



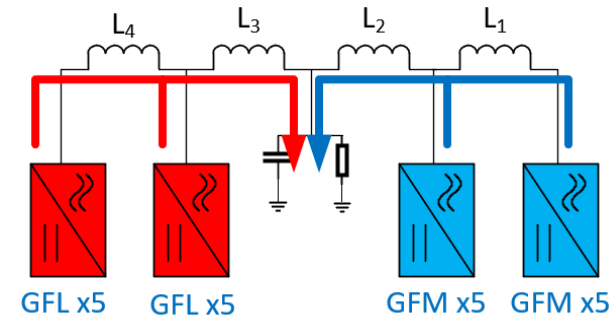
## Full System



# Final Step: Turn on Last 5 GFLs



- Last 5 units turn on sequentially at 250 W output
- System robust to load/generation fluctuations



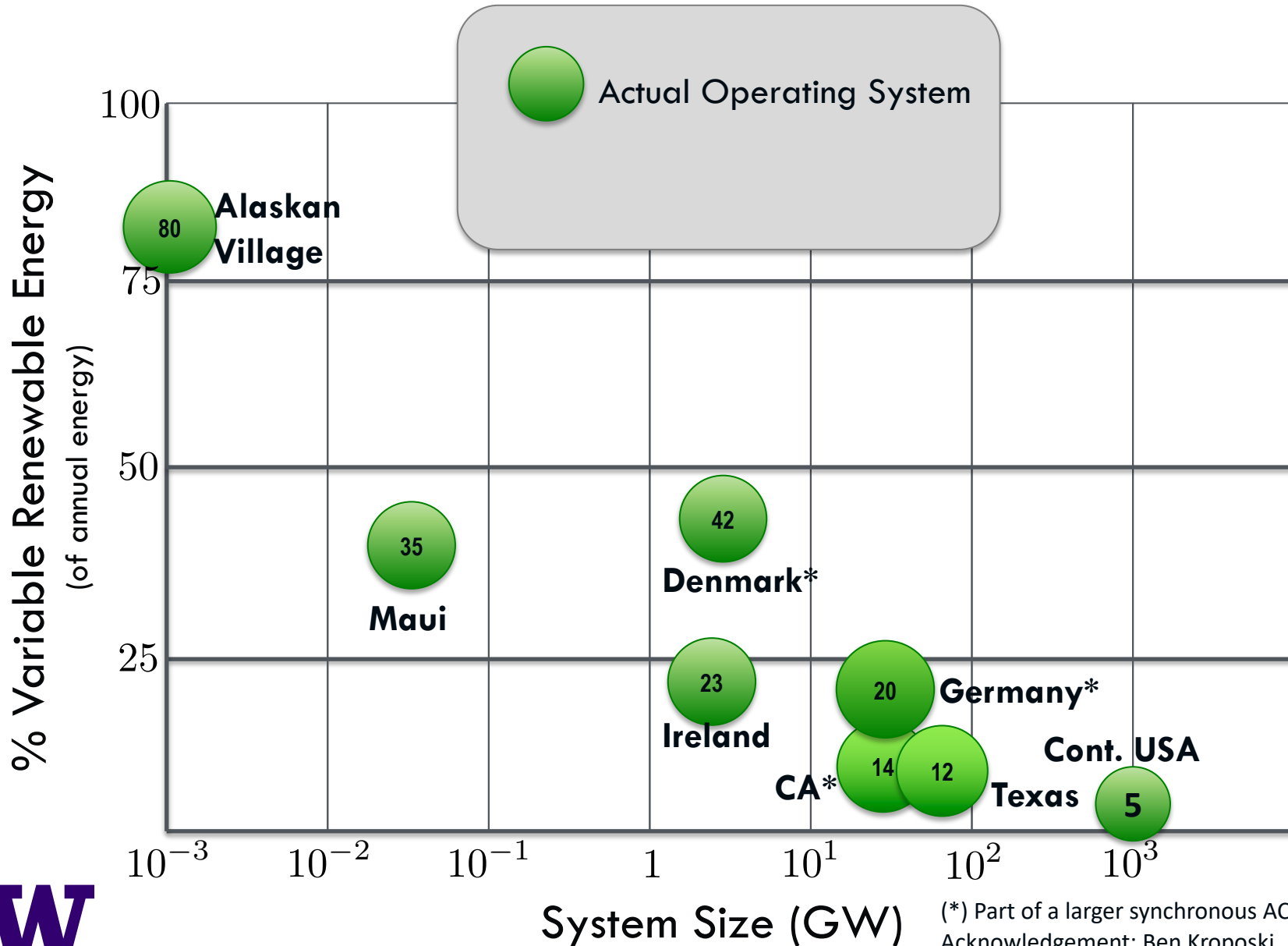
Thanks for your attention!

Brian Johnson

Contact: [brianbj@uw.edu](mailto:brianbj@uw.edu)

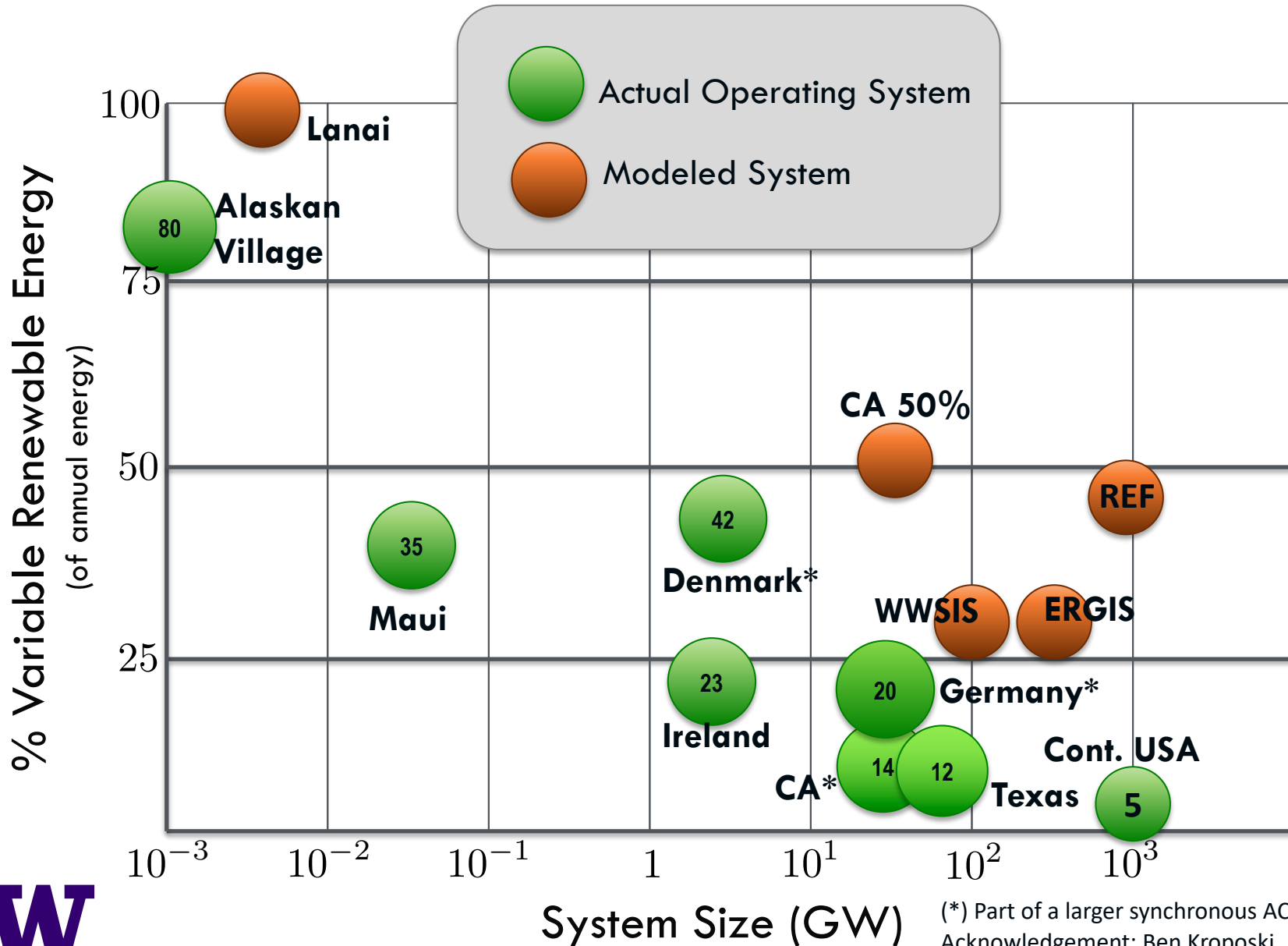


# Transforming the Grid at a Scale That Matters



(\*) Part of a larger synchronous AC power system  
Acknowledgement: Ben Kroposki, NREL

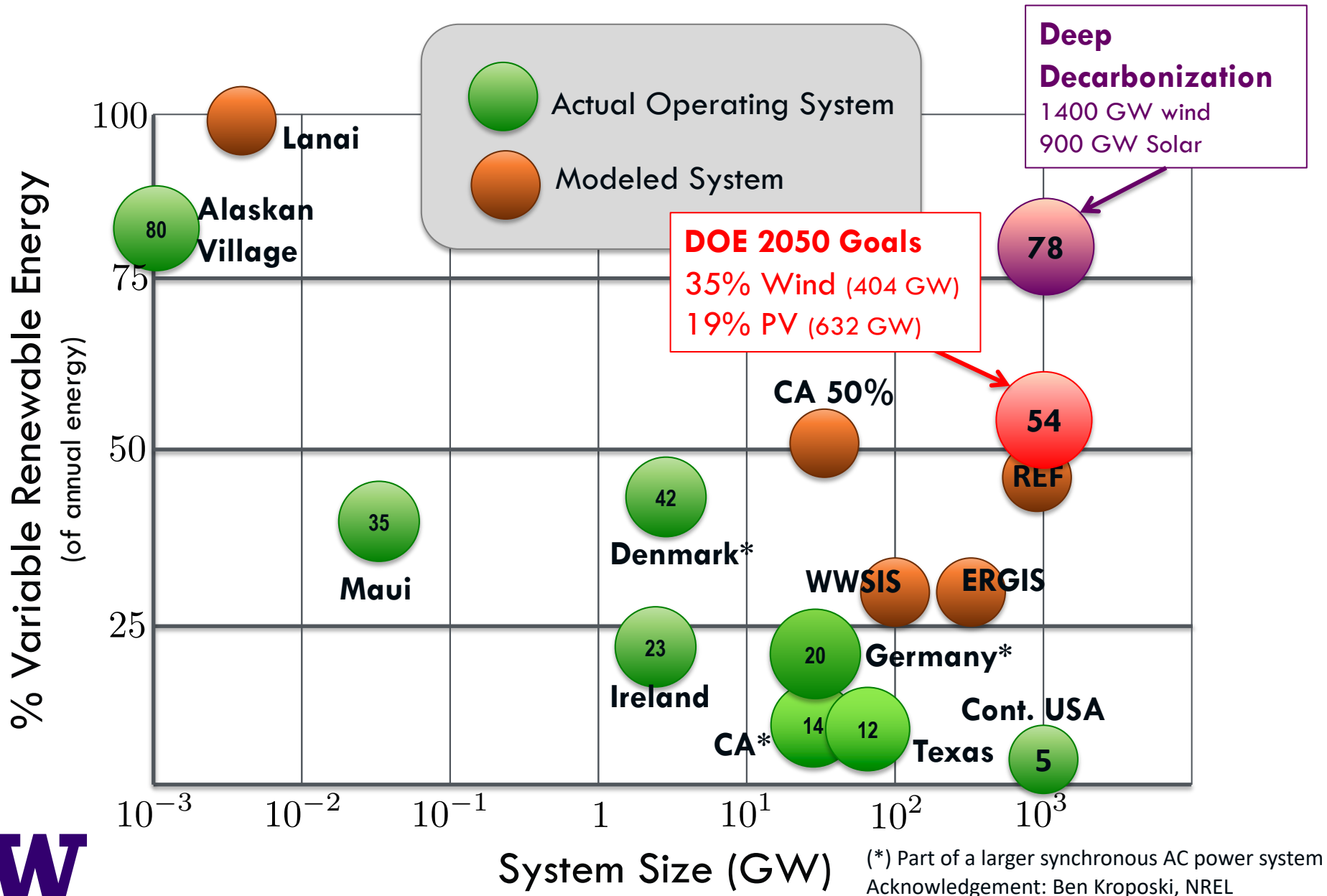
# Transforming the Grid at a Scale That Matters



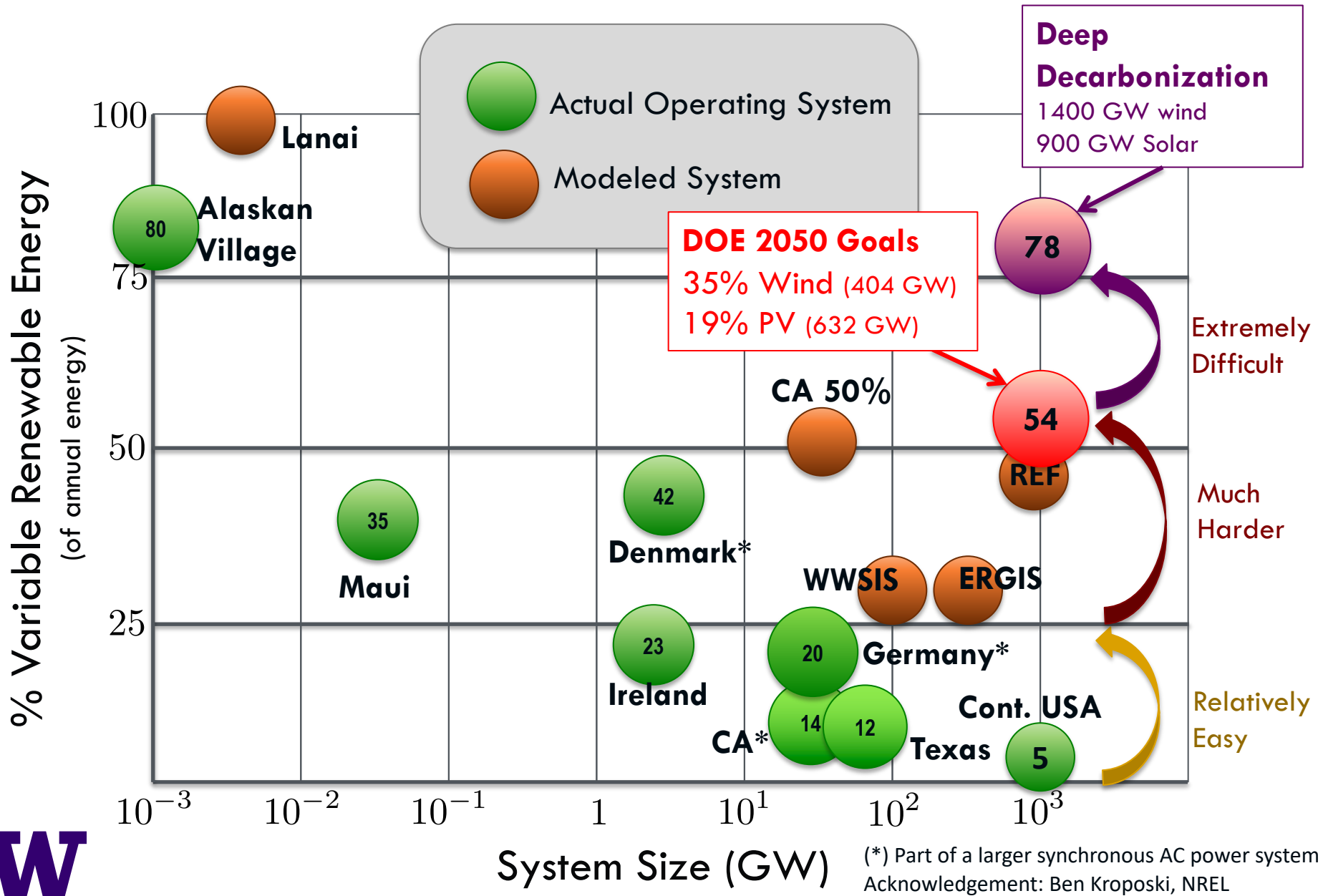
(\*) Part of a larger synchronous AC power system  
 Acknowledgement: Ben Kroposki, NREL



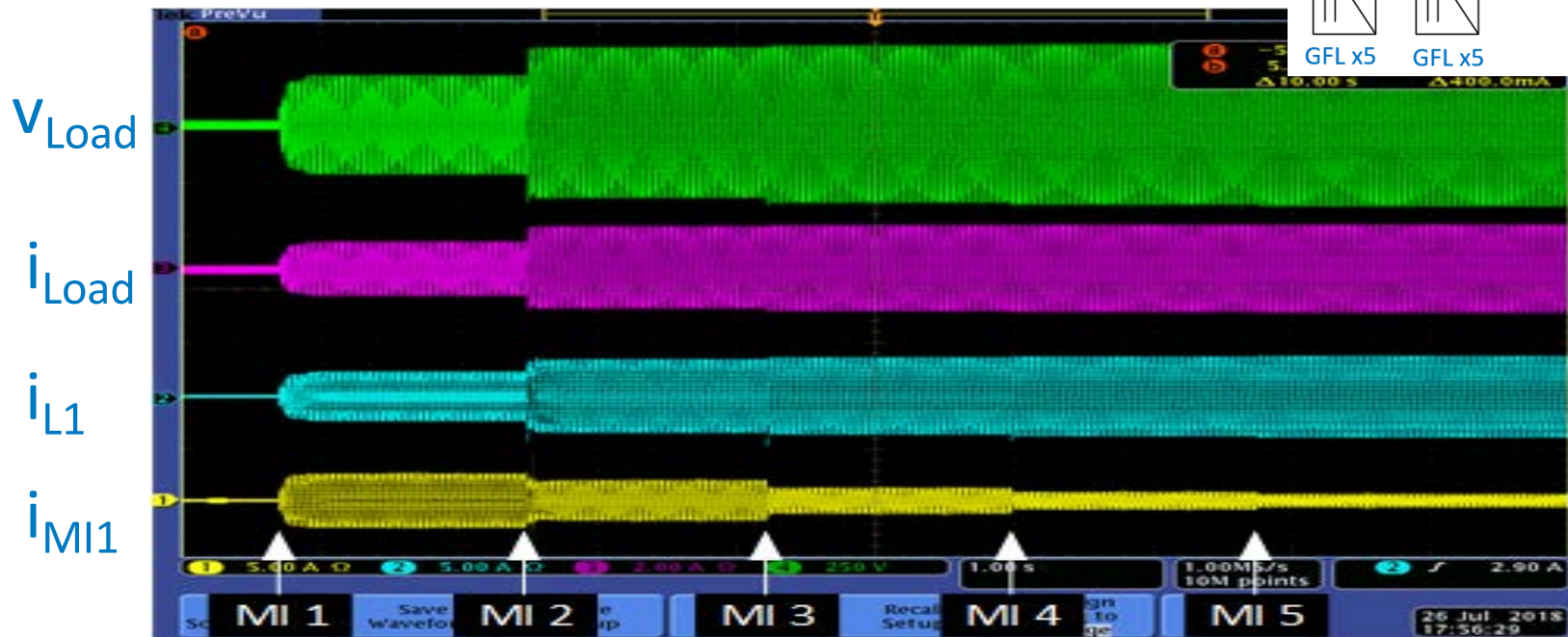
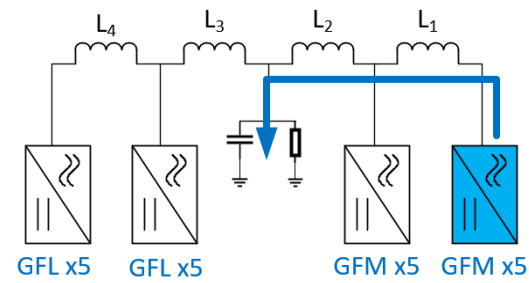
# Transforming the Grid at a Scale That Matters



# Transforming the Grid at a Scale That Matters

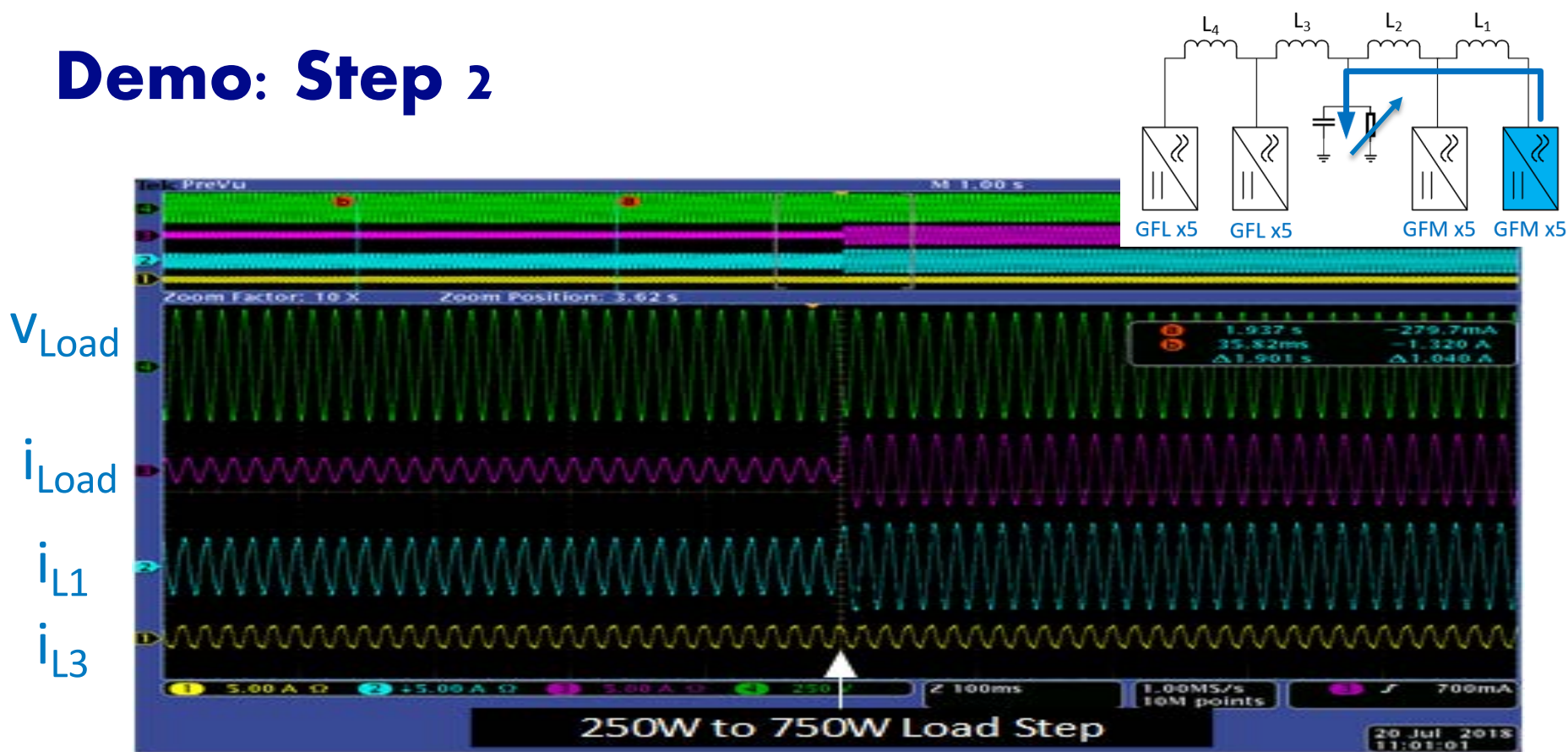


# Demo Step 1: Black-start



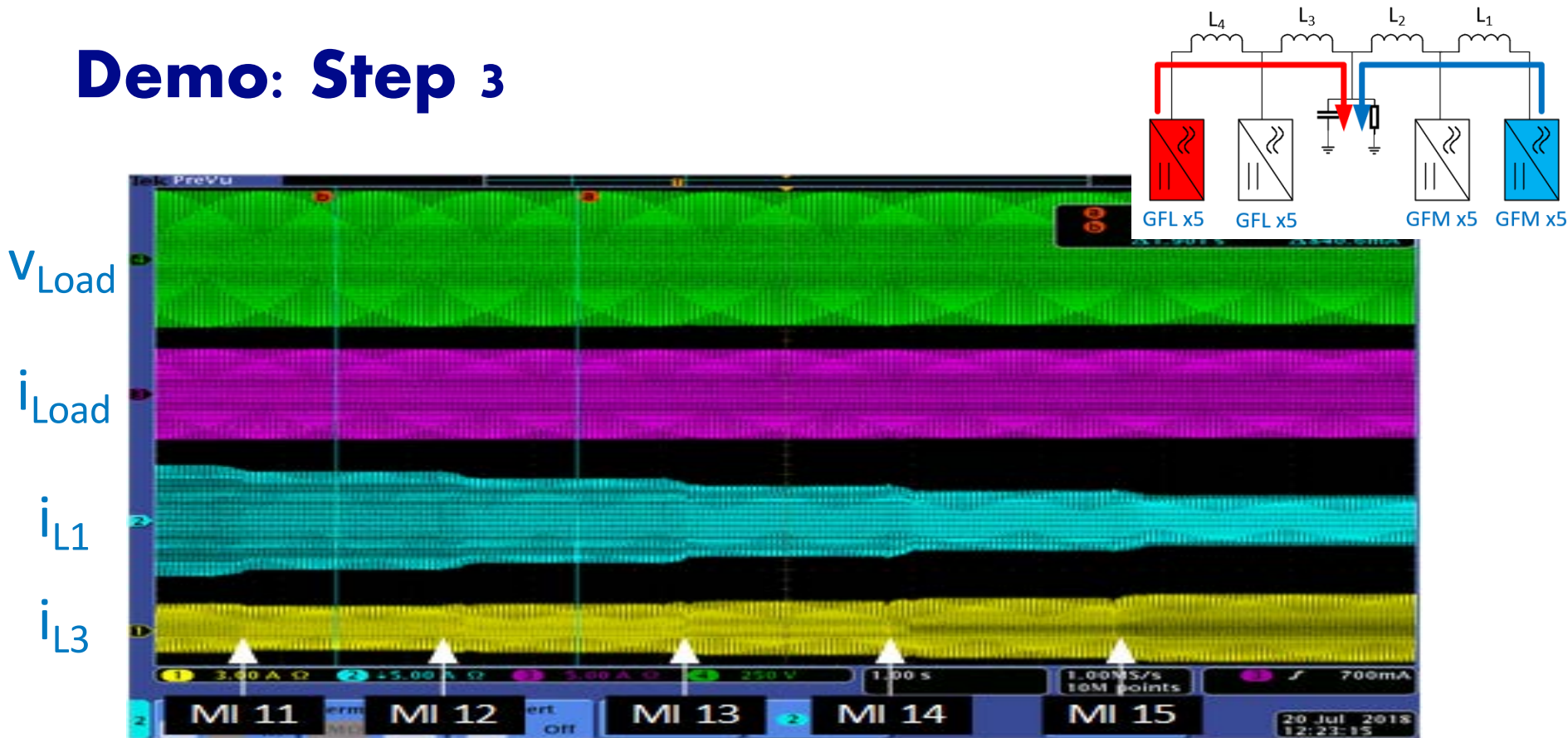
- Successful Black Start by Grid Forming Inverters under 250W condition
  - ✓ Black Start
  - ✓ Dynamic Load Sharing

# Demo: Step 2



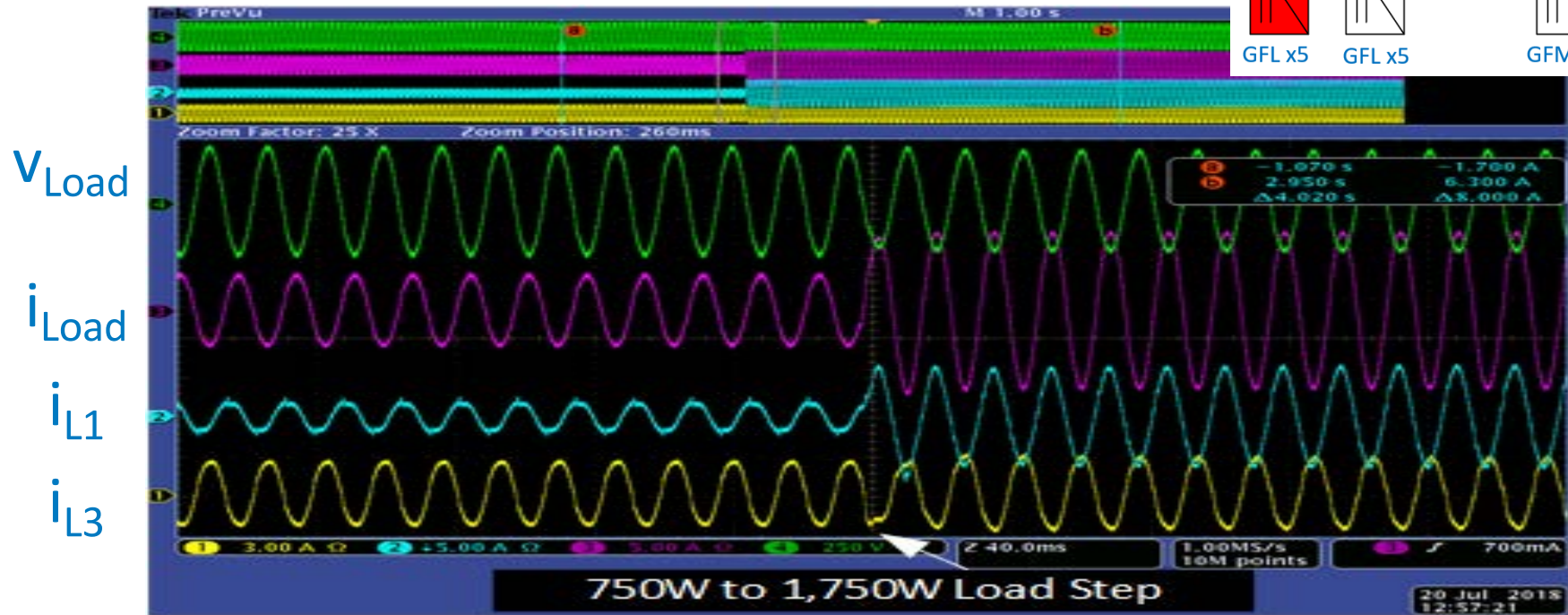
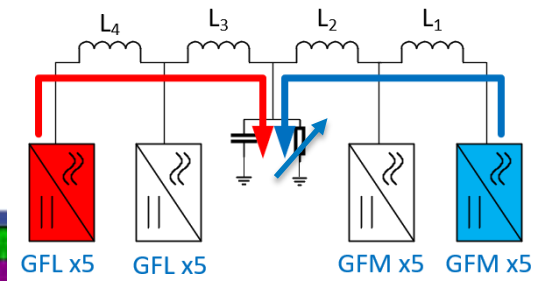
- Load transient from 250W to 750W with five inverters sharing the load
  - ✓ Dynamic Load Sharing
  - ✓ Transient Voltage Regulation

# Demo: Step 3



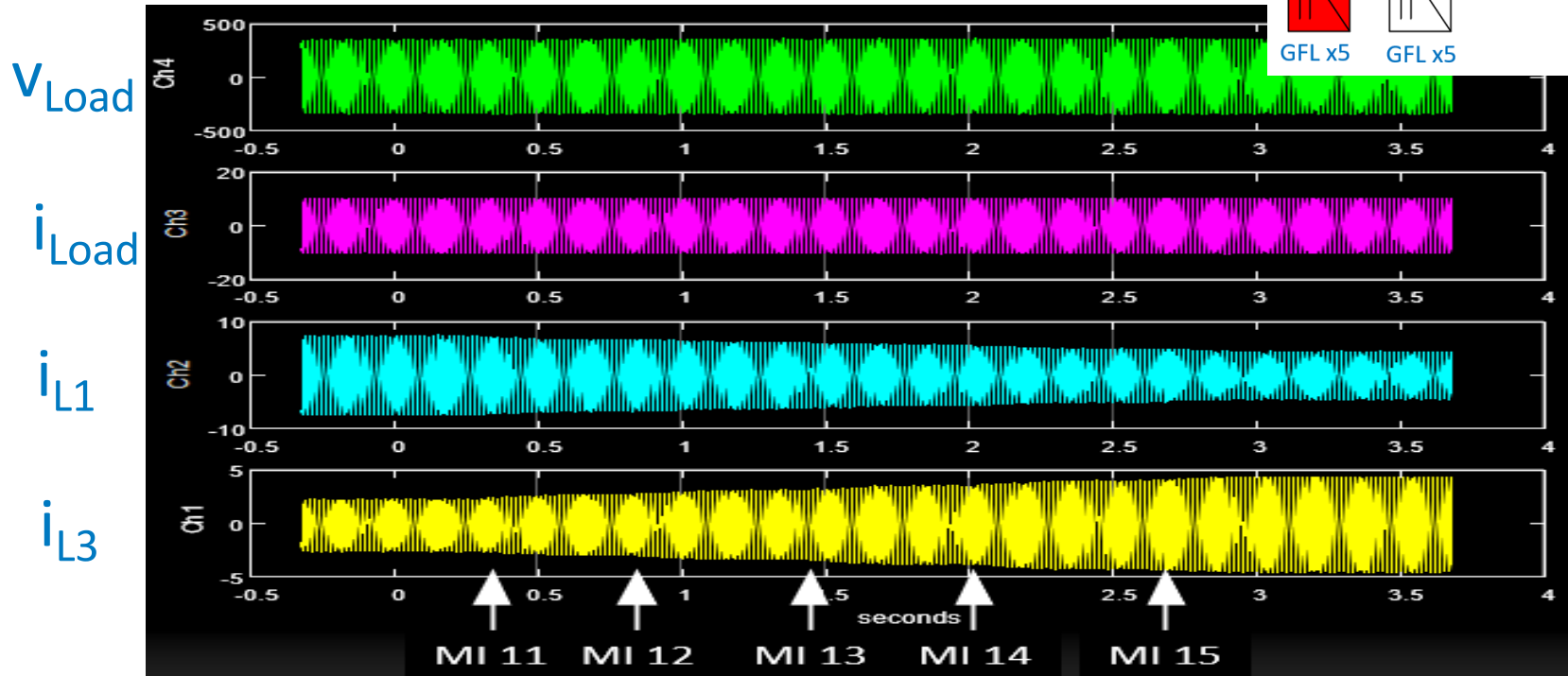
- Power Generation of Grid-Following Inverters
  - ✓ Grid Regulation under Grid-Following inverter operations
  - ✓ Compatibility with Grid Following Inverters
  - ✓ Tight Grid Voltage Regulation

# Demo: Step 4



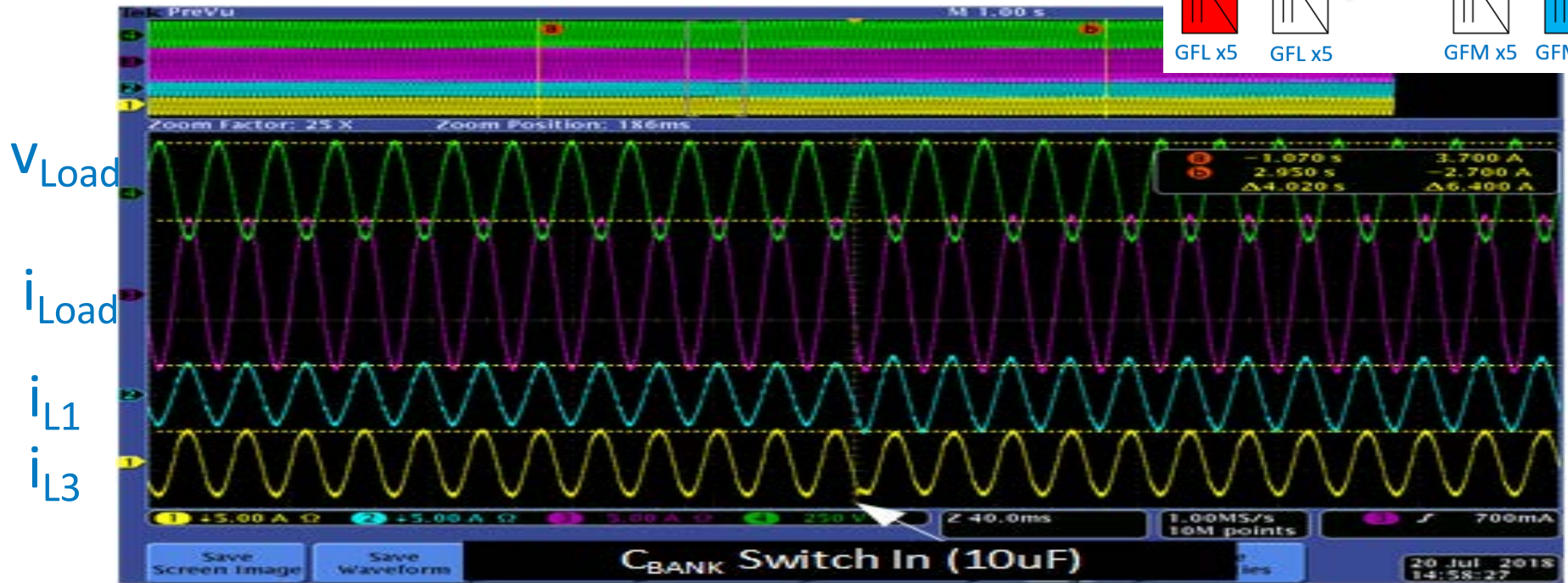
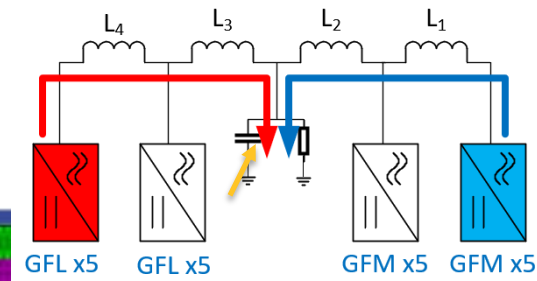
- Load Step from 750W to 1750W with 5 GFM MIs and 5 GFL MIs generating 500W
  - ✓ Grid Voltage Regulated by GFM MIs

# Demo: Step 5



- GFL Inverter Power Gen Increase to 200W
  - ✓ Grid Voltage Regulated by GFM MIs

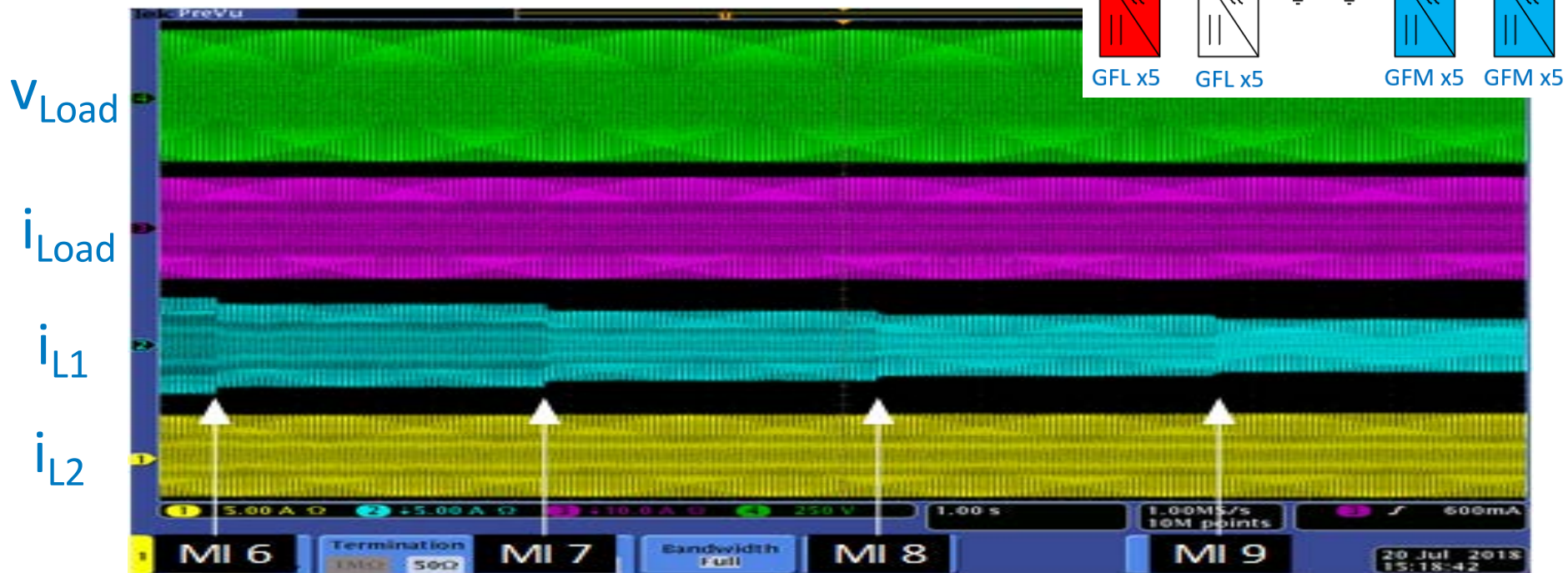
# Demo: Step 6



- 10uF Capacitive Load Turn on (Load Voltage Compensation Simulation)
  - ✓ Reactive Power Transient Covered By GFM

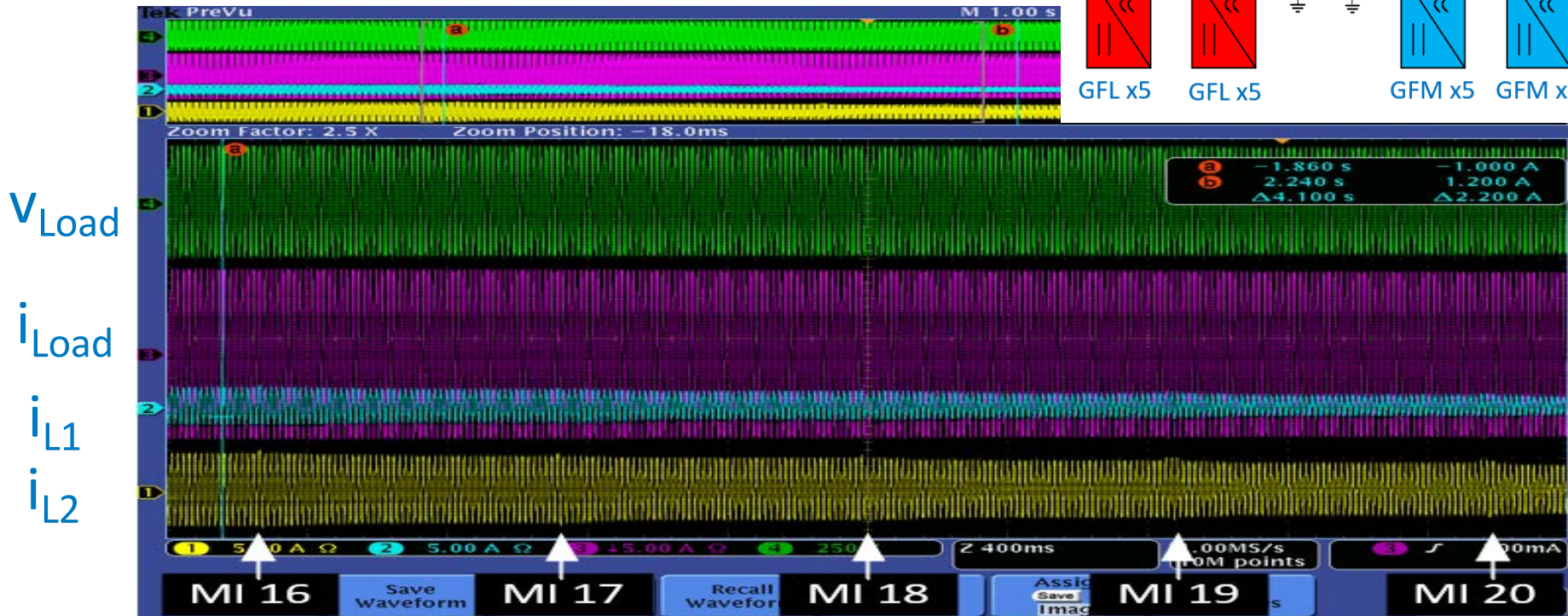
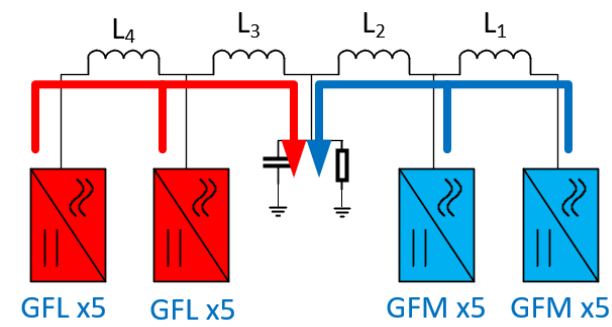


# Demo: Step 7



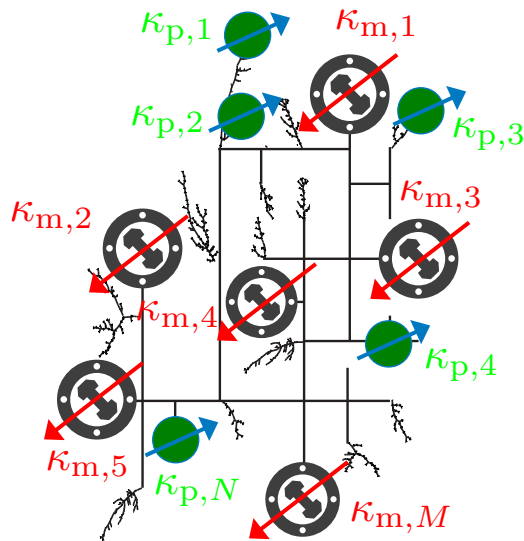
- GFM Inverters 6-10 Turned on to join
  - ✓ Successful Synchronization between GFM Inverters + Load Sharing

# Demo: Step 8



- GFL Inverters 16-20 Generate 250W
  - ✓ GFM Inverters Continue to Regulate Grid Voltage by Adjusting Their Power Generations Depending on the Load.

# Framework for Multi-Machine Multi-Inverter System



Network algebra:  $I = YV$

Machine & inverter dynamics:  $\dot{x} = f(x, u)$

inverter penetration :=  $\frac{\bar{P}_i}{(\bar{P}_i + \bar{P}_m)}$

- Start with zero inverter penetration  $\kappa_m = \text{nominal}, \kappa_p = 0$
1. Solve power flow to obtain machine/inverter terminal variables
  2. Compute machine/inverter equilibrium states  $\dot{x}^* = f(x^*, u) = 0$ 
    - Linearize, compute eigenvalues  $\lambda \in \mathbb{C}^{|x|}$ , assess stability
    - Increment  $\kappa_p$  or replace machine with inverter of equal rating