



**Research  
Symposium 2023**

# **PMSM Control Strategies in Consideration of Machine Nonidealities**

Dr. Heonyoung Kim

Renesas Electronics America

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# Outline

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- **Research Background and Objectives**
  - **Nonideal PMSM Model**
  - **Harmonic Identification of Back-EMF**
  - **Current Control Strategies of PMSMs with Non-sinusoidal Back-EMF**
  - **Impact on Power Loss**
  - **Impact on Extended Back-EMF Based Position Sensorless Control**
  - **Research Opportunities**
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# Research Background and Objectives

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## ▪ Non-idealities in PMSMs

- A limited number of stator and rotor core slots result in **non-uniform air-gap lengths** causing **machine parameters to have harmonic components** [1]
- **Non-uniform magnetic saturation** causes **cross-coupling of inductance** between  $d$ - and  $q$ -axes and **varying magnet flux linkage** with motor current [2]
- Nonideal characteristics become severe in low-cost or medium voltage motor applications with full-pitch and concentric coils

## ▪ Related Research Topic

1. Torque ripple reduction (Low speed)
    - Optimal design of the stator and rotor [3]-[5]
    - Optimal current reference and its control [6]-[10]
  2. Harmonic loss reduction control [8]
  3. Position sensorless control
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# Research Background and Objectives

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## ▪ Objectives

- Experimental identification of machine non-idealities
  - Sinusoidal current control scheme
    - 1) Efficiency improvement
    - 2) Improvement in angle estimation performance in EEMF based sensorless control
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# Nonideal PMSM Model

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## ▪ Nonideal IPMSM Model

$$v_{ds} = R_s i_{ds} + \frac{d}{dt} \lambda_{ds}(\theta_r) - \omega \lambda_{qs}(\theta_r)$$

$$\lambda_{ds}(\theta_r) = L_d(\theta_r) i_{ds} + L_{dq}(\theta_r) i_{qs} + \lambda_{dPM}(\theta_r)$$

$$v_{qs} = R_s i_{qs} + \frac{d}{dt} \lambda_{qs}(\theta_r) + \omega \lambda_{ds}(\theta_r)$$

$$\lambda_{qs}(\theta_r) = L_q(\theta_r) i_{qs} + L_{qd}(\theta_r) i_{ds} + \lambda_{qPM}(\theta_r)$$

$$L_d(\theta_r) = L_{d0} + L_{d6} \cos 6\theta_r + L_{d12} \cos 12\theta_r + \dots$$

$$L_{dq}(\theta_r) = L_{dq0} + L_{dq6} \sin 6\theta_r + L_{dq12} \sin 12\theta_r + \dots$$

$$L_q(\theta_r) = L_{q0} + L_{q6} \cos 6\theta_r + L_{q12} \cos 12\theta_r + \dots$$

$$L_{qd}(\theta_r) = L_{qd0} + L_{qd6} \sin 6\theta_r + L_{qd12} \sin 12\theta_r + \dots$$

$$\lambda_{dPM}(\theta_r) = \lambda_{dPM.0} + \lambda_{dPM.6} \cos 6\theta_r + \lambda_{dPM.12} \cos 12\theta_r \dots$$

$$\lambda_{qPM}(\theta_r) = \lambda_{qPM.0} + \lambda_{qPM.6} \sin 6\theta_r + \lambda_{qPM.12} \sin 12\theta_r \dots$$

- The triplen harmonics are absent in a Y-connected balanced 3-phase circuit
  - Other harmonics in order of  $(6n \pm 1)$  in abc frame are presented as multiples of 6<sup>th</sup> order harmonics in SRF
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# Nonideal PMSM Model

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## ▪ Simplified Nonideal IPMSM Model

$$v_{ds} = R_s i_{ds} + L_{d0} \frac{di_{ds}}{dt} - L_{q0} i_{qs} \omega_r + \lambda_{dPM} \omega_r \quad \lambda_{dPM} = \lambda_{dPM.0} + \lambda_{dPM.6} \cos 6\theta_r + \lambda_{dPM.12} \cos 12\theta_r \dots$$

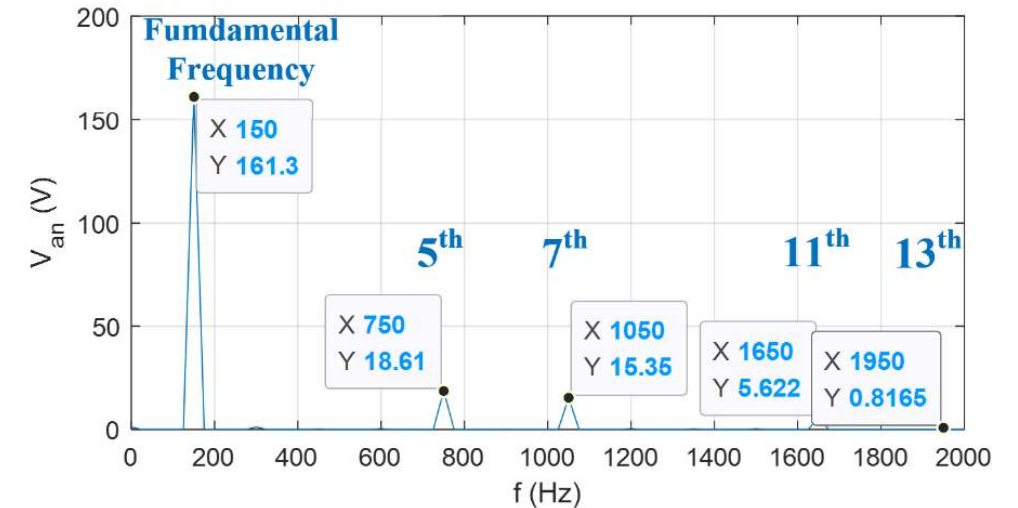
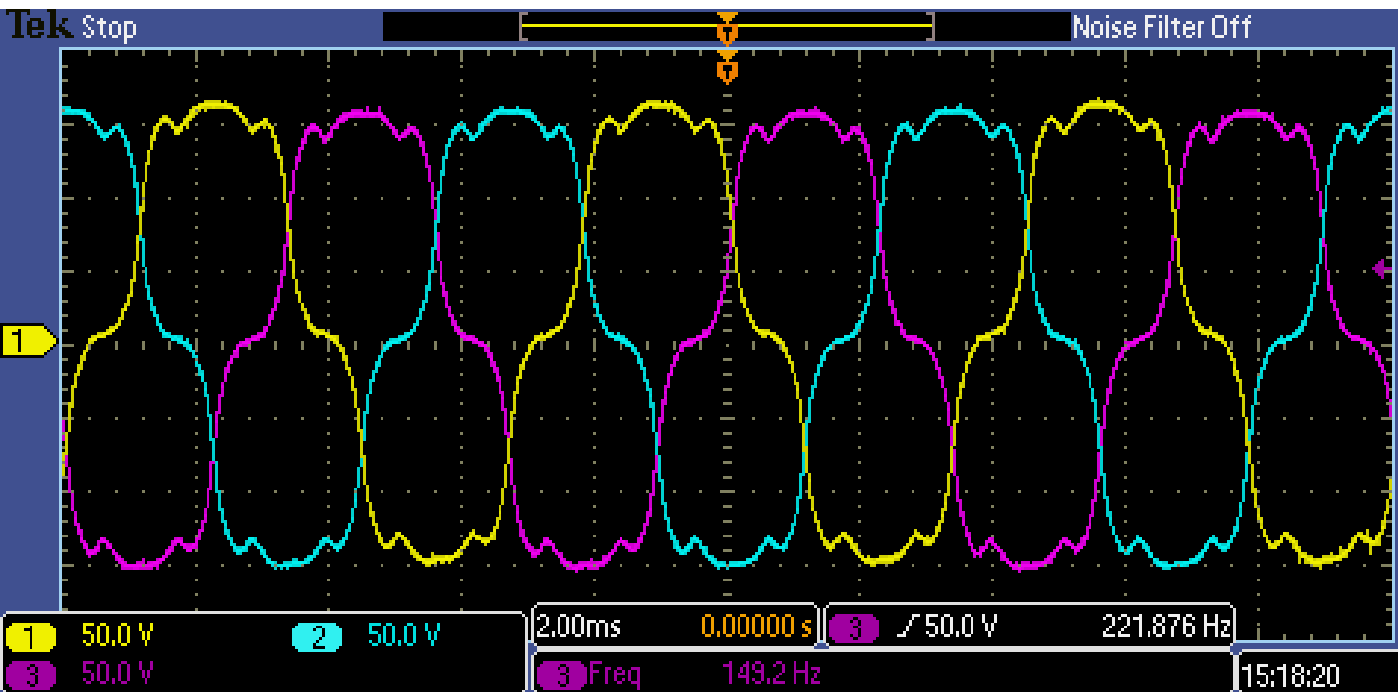
$$v_{qs} = R_s i_{qs} + L_{q0} \frac{di_{qs}}{dt} + L_{d0} i_{ds} \omega_r + \lambda_{qPM} \omega_r \quad \lambda_{qPM} = \lambda_{qPM.6} \sin 6\theta_r + \lambda_{qPM.12} \sin 12\theta_r \dots$$

$$T_e = \frac{3}{2} \frac{P}{2} \left[ \lambda_{dPM} i_{qs} + \lambda_{qPM} i_{ds} + (L_{d0} - L_{q0}) i_{qs} i_{ds} \right]$$

- If the motor is manufactured with a high-coercive PM, the effect of the inductance harmonics and mutual inductance is negligible compared to that of rotor magnet flux linkage harmonics [6], [11]
  - Assuming  $L_d = L_{d0} \quad L_q = L_{q0} \quad L_{dq} = L_{qd} = 0 \quad \lambda_{qPM.0} = 0$
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# Harmonic Identification of Back-EMF

## Offline Harmonic Identification



$f_{fund}$	$\lambda_{fund}$	$\lambda_{5th}$	$\lambda_{7th}$	$\lambda_{11th}$	$\lambda_{13th}$
50Hz	0.1714	0.0197	0.0165	0.0066	0.0008
100Hz	0.1711	0.0198	0.0164	0.0063	0.0009
150Hz	0.1715	0.0198	0.0163	0.0062	0.0009

\*Unit :  $Wb - t$

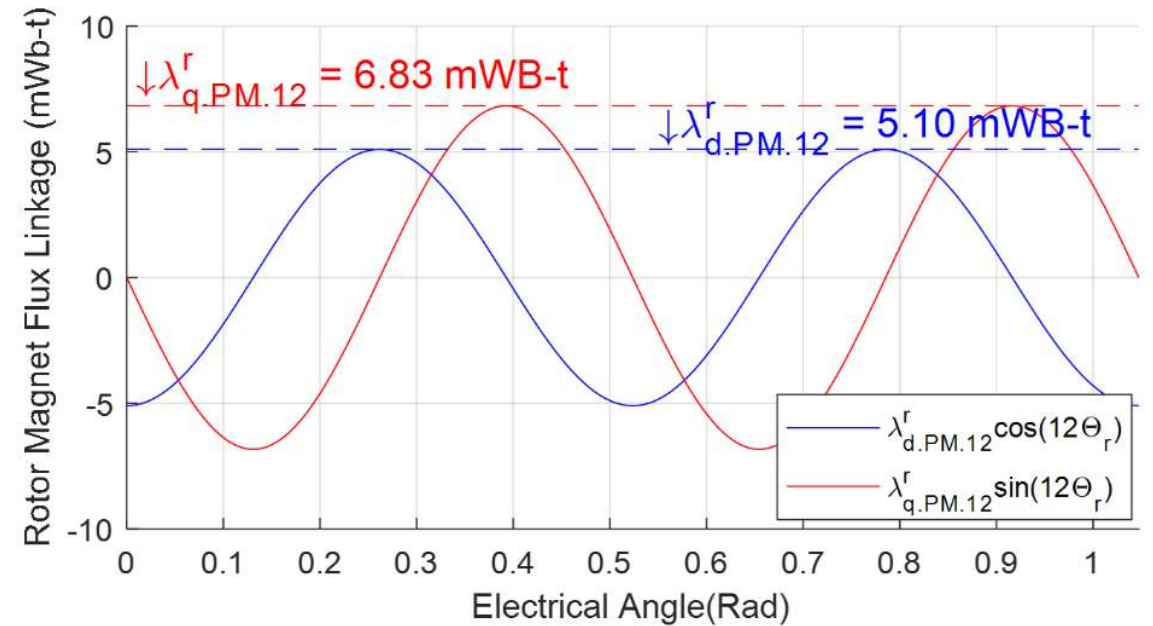
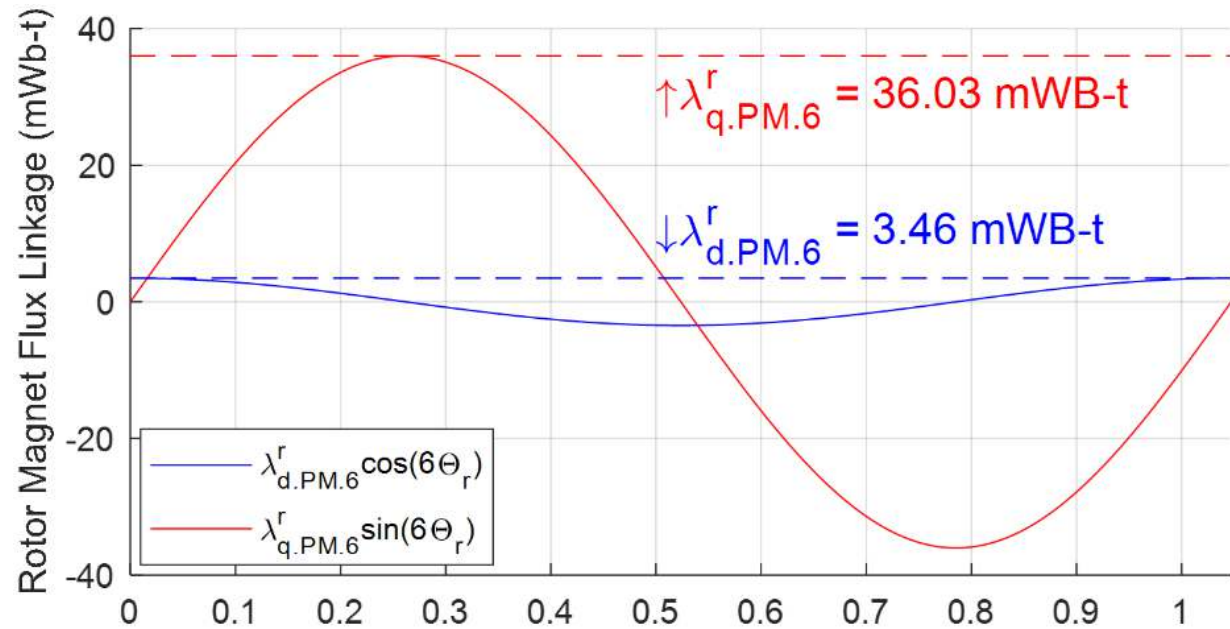
- The saturation effect cannot be considered with offline method
- Online identification is available in [12]

# Harmonic Identification of Back-EMF

## ▪ Rotor Magnet Flux Linkage Representation in SRF

$$v_{ds.emf} = \lambda_{qPM} \omega_r \quad \lambda_{dPM} = \lambda_{dPM.0} + \lambda_{dPM.6} \cos 6\theta_r + \lambda_{dPM.12} \cos 12\theta_r \dots$$

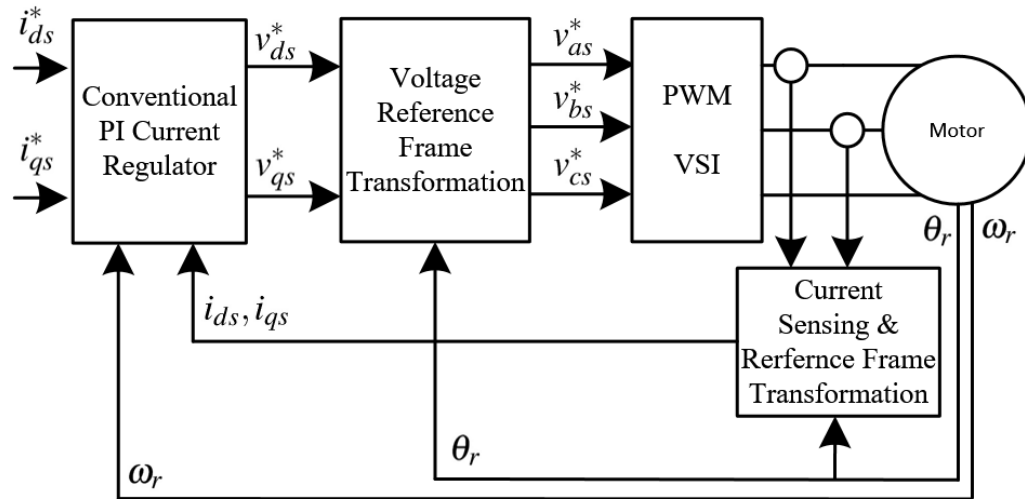
$$v_{qs.emf} = \lambda_{dPM} \omega_r \quad \lambda_{qPM} = \lambda_{qPM.6} \sin 6\theta_r + \lambda_{qPM.12} \sin 12\theta_r \dots$$



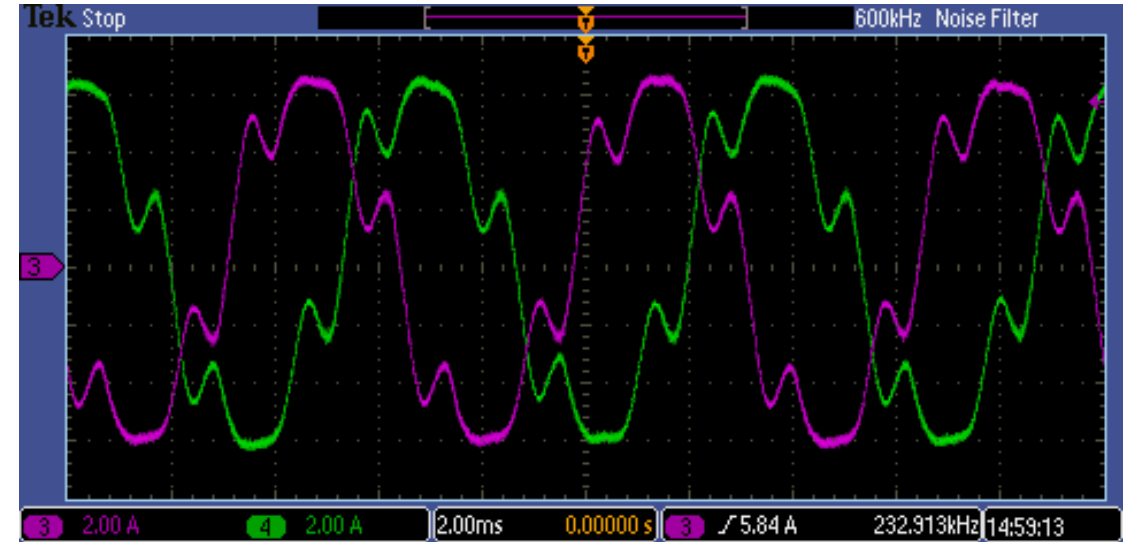


# Current Control of PMSMs with Non-sinusoidal Back-EMF

## ■ Conventional PI



- Controller mainly serves for the control of fundamental frequency components
- Multiples of 6<sup>th</sup> harmonic components cannot be handled properly

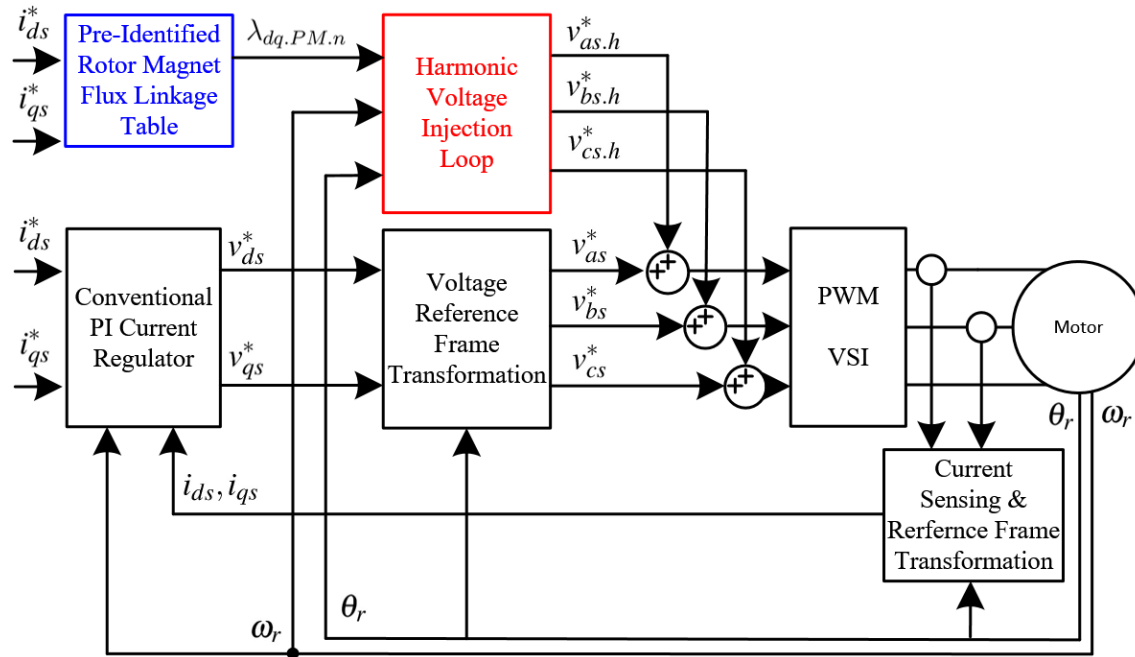


$T_{load}$	$I_{fund}$	$I_{5th}$	$I_{7th}$	$I_{11th}$	$I_{13th}$	THD
25%	1.50A	1.09A	0.90A	0.09A	0.02A	0.94
50%	2.98A	1.10A	0.89A	0.09A	0.02A	0.48
75%	4.49A	1.10A	0.88A	0.10A	0.03A	0.31
100%	6.04A	1.08A	0.87A	0.11A	0.03A	0.23

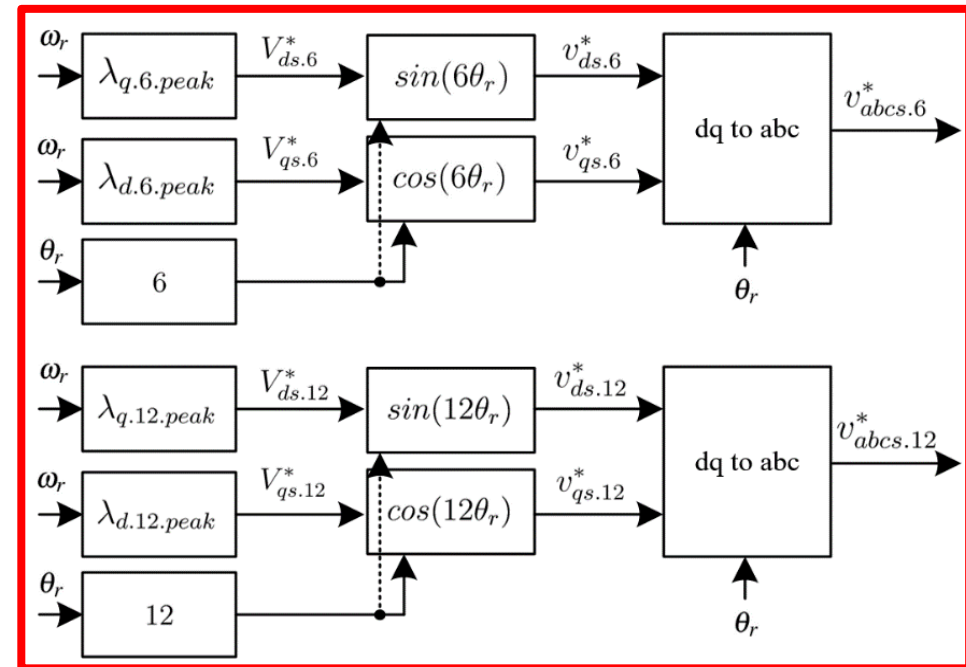
< Tested with various  $T_e$  >

# Current Control of PMSMs with Non-sinusoidal Back-EMF

## ■ Proposed Controller



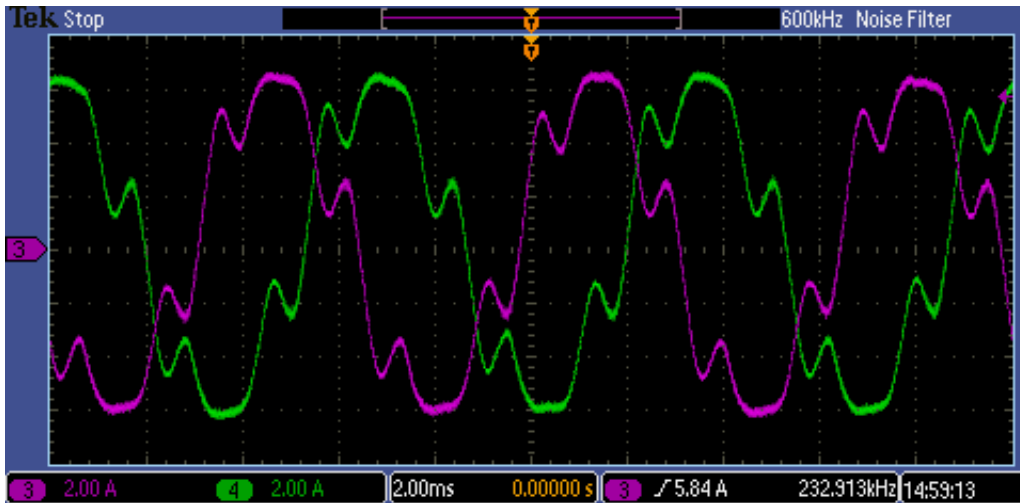
\* PIR controller is available in [12]



- Harmonic voltage injection loop appears as a feed-forward term
- 6<sup>th</sup> and 12<sup>th</sup> harmonic voltages are injected

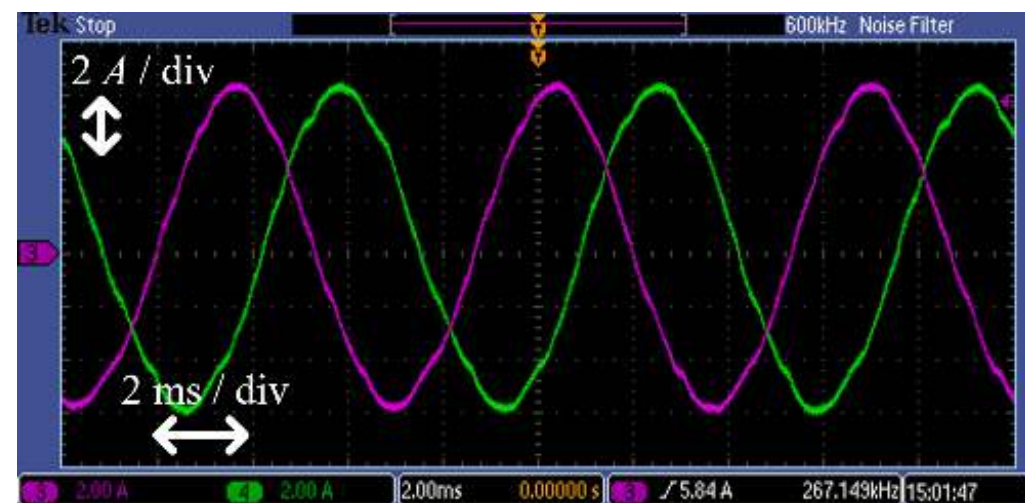
# Impact on THD

## THD Improvement



$T_{load}$	$I_{fund}$	$I_{5th}$	$I_{7th}$	$I_{11th}$	$I_{13th}$	THD
25%	1.50A	1.09A	0.90A	0.09A	0.02A	0.94
50%	2.98A	1.10A	0.89A	0.09A	0.02A	0.48
75%	4.49A	1.10A	0.88A	0.10A	0.03A	0.31
100%	6.04A	1.08A	0.87A	0.11A	0.03A	0.23

< Conventional PI >

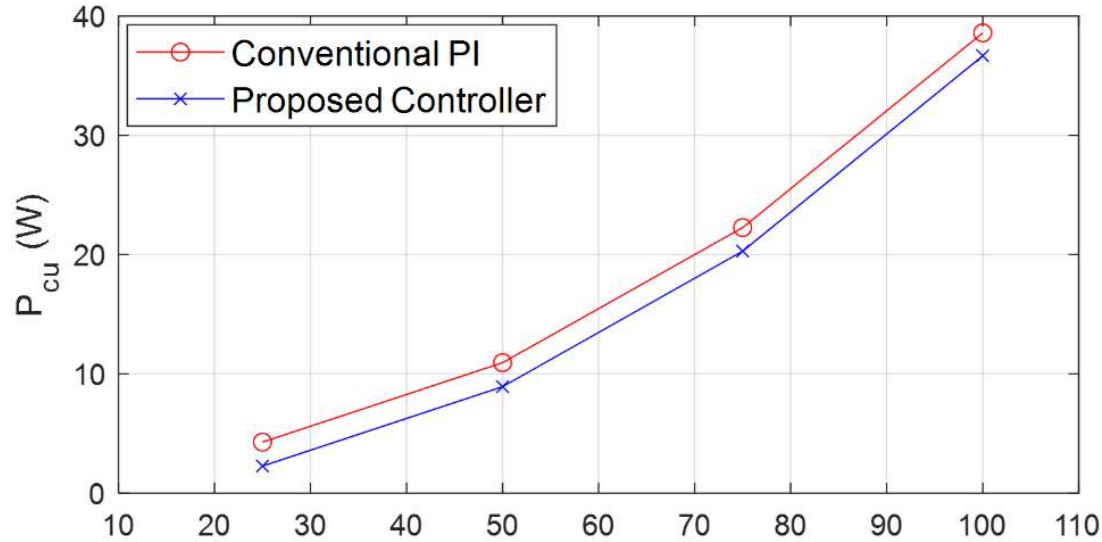


$T_{load}$	$I_{fund}$	$I_{5th}$	$I_{7th}$	$I_{11th}$	$I_{13th}$	THD
25%	1.51A	0.05A	0.06A	0.04A	0.01A	0.06
50%	3.00A	0.10A	0.03A	0.03A	0.02A	0.04
75%	4.48A	0.09A	0.05A	0.08A	0.02A	0.03
100%	5.98A	0.08A	0.05A	0.07A	0.02A	0.02

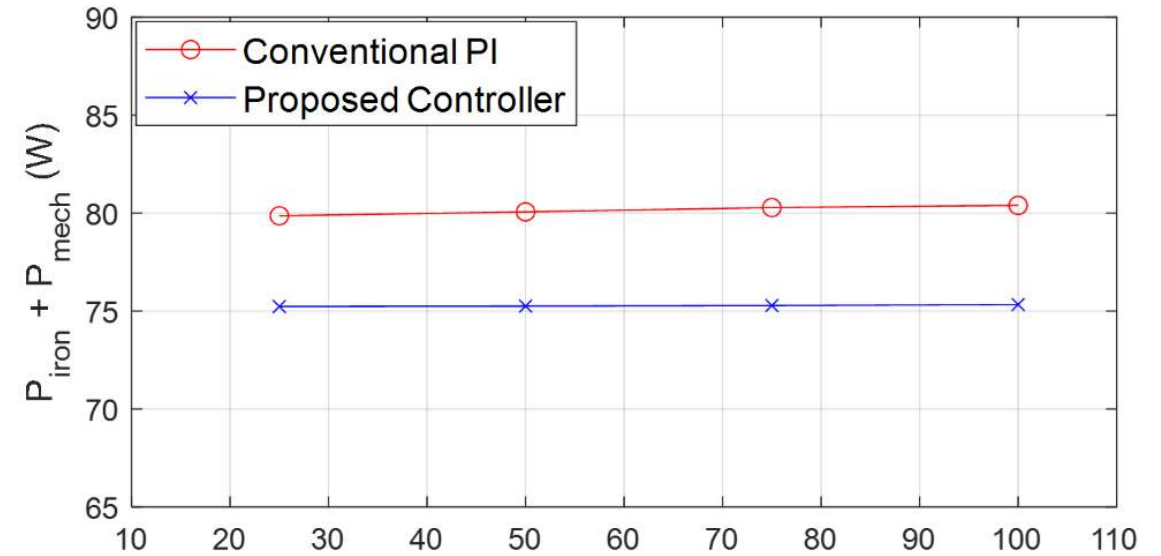
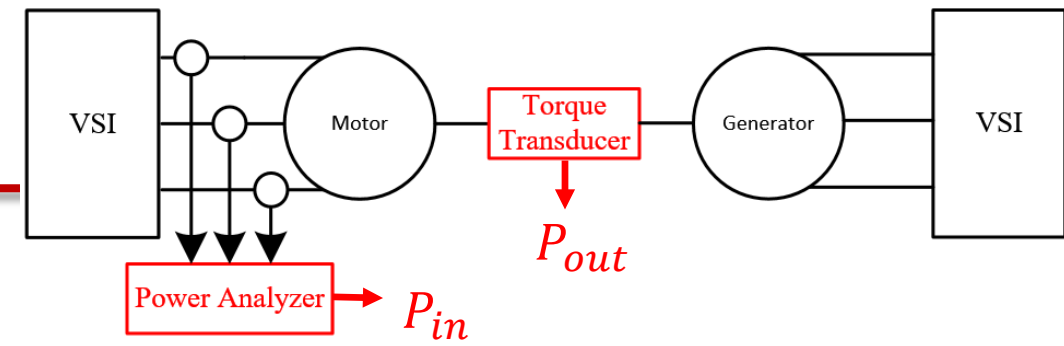
< Proposed Control >

# Impact on Power Loss

## Power Loss Improvement



$T_L$	25%	50%	75%	100%
$\Delta P_{cu}$	2.02W	2.02W	2.01W	1.95W
$\Delta P_{iron}$	4.63W	4.81W	5.00W	5.06W
$\Delta P_{total}$	6.65W	6.83W	7.01W	7.01W
$\Delta \eta$	1.77%	0.91%	0.62%	0.47%



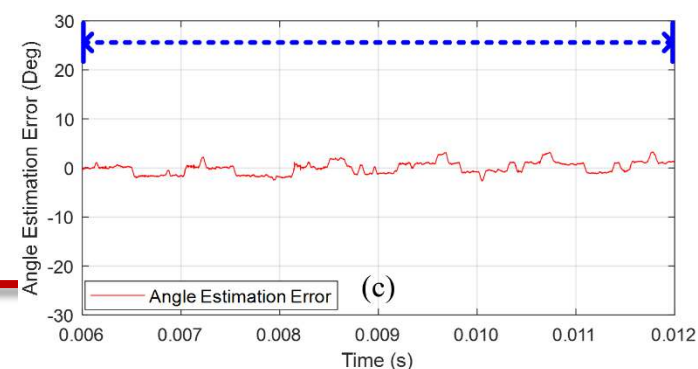
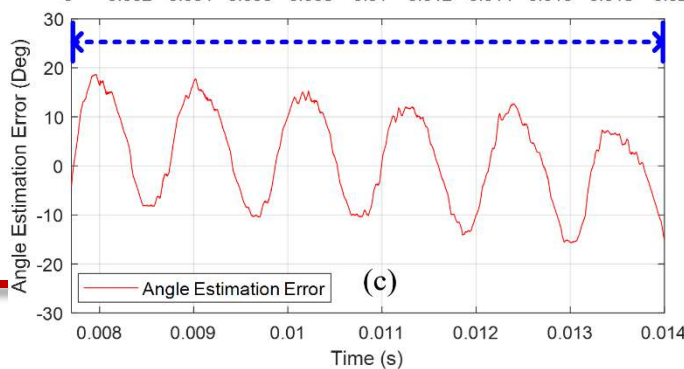
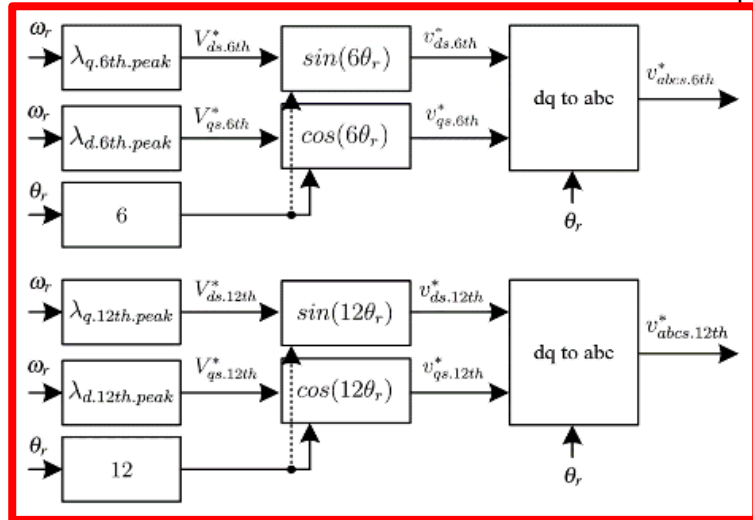
$$\Delta P_{total} = \Delta P_{cu} + \Delta P_{iron}$$

$$P_{cu} = R_s (I_{Arms}^2 + I_{Brms}^2 + I_{Crms}^2)$$

$$P_{iron} + P_{mech} = P_{in} - P_{out} - P_{cu}$$

$$\Delta \eta = \frac{\Delta P_{total}}{P_{in}}$$

- **Angle Estimation Improvement [13]**



# Ongoing Research

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- Injecting optimal 6<sup>th</sup> and 12<sup>th</sup> harmonic currents to reduce torque ripple in low-speed range [10]
  - Current control for minimizing cross-coupling effect [14]
  - Sensorless control for low-speed range
  - Experimental harmonic identification of self- and cross-coupling inductance
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# References

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**Q & A**

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